

# Sparse, Empirically Optimized Quadrature for Broadband Radiative Fluxes and Heating Rates

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Applied Physics and Applied Math, Columbia University

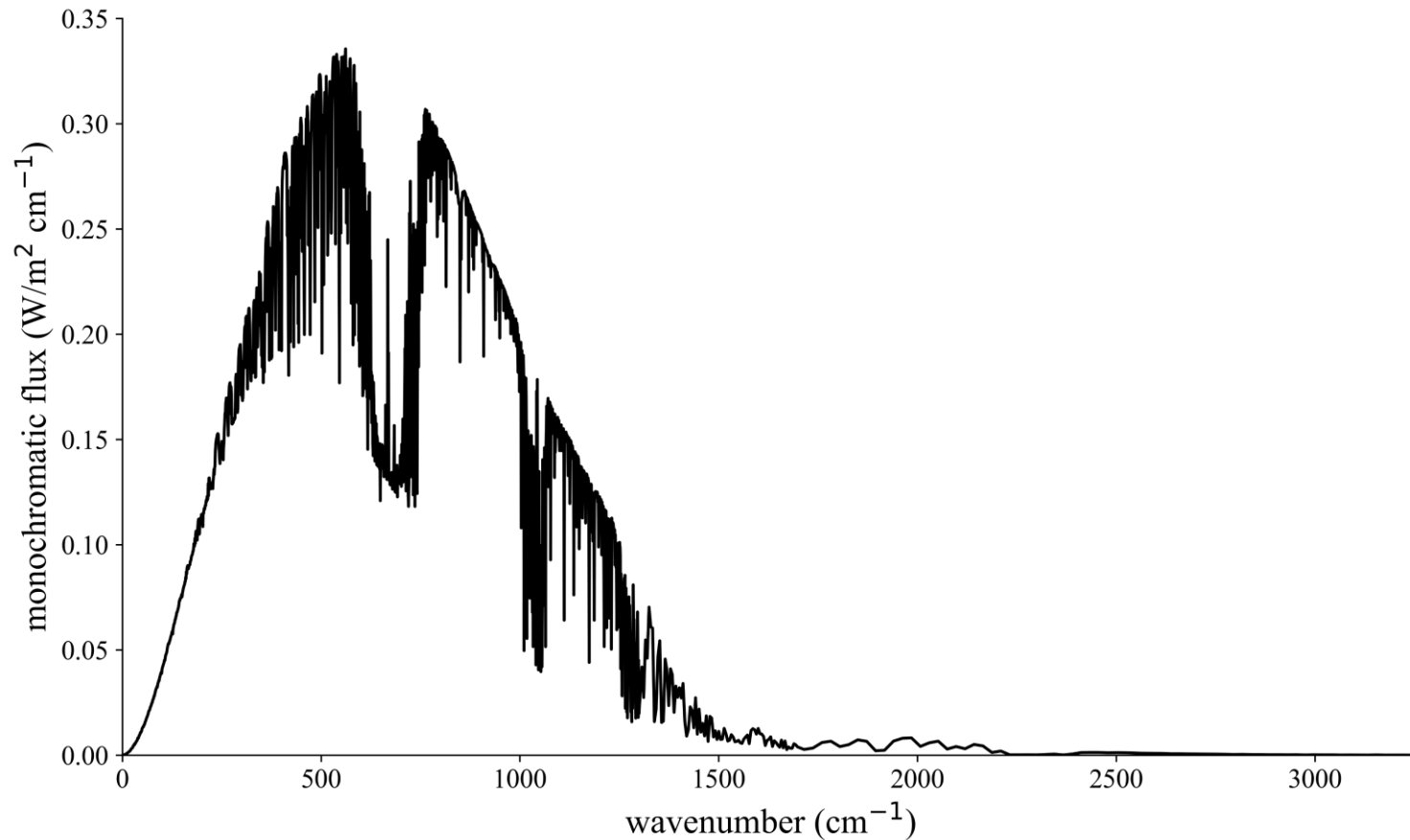
Advised by: Robert Pincus and Lorenzo Polvani

**NASA CERES Meeting**

**October 18<sup>th</sup>, 2023**

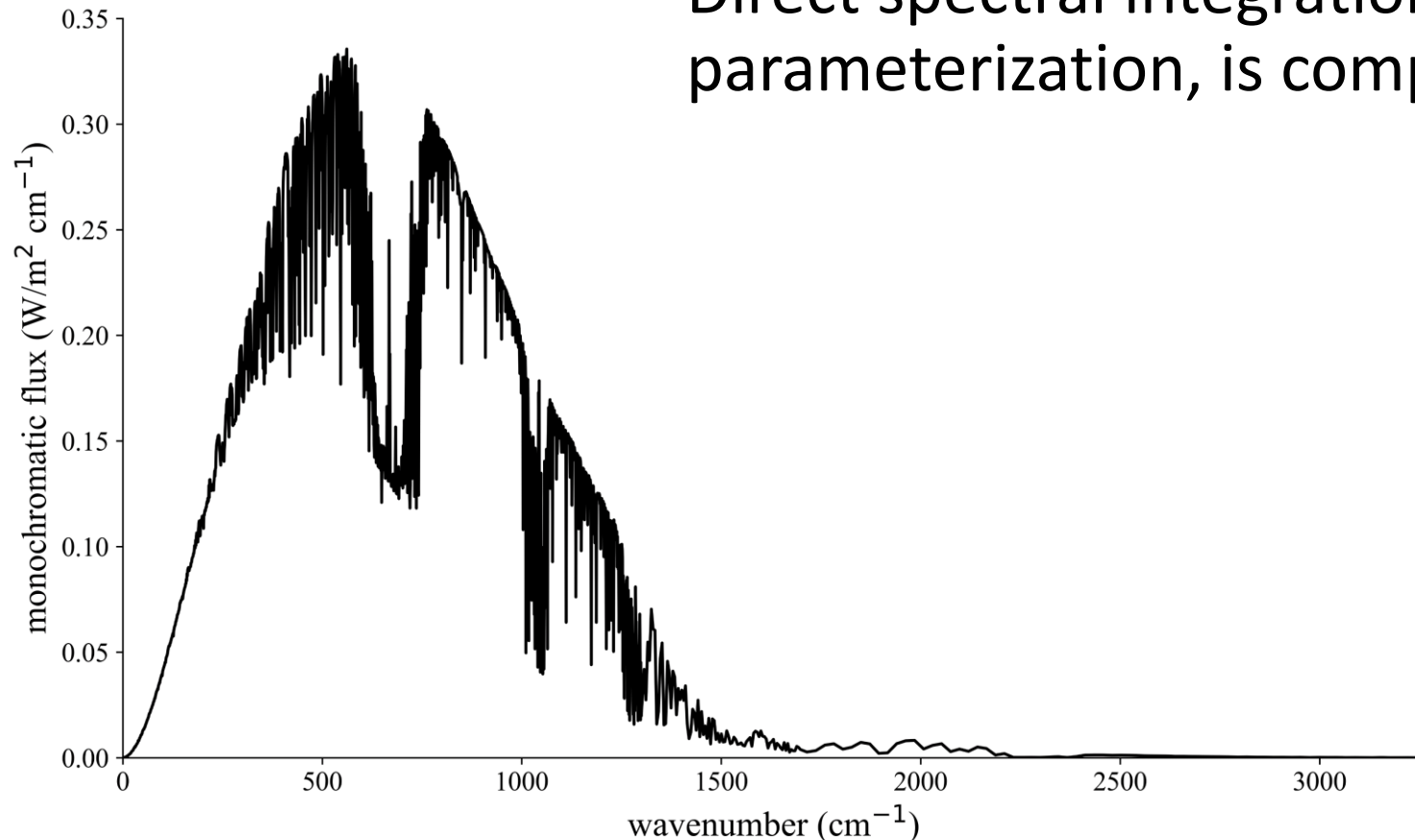
# Calculating Radiative Quantities

- Physics of radiative transfer is well-known



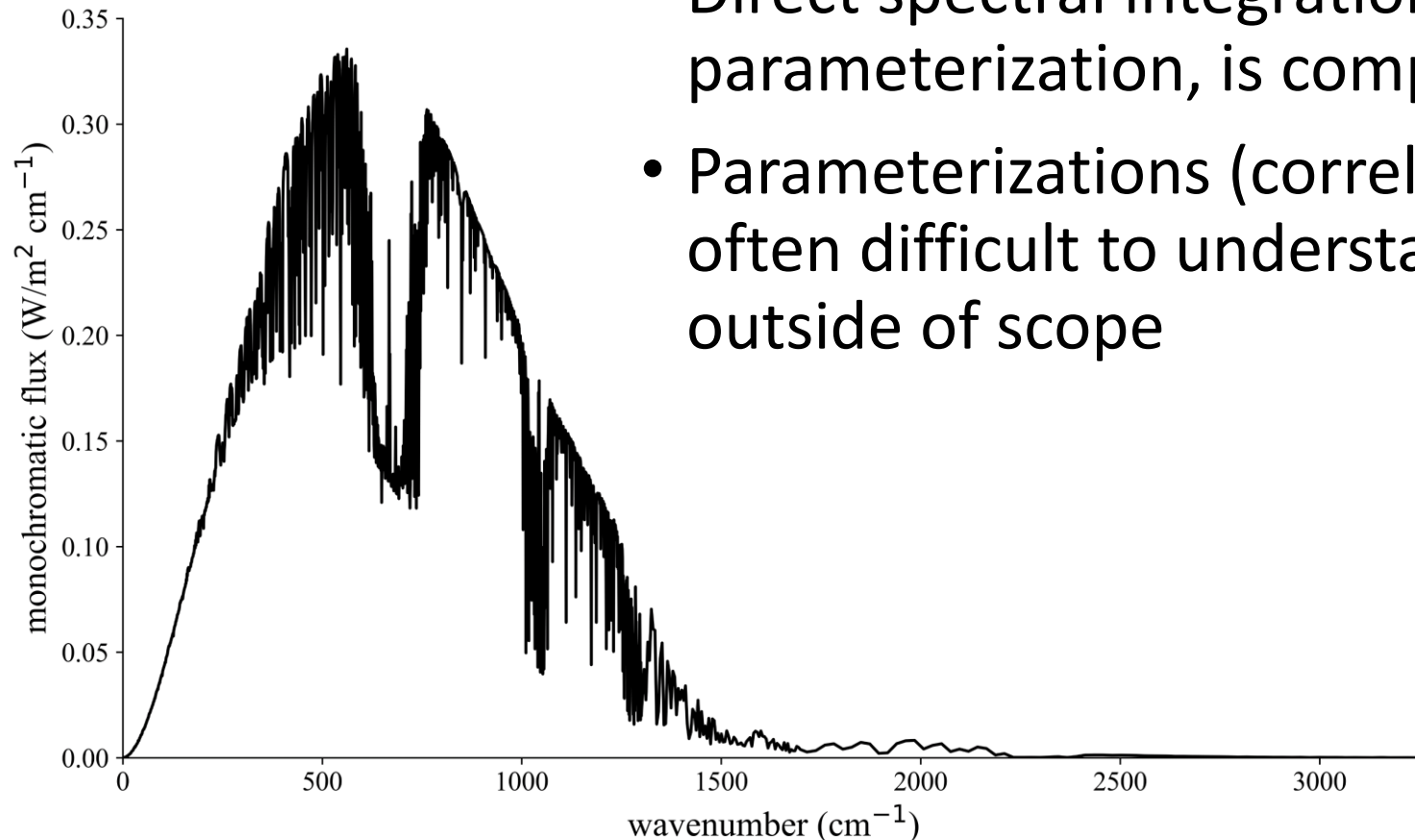
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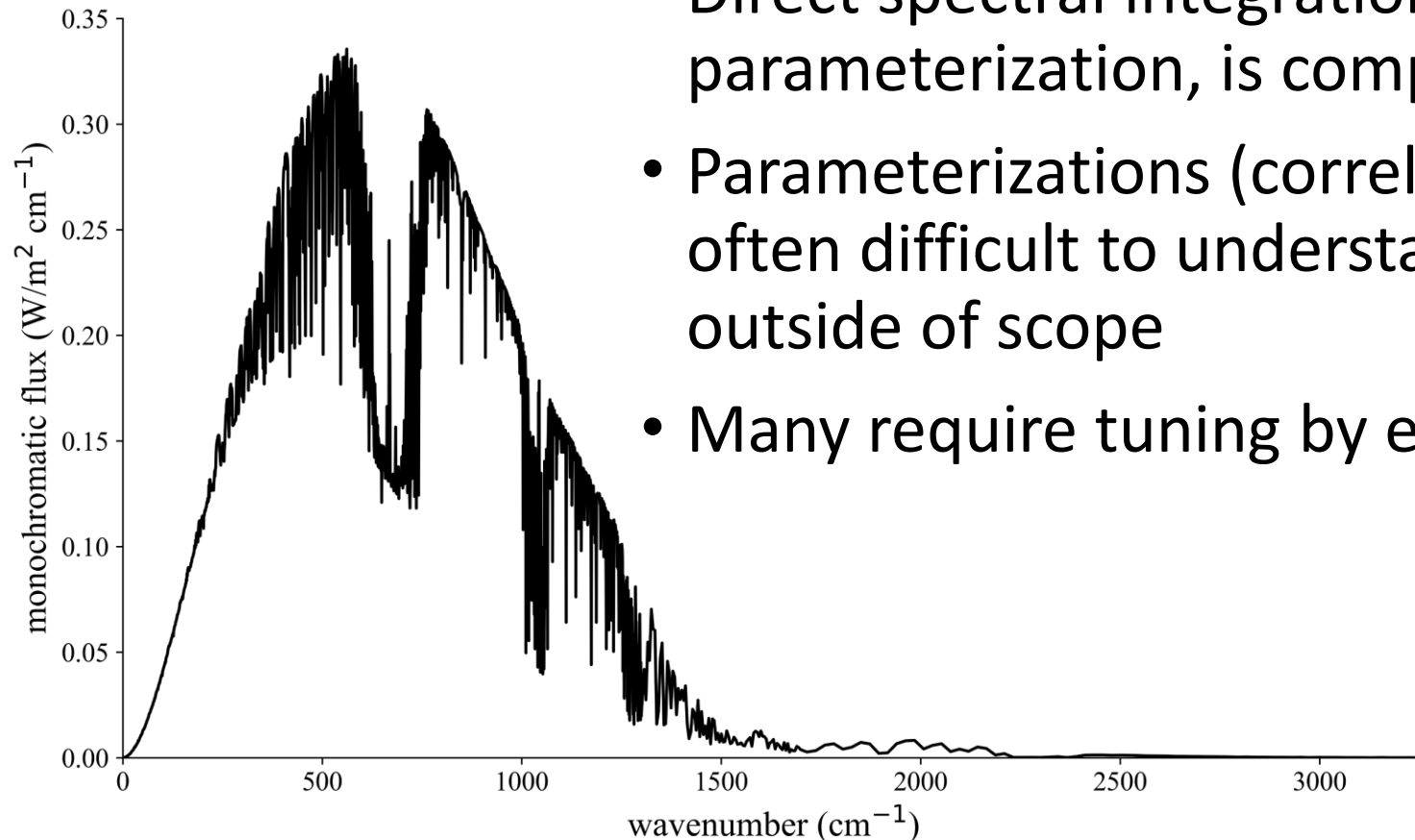
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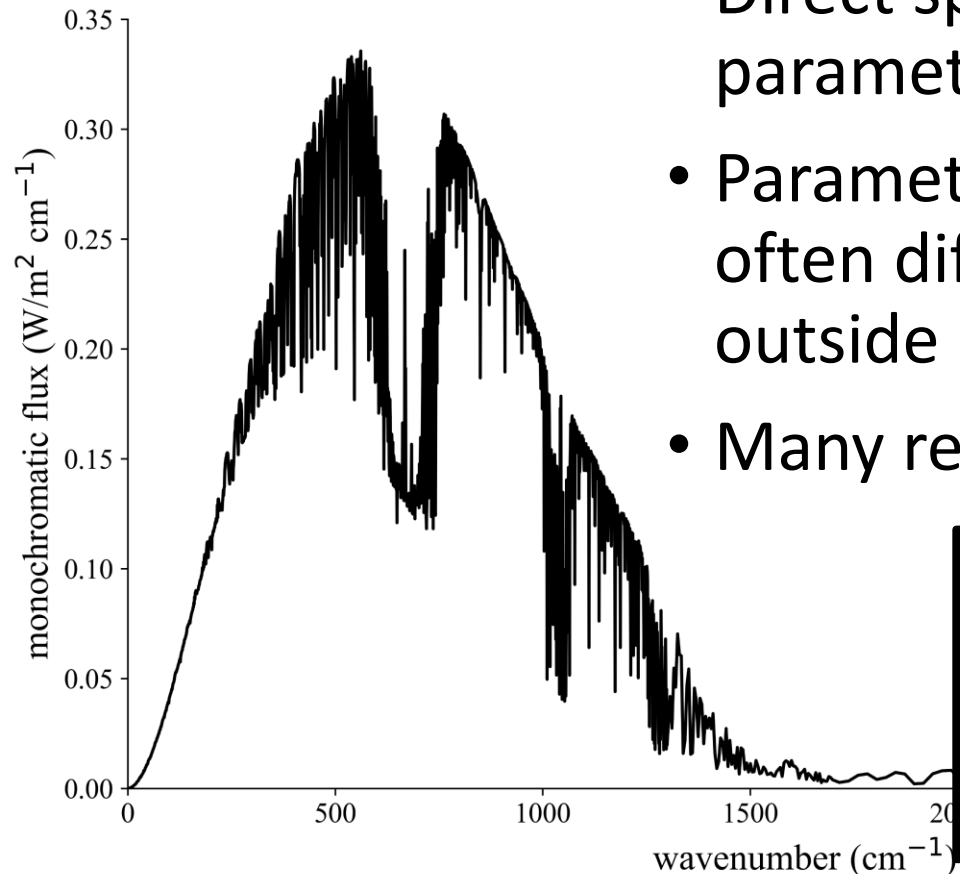
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**Aim: create an alternative method that is easy to understand and customizable to different problems**

# Proposed Approach

- Can we sparsely sample the spectrum instead?

Strongly inspired by Buehler et al., 2010; Moncet et al., 2008

$$F_{int} = \int F_{\nu} d\nu \approx \sum_i F_{\nu_i} \Delta\nu_i$$

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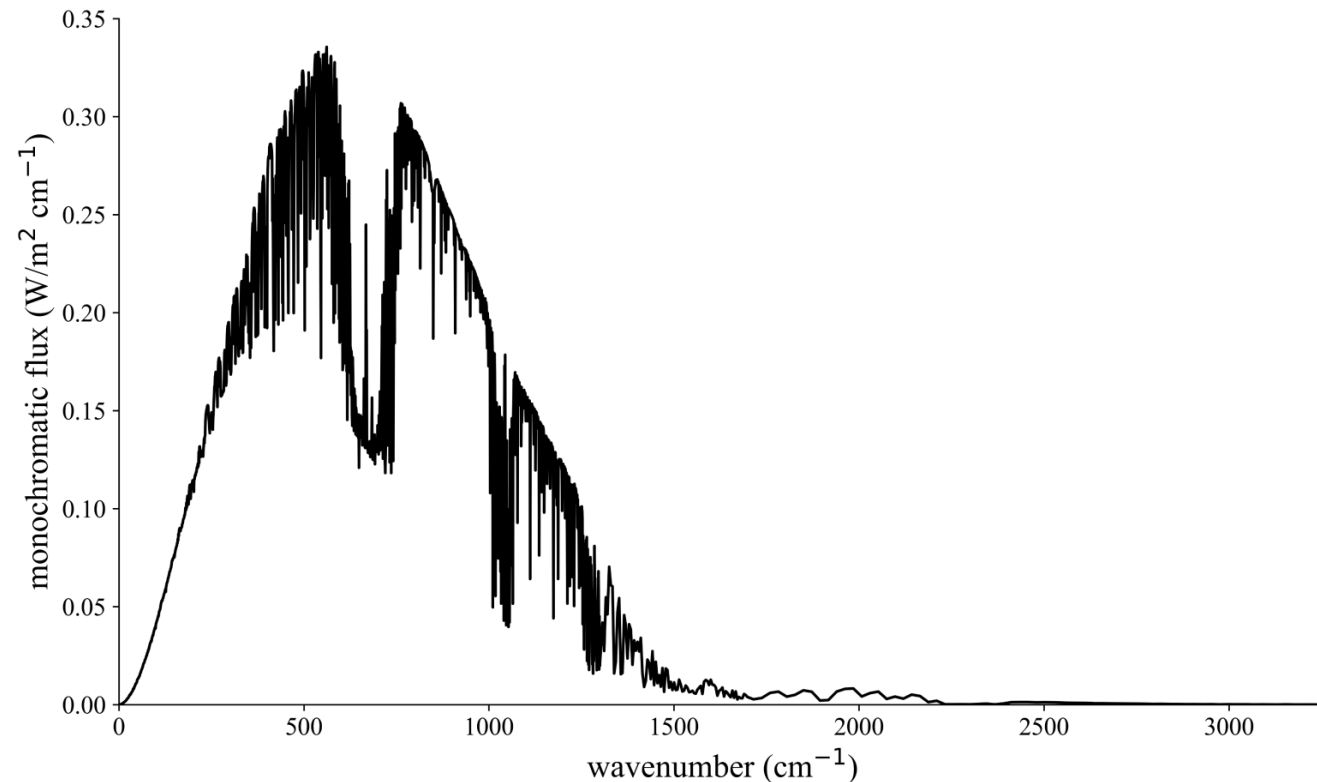
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- Two parts of the problem:
  - Predict the total flux with linear weights
  - Optimize the subset using simulated annealing

# Training and Testing Data

- CKDMIP: high-resolution spectral fluxes and broadband reference calculations
  - Two independent datasets, 50 atmospheric profiles, 55 vertical levels, 7 million wavenumbers
- Here – present-day clear-sky longwave fluxes
  - Variation only in water vapor, temperature, and ozone





# Flux Profiles

$$C = \|H_{est} - H_{ref}\| + f\|F_{est} - F_{ref}\|$$

# Flux Profiles

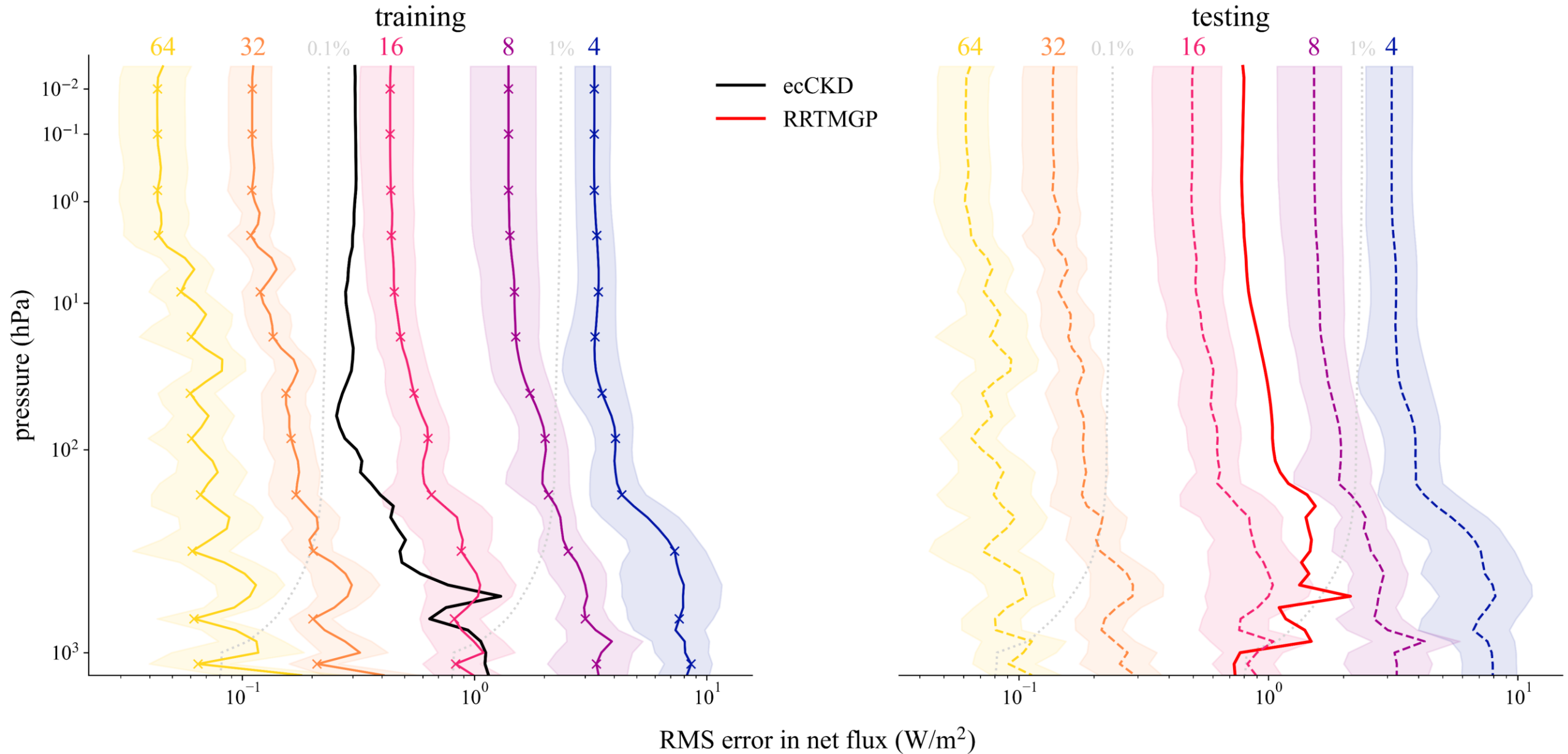
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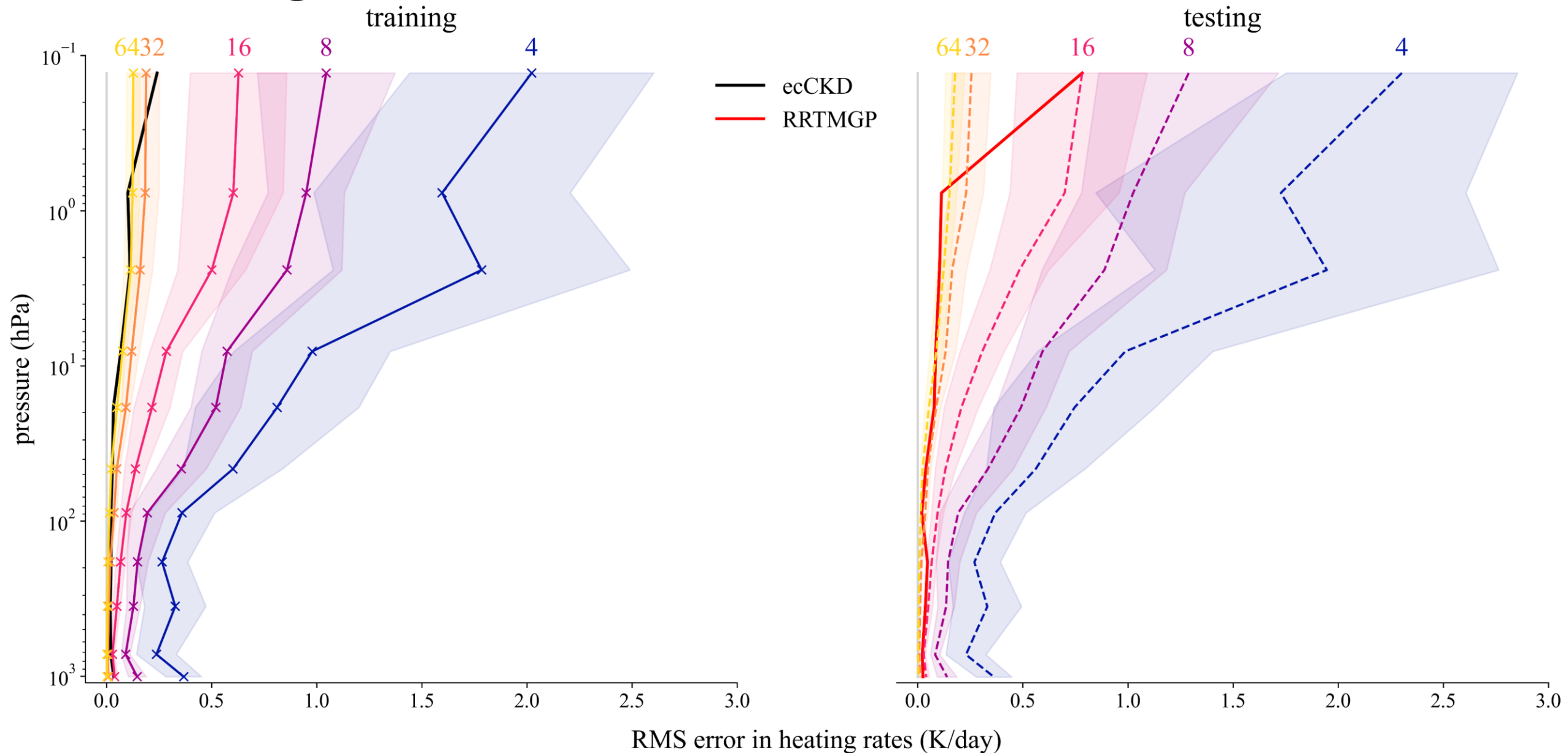
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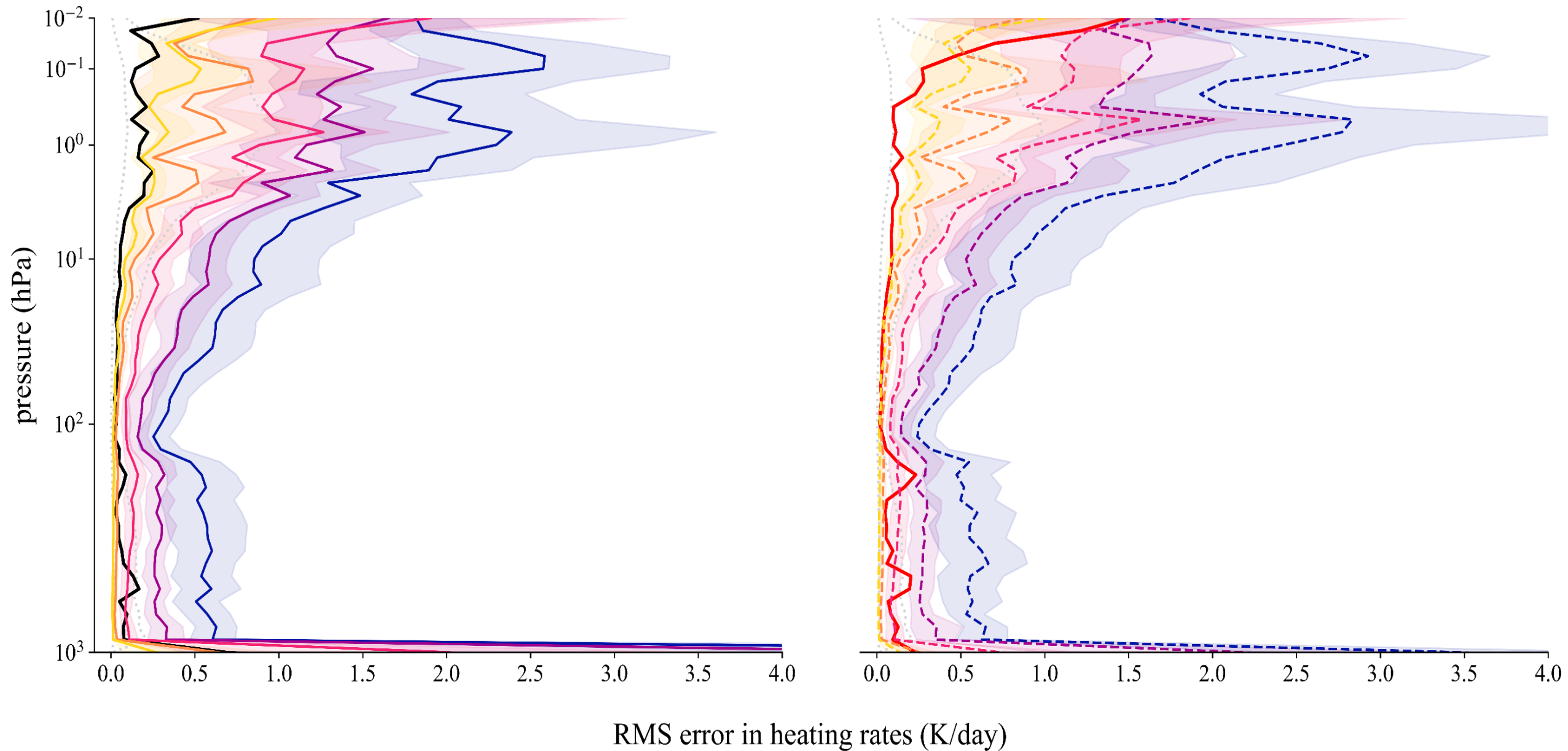
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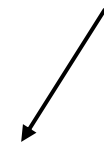
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Forcing by CO<sub>2</sub>  $C = \|H_{est} - H_{ref}\| + f\|F_{est} - F_{ref}\| + \|\mathcal{F}_{est} - \mathcal{F}_{ref}\|$

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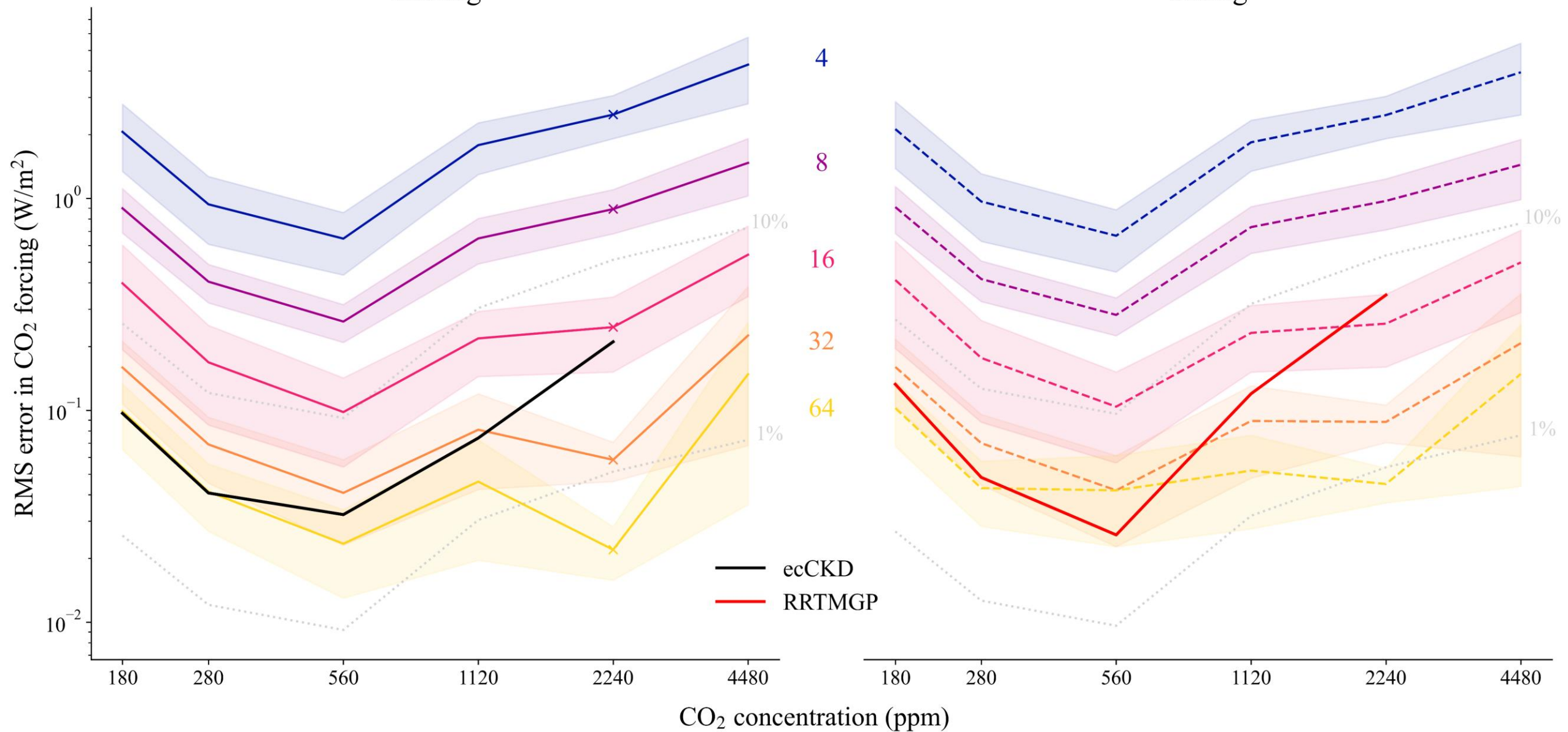
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8 x CO<sub>2</sub>

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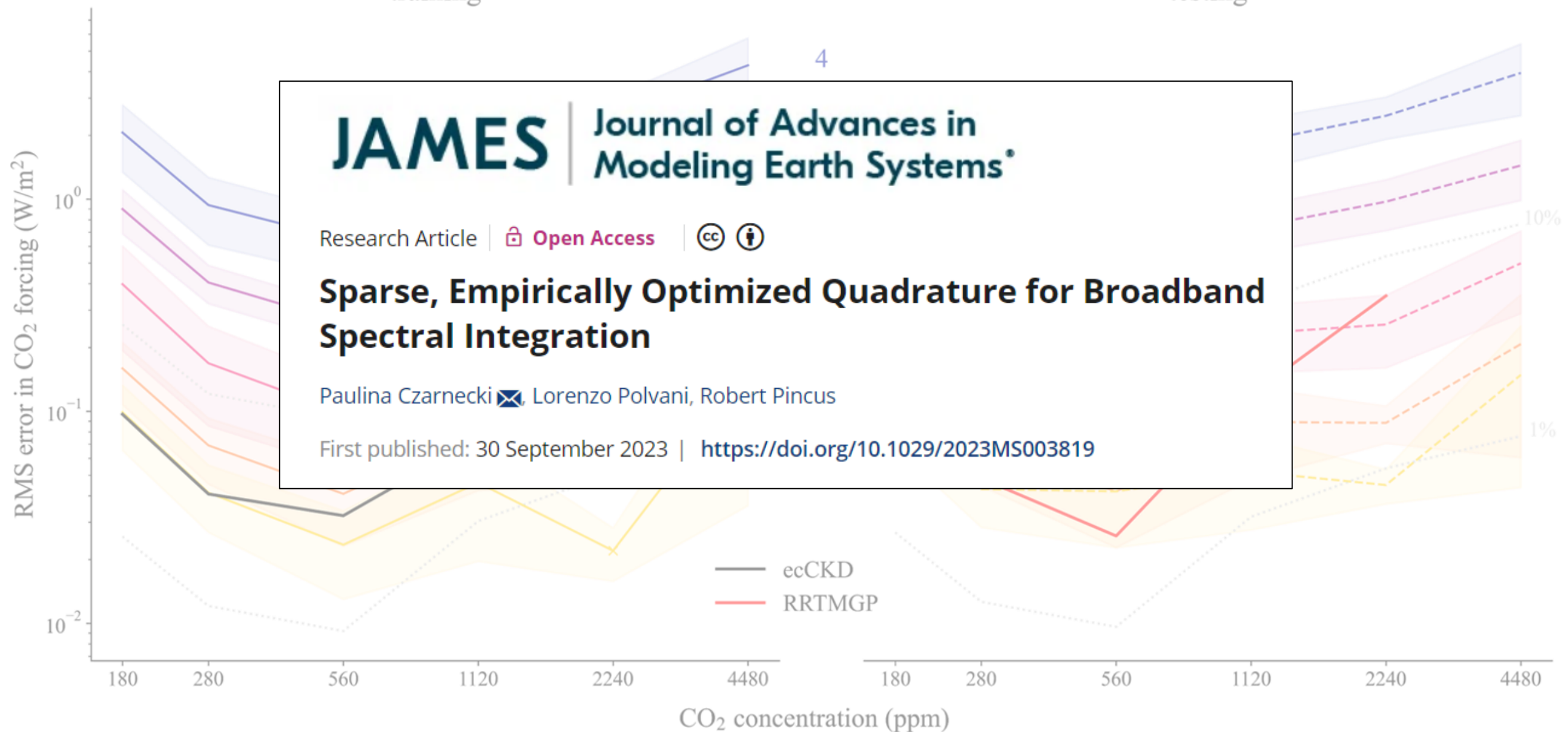
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testing





# Implementation in a Simple Model

With Stefan Buehler (UHH), Manfred Brath (UHH), Richard Larsson (UHH), and Lukas Klufft (MPI)

# Implementation in a Simple Model



Single-column RCE model  
developed by Lukas Kluft et al. at  
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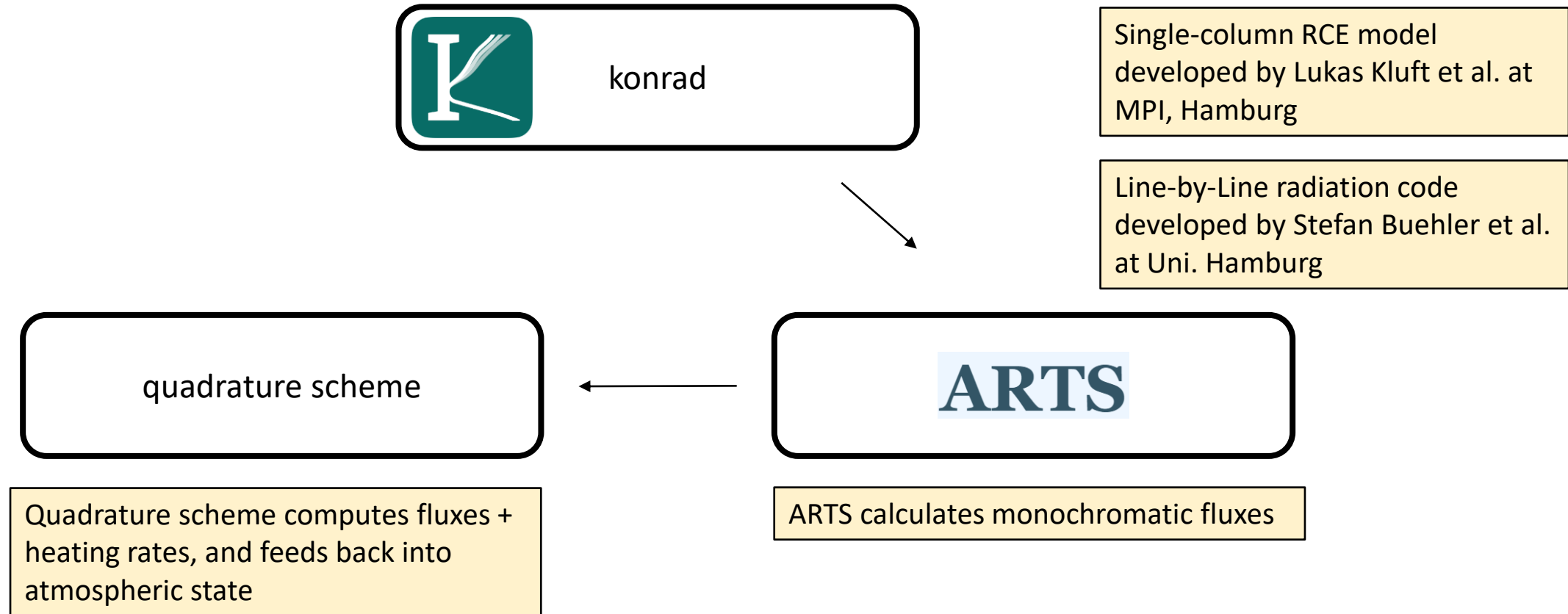
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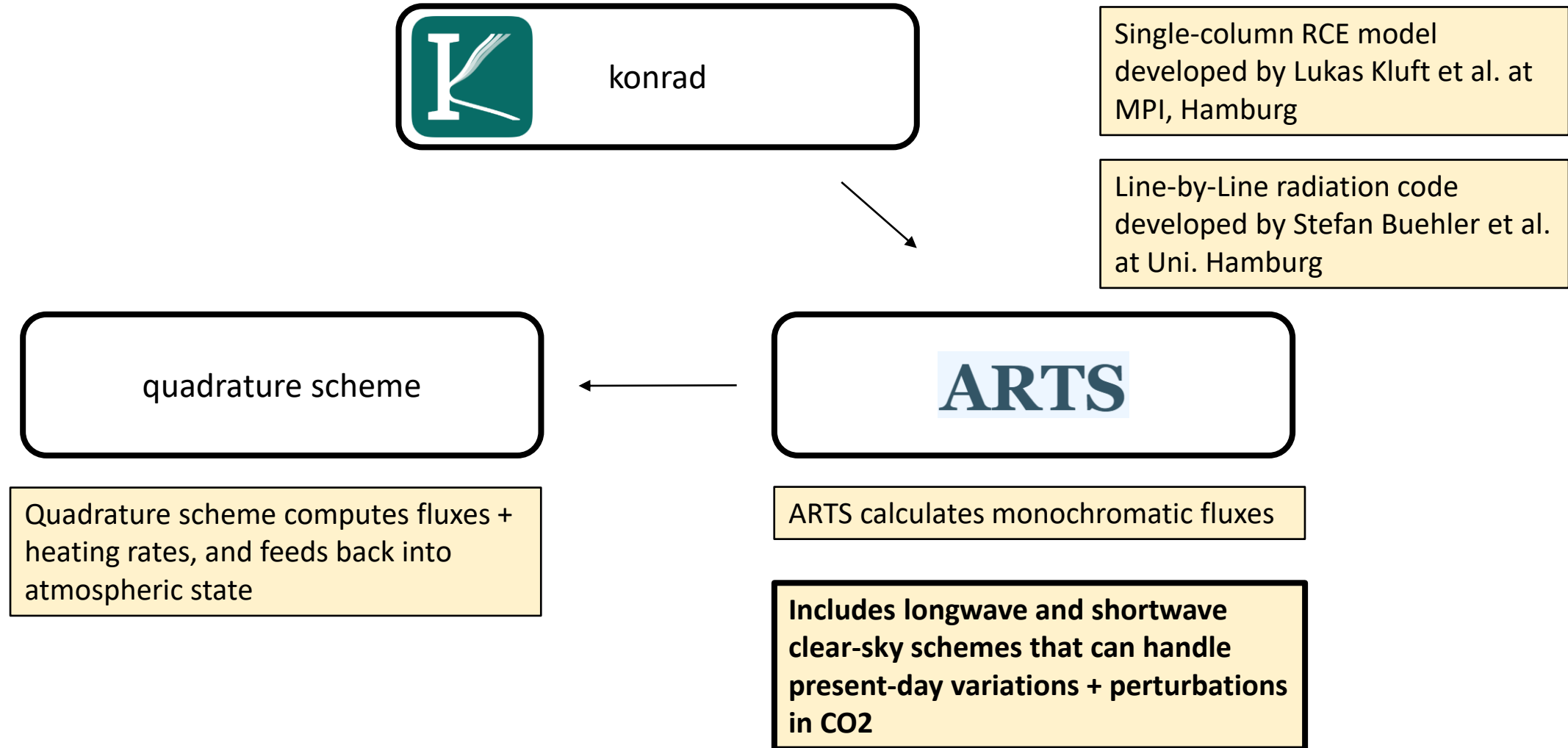


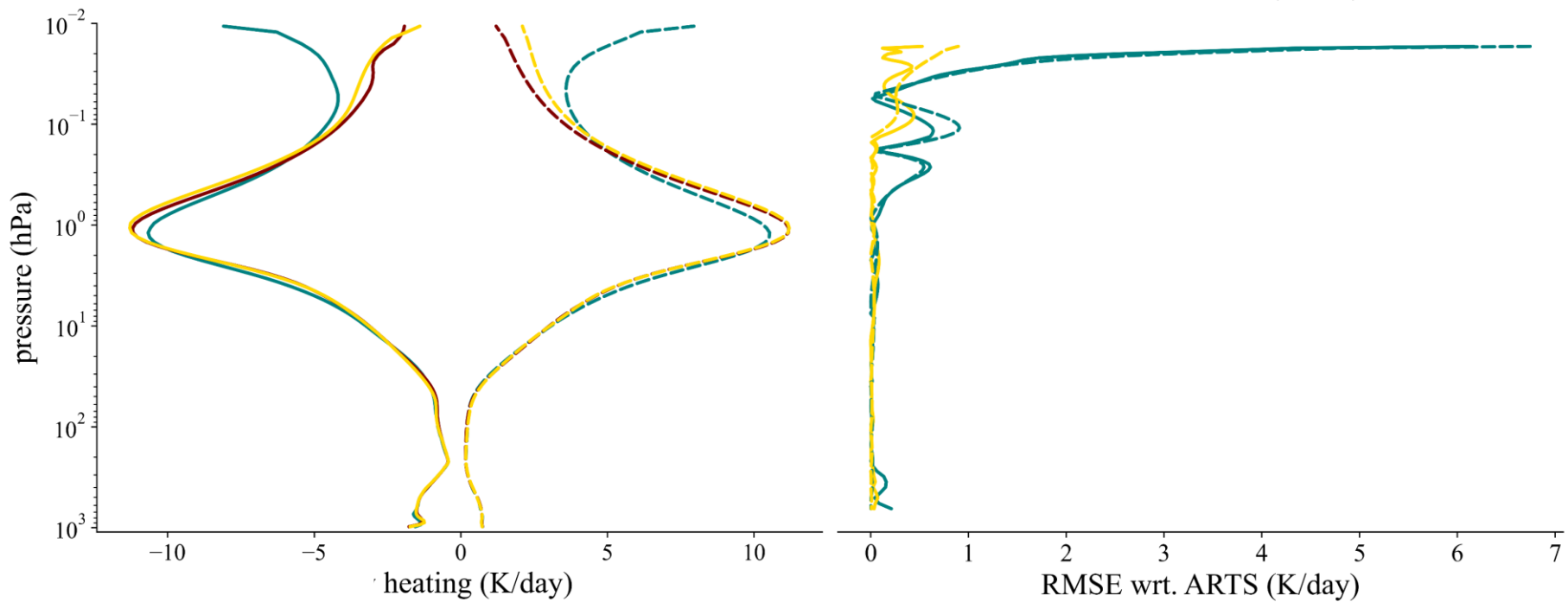
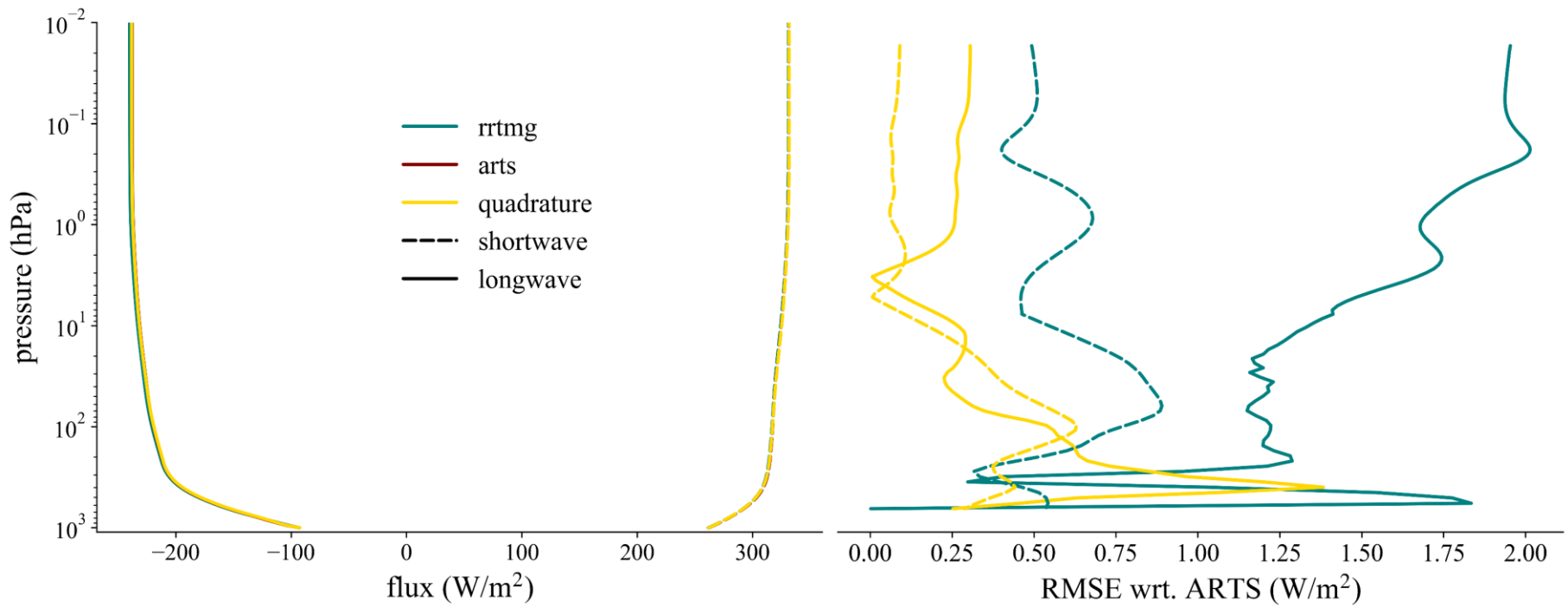
ARTS calculates monochromatic fluxes

# Implementation in a Simple Model



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# Conclusions

- The quadrature scheme is more flexible than leading models
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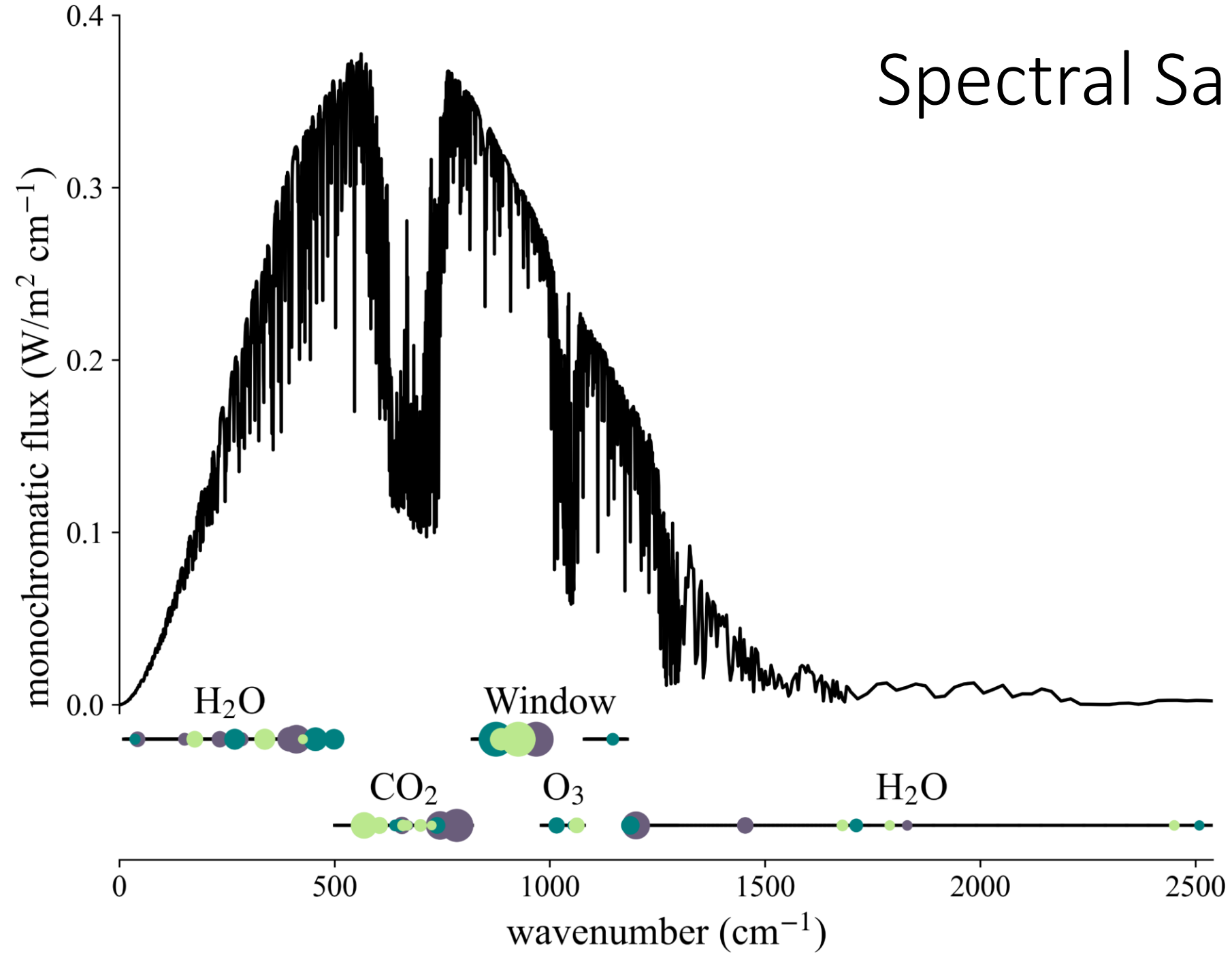
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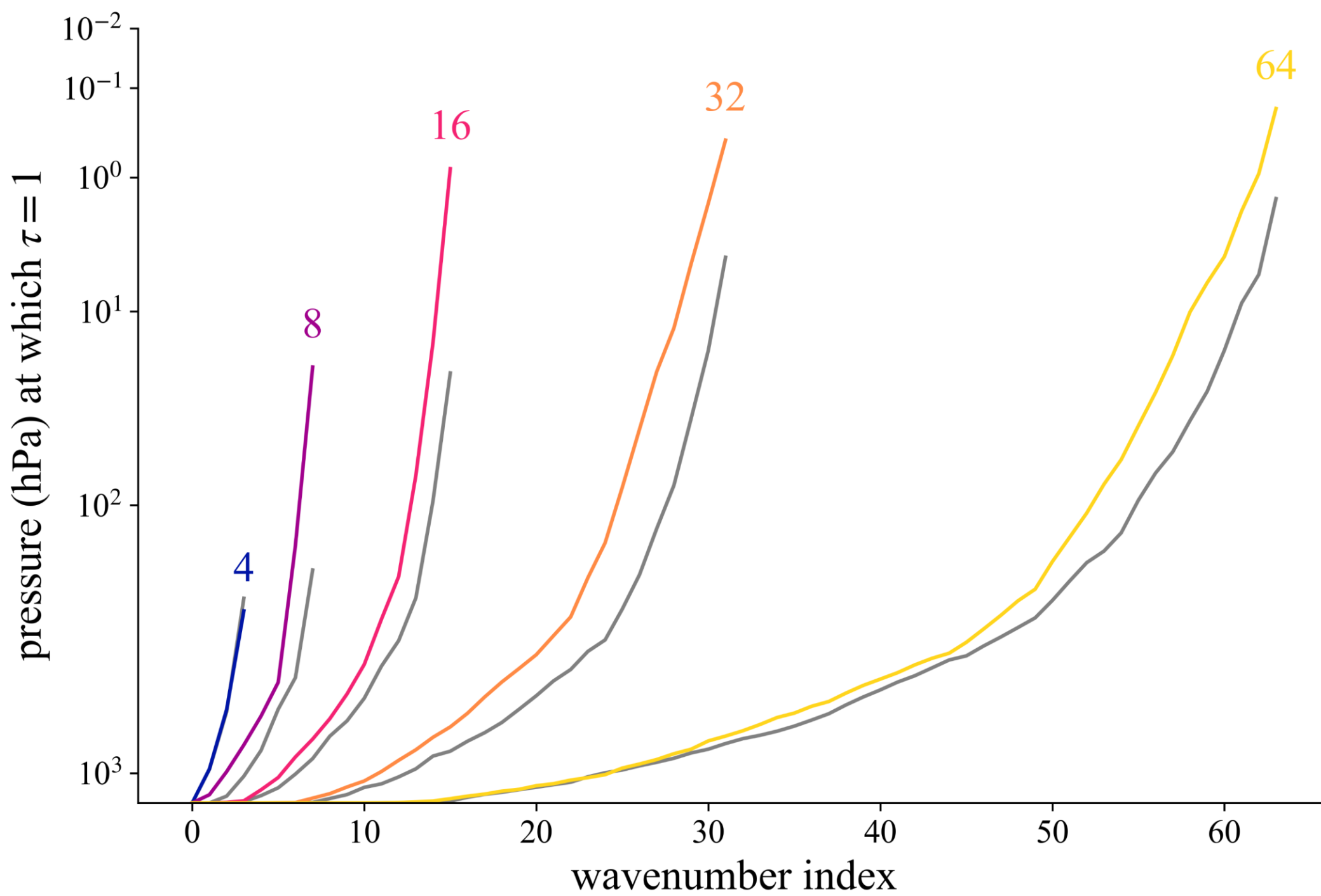
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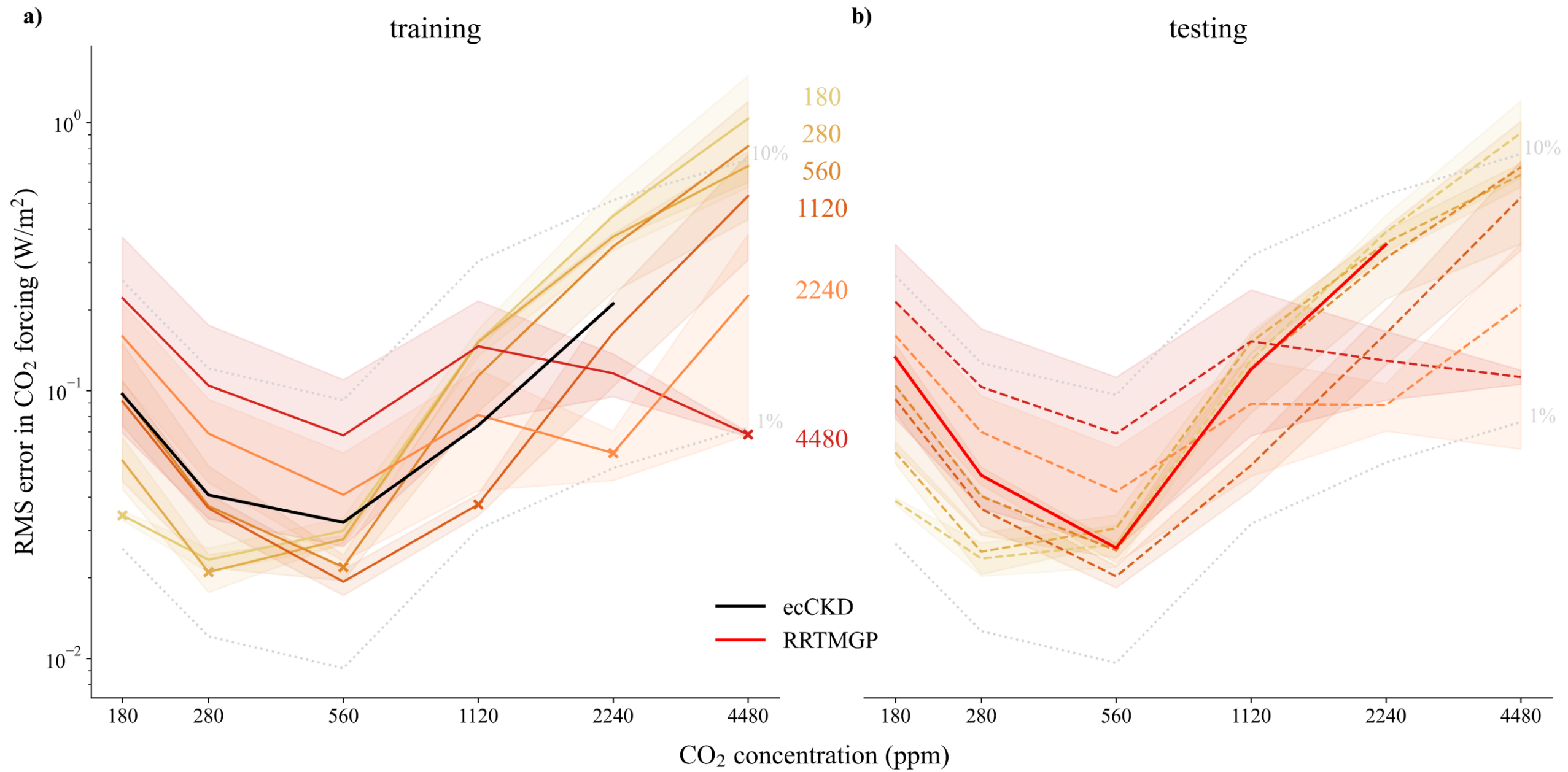
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  - Our computational cost/accuracy are competitive
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- Further challenges:
  - Clouds
  - Variation in a wider set of gases

Thank you!

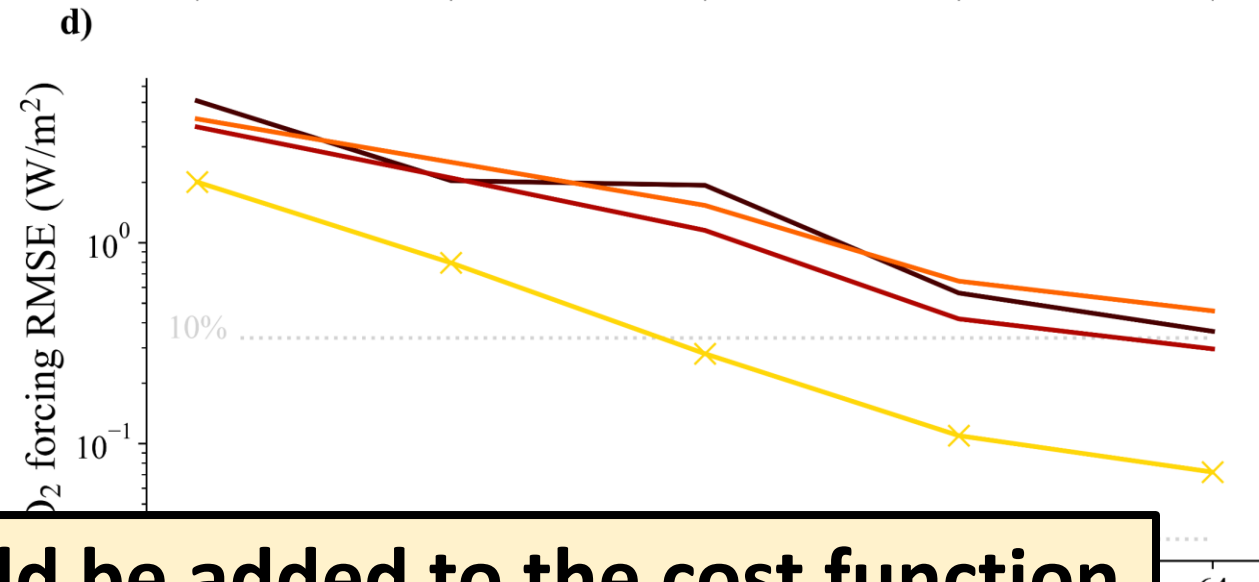
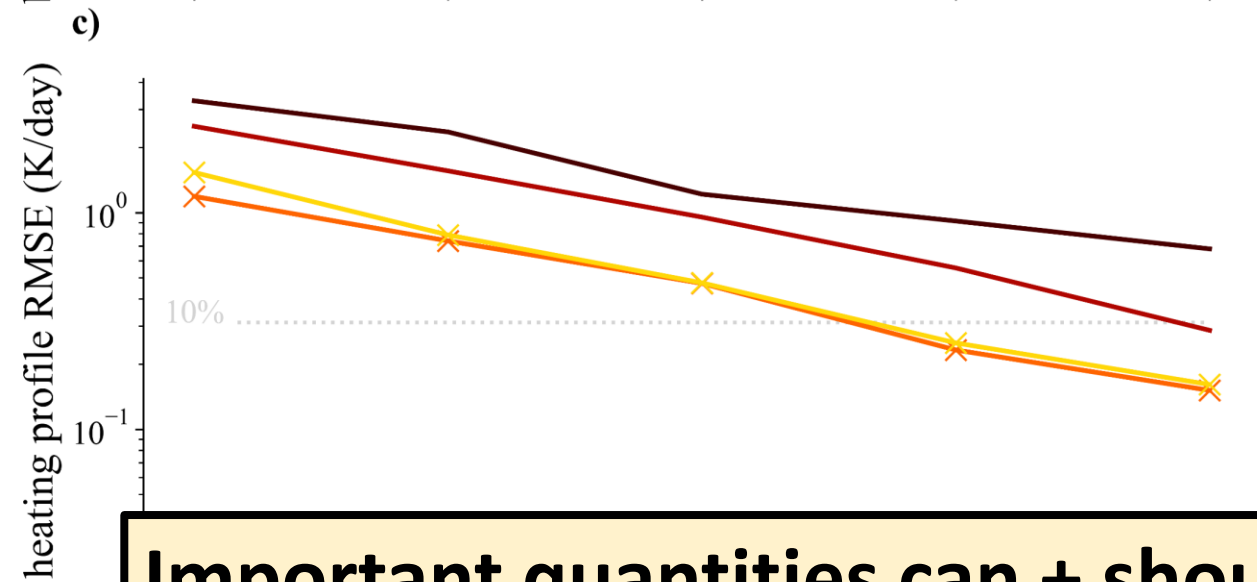
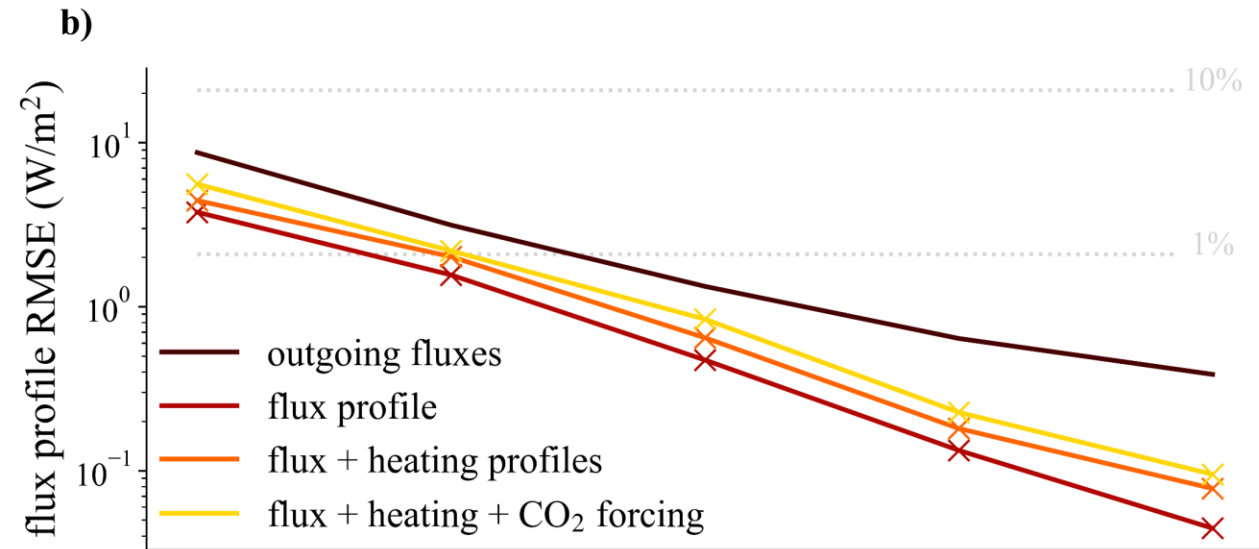
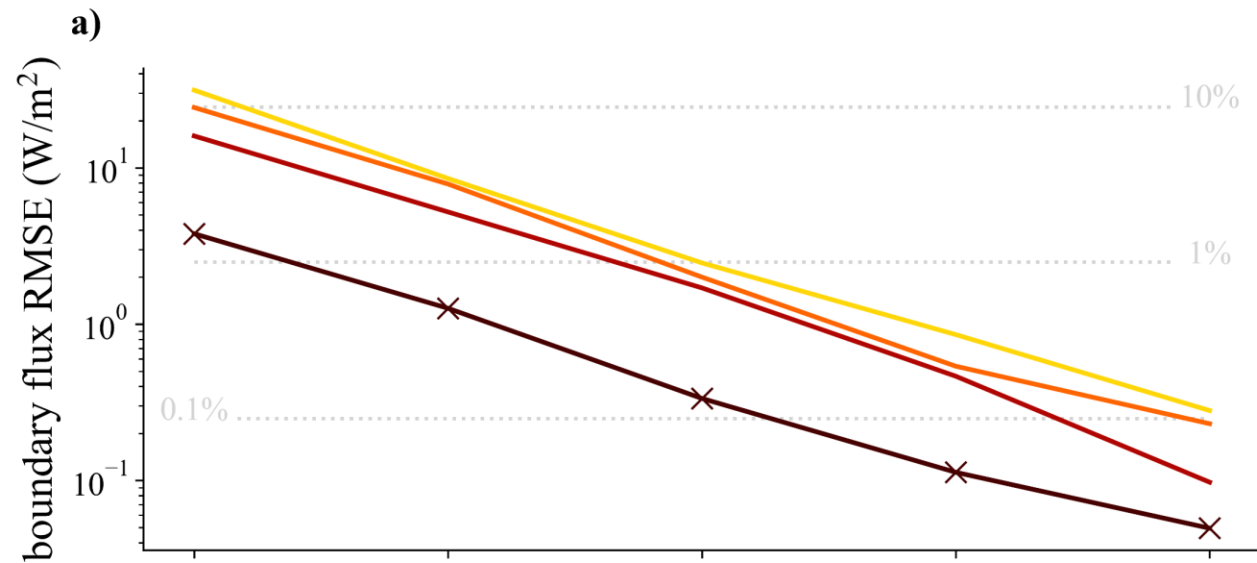
# Spectral Sampling







# Cost Function Tradeoffs



**Important quantities can + should be added to the cost function**