

EBAF Ed4.2 vs 4.1 & TOA SW Up

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(Remote Presentation)

$$E = \frac{A_0}{2} (1 + \bar{\tau}), \quad A = \frac{A_0}{2} (2 + \bar{\tau}), \quad B = \frac{A_0}{2} \bar{\tau}. \quad (11)$$

Schwarzschild (1906, Eq. 11)

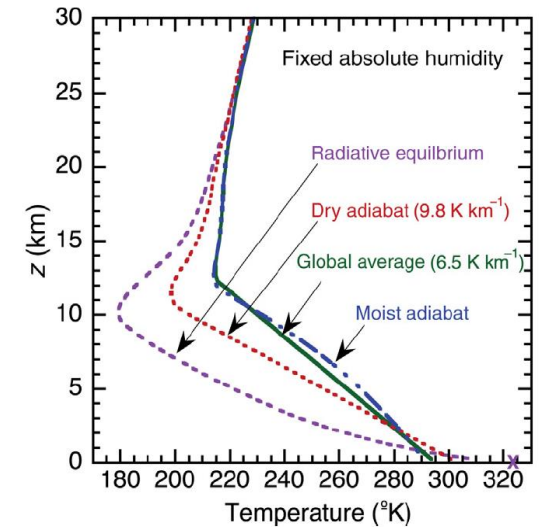
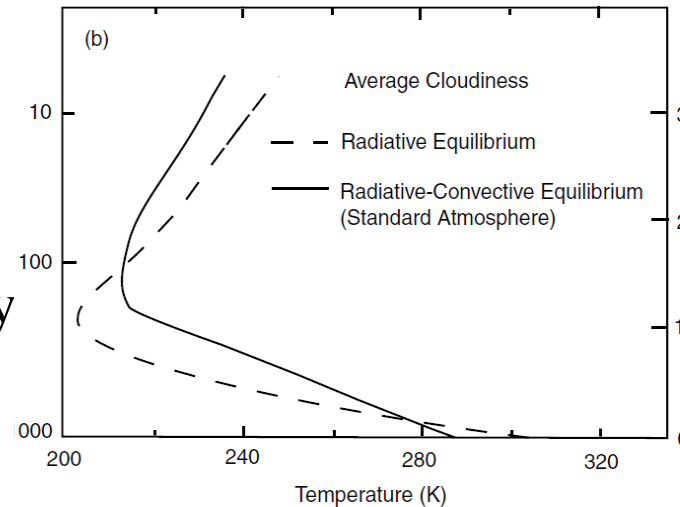
E emission of a layer

A upward beam at the given layer

B downward beam at that layer

A_0 emerging beam at the upper boundary

τ optical depth



Net radiation at the surface:

Eq. (1) $A - E = SH + LH = A_0/2$ Liou (2002, Fig. 8.9)

Hartmann (2016, Fig. 3.16)

May be derived from first principles (Milne 1930, Handbook of Astrophysics)

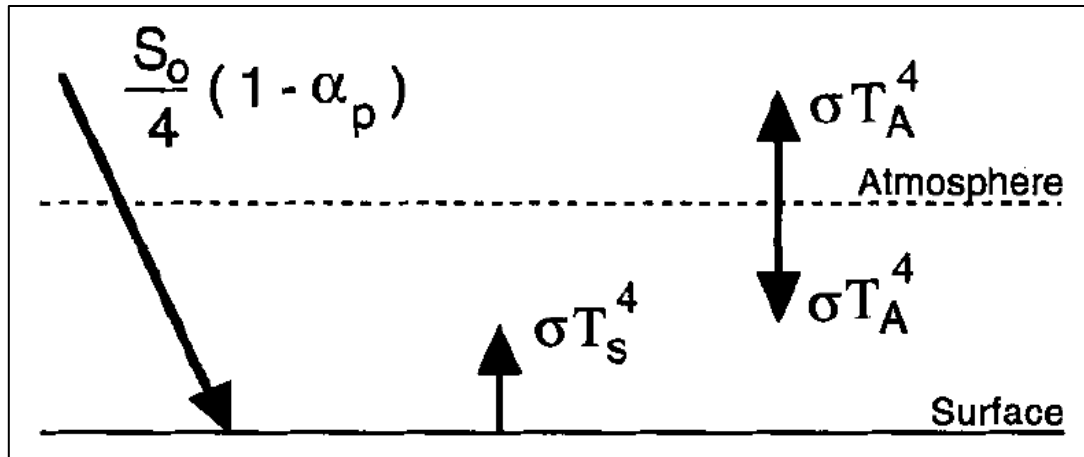
Represented in: Ostriker (1963, Eq. 15); Goody (1964, Eq. 2.115); Houghton (1977, Eq. 2.13); Chamberlain (1978, Eq. 1.2.29); Goody and Yung (1989, 2.146); Stephens (1991, Eq. 1 & 2; 1994, Eq. 5a & 5b); Hartmann (1994, Fig. 3.10-3.11); Liou (2002, Fig. 8.9); Pierrehumbert (2010, Eq. 4.44-4.45); Hartmann (2016, Fig. 3.16) ...

I think my study is the first that controls it on global mean observed data.

$$E = \frac{A_0}{2} (1 + \bar{\tau}), \quad A = \frac{A_0}{2} (2 + \bar{\tau}), \quad B = \frac{A_0}{2} \bar{\tau}. \quad (\text{II})$$

Eq. (2) $A = 2A_0$ at $\tau = 2$

2.5 Greenhouse Effect



Hartmann (1994, Fig. 2.3) $\sigma T_s^4 = 2\sigma T_A^4$

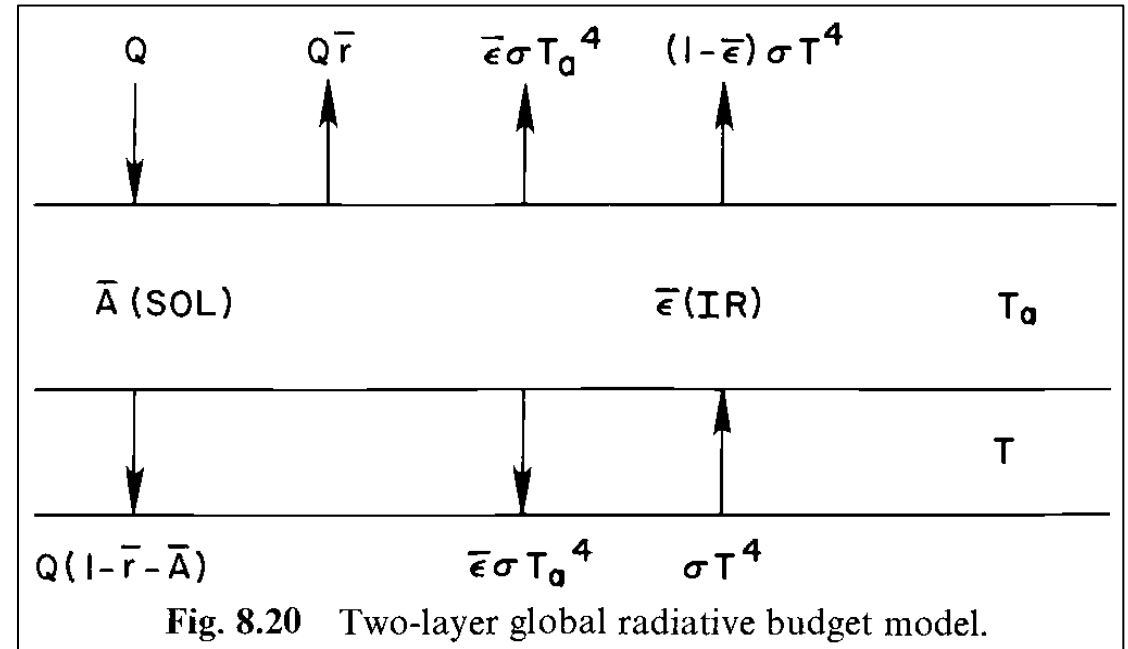


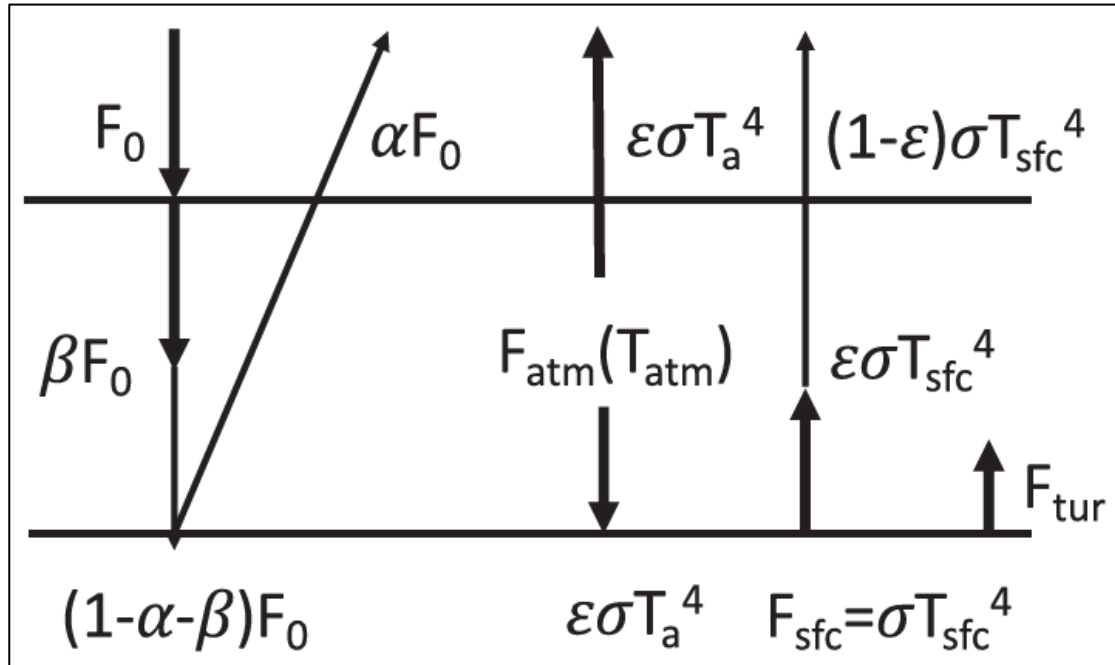
Fig. 8.20 Two-layer global radiative budget model.

Liou (1980, Fig. 8.20) $\epsilon = 1 \Rightarrow \sigma T^4 = 2\sigma T_a^4$

Total radiation at the surface if $\epsilon = 1$:

$$\text{Eq. (2)} \quad A = 2A_0$$

Eq. (2): Why $\varepsilon = 1$? Maximum entropy production?



Kato and Rose (2020, Fig. 1)

Entropy export to space by radiation (Eq.5), entropy produced within the atmosphere (Eq.7), and the total entropy produced by the Earth system (Eq.8), as a function of ε , is at maximum if $\varepsilon = 1$.

T_{sfc}). Therefore, entropy export to space by radiation is

$$J_{\text{TOA}}^{\text{net}} = J_{\text{ref}} - J_{\text{atm}} - (1 - \varepsilon)J_{\text{sfc}} + (1 - \alpha)J_{\text{sun}}. \quad (5)$$

Entropy produced by radiation exchange and heating at the surface is

$$\dot{\Sigma}_{\text{sfc}} = \frac{F_{\text{sfc}}^{\text{net}}}{T_{\text{sfc}}} = \frac{(1 - \alpha - \beta)F_0 + F_{\text{atm}} - F_{\text{sfc}} - F_{\text{tur}}}{T_{\text{sfc}}}, \quad (6)$$

and entropy produced within the atmosphere is

$$\dot{\Sigma}_{\text{atm}} = \frac{F_{\text{atm}}^{\text{net}}}{T_{\text{atm}}} = \frac{\beta F_0 + \varepsilon F_{\text{sfc}} + F_{\text{tur}} - 2F_{\text{atm}}}{T_{\text{atm}}}. \quad (7)$$

The sum of Eqs. (5)–(7) is equal to the total entropy produced by the Earth system $\dot{\Sigma}_{\text{tot}}$,

$$\dot{\Sigma}_{\text{tot}} = J_{\text{TOA}}^{\text{net}} + \dot{\Sigma}_{\text{sfc}} + \dot{\Sigma}_{\text{atm}}. \quad (8)$$

$$\text{Eq. (1) SFC SW+LW Net (clear)} = A - E = A_0/2$$

$$\text{Eq. (2) SFC SW+LW Total (clear)} = A = 2A_0$$

Creating the all-sky versions (including LWCRE):

$$\text{Eq. (3) SFC SW+LW Net (all)} = A - E = (A_0 - L)/2$$

$$\text{Eq. (4) SFC SW+LW Total (all)} = A = 2A_0 + L$$

$$\text{Eq. (1) SFC (SW down - SW up + LW down - LW up) (clear)} = \text{TOA LW (clear) / 2}$$

$$\text{Eq. (2) SFC (SW down - SW up + LW down) (clear)} = \text{TOA LW (clear) } \times 2$$

$$\text{Eq. (3) SFC (SW down - SW up + LW down - LW up) (all)} = \text{TOA [LW (all) - LWCRE] / 2}$$

$$\text{Eq. (4) SFC (SW down - SW up + LW down) (all)} = \text{TOA LW (all) } \times 2 + \text{LWCRE}$$

Four Equations, EBAF Edition 2.8

(March 2000 – Feb 2016) (Rose et al. 2017, 27th CERES STM)

Eq. (1) SFC SW down – SW up + LW down – LW up (clear) = TOA LW (clear)/2

Eq. (2) SFC SW down – SW up + LW down (clear) = 2 × TOA LW (clear)

Eq. (3) SFC SW down – SW up + LW down – LW up (all) = [TOA LW (all) – LWCRE]/2

Eq. (4) SFC SW down – SW up + LW down (all) = 2 × TOA LW (all) + LWCRE

Four Equations, EBAF Edition 2.8

(March 2000 – Feb 2016) (Rose et al. 2017, 27th CERES STM)

Eq. (1)	SFC	SW down	– SW up	+ LW down	– LW up (clear)	= TOA LW (clear)/2	Diff
Ed2.8		244.06	– 29.74	+ 316.27	– 398.40	= 265.59 /2	–0.60

Eq. (2)	SFC	SW down	– SW up	+ LW down	(clear)	= 2 × TOA LW (clear)	
Ed2.8		244.06	– 29.74	+ 316.27		= 2 × 265.59	–0.59

Eq. (3)	SFC	SW down	– SW up	+ LW down	– LW up	(all) = [TOA LW (all) – LWCRE]/2	
Ed2.8		186.47	– 24.13	+ 345.15	– 398.27	= (239.60 – 25.99)/2	+2.41

Eq. (4)	SFC	SW down	– SW up	+ LW down	(all)	= 2 × TOA LW (all) + LWCRE	
Ed2.8		186.47	– 24.13	+ 345.15		= 2 × 239.60 + 25.99	+2.30

Four Equations, EBAF Edition 4.1

CERES EBAF Ed4.1 & Ed4.2, 22 years (April 2000 – March 2022) (Wm^{-2})

Eq. (1) Ed4.1	SFC SW down – SW up + LW down – LW up (clear)	= TOA LW (clear)/2	Diff	}	-2.5752
	240.8680 – 29.0724 + 317.4049 – 398.5211	= 266.0122 /2	-2.3267		
Eq. (2) Ed4.1	SFC SW down – SW up + LW down	(clear) = 2 × TOA LW (clear)		}	
	240.8680 – 29.0724 + 317.4049	= 2 × 266.0122	-2.8238		
Eq. (3) Ed4.1	SFC SW down – SW up + LW down – LW up	(all) = [TOA LW (all) – LWCRE]/2		}	+2.5766
	186.8544 – 23.1629 + 345.0108 – 398.7454	= (240.2450 – 25.7672)/2	+2.7083		
Eq. (4) Ed4.1	SFC SW down – SW up + LW down	(all) = 2 × TOA LW (all) + LWCRE		}	
	186.8544 – 23.1629 + 345.0108	= 2 × 240.2450 + 25.7672	+2.4450		
Ed4.1			Mean		+0.0007

The four equations are intimately connected

Decrease TOA LW(clear) by 1 Wm⁻²

Eq. (1)	SFC	SW down – SW up + LW down – LW up (clear)	= TOA LW (clear)/2	Diff	
Ed4.1		240.8680 – 29.0724 + 317.4049 – 398.5211	= 266.0122 /2	-2.3267	
Ed4.1		240.8680 – 29.0724 + 317.4049 – 398.5211	= 265.0122 /2	-1.8267	} -2.5752
Eq. (2)	SFC	SW down – SW up + LW down	(clear) = 2 × TOA LW (clear)		
Ed4.1		240.8680 – 29.0724 + 317.4049	= 2 × 266.0122	-2.8238	} -1.3252
Ed4.1		240.8680 – 29.0724 + 317.4049	= 2 × 265.0122	-0.8238	
Eq. (3)	SFC	SW down – SW up + LW down – LW up	(all) = [TOA LW (all) – LWCRE]/2		
Ed4.1		186.8544 – 23.1629 + 345.0108 – 398.7454	= (240.2450 – 25.7672)/2	+2.7083	
Ed4.1		186.8544 – 23.1629 + 345.0108 – 398.7454	= (240.2450 – 24.7672)/2	+2.2083	} +2.5766
Eq. (4)	SFC	SW down – SW up + LW down	(all) = 2 × TOA LW (all) + LWCRE		
Ed4.1		186.8544 – 23.1629 + 345.0108	= 2 × 240.2450 + 25.7672	+2.4450	} +2.8266
Ed4.1		186.8544 – 23.1629 + 345.0108	= 2 × 240.2450 + 24.7672	+3.4450	
Ed4.1			Mean	+0.0007	
Ed4.1			Mean	+0.7507	

Four Equations, EBAF Edition 4.1 & 4.2

CERES EBAF Ed4.1 & Ed4.2, 22 years (April 2000 – March 2022) (Wm^{-2})

Eq. (1)	SFC SW down – SW up + LW down – LW up (clear) = TOA LW (clear)/2	Diff	
Ed4.1	240.8680 – 29.0724 + 317.4049 – 398.5211 = 266.0122 /2	-2.3267	
Ed4.2	241.1519 – 29.7397 + 317.8570 – 398.6099 = 266.1348 /2	-2.4081	} -2.7043
Eq. (2)	SFC SW down – SW up + LW down (clear) = 2 × TOA LW (clear)		
Ed4.1	240.8680 – 29.0724 + 317.4049 = 2 × 266.0122	-2.8238	
Ed4.2	241.1519 – 29.7397 + 317.8570 = 2 × 266.1348	-3.0005	
Eq. (3)	SFC SW down – SW up + LW down – LW up (all) = [TOA LW (all) – LWCRE]/2		
Ed4.1	186.8544 – 23.1629 + 345.0108 – 398.7454 = (240.2450 – 25.7672)/2	+2.7083	
Ed4.2	187.0918 – 23.4436 + 346.1147 – 398.4220 = (240.3317 – 25.8032)/2	+4.0766	} +3.6865
Eq. (4)	SFC SW down – SW up + LW down (all) = 2 × TOA LW (all) + LWCRE		
Ed4.1	186.8544 – 23.1629 + 345.0108 = 2 × 240.2450 + 25.7672	+2.4450	
Ed4.2	187.0918 – 23.4436 + 346.1147 = 2 × 240.3317 + 25.8032	+3.2963	
Ed4.1		Mean	+0.0007
Ed4.2		Mean	+0.4911

Bias, or Ed4.2 captured something physical that Ed4.1 missed?

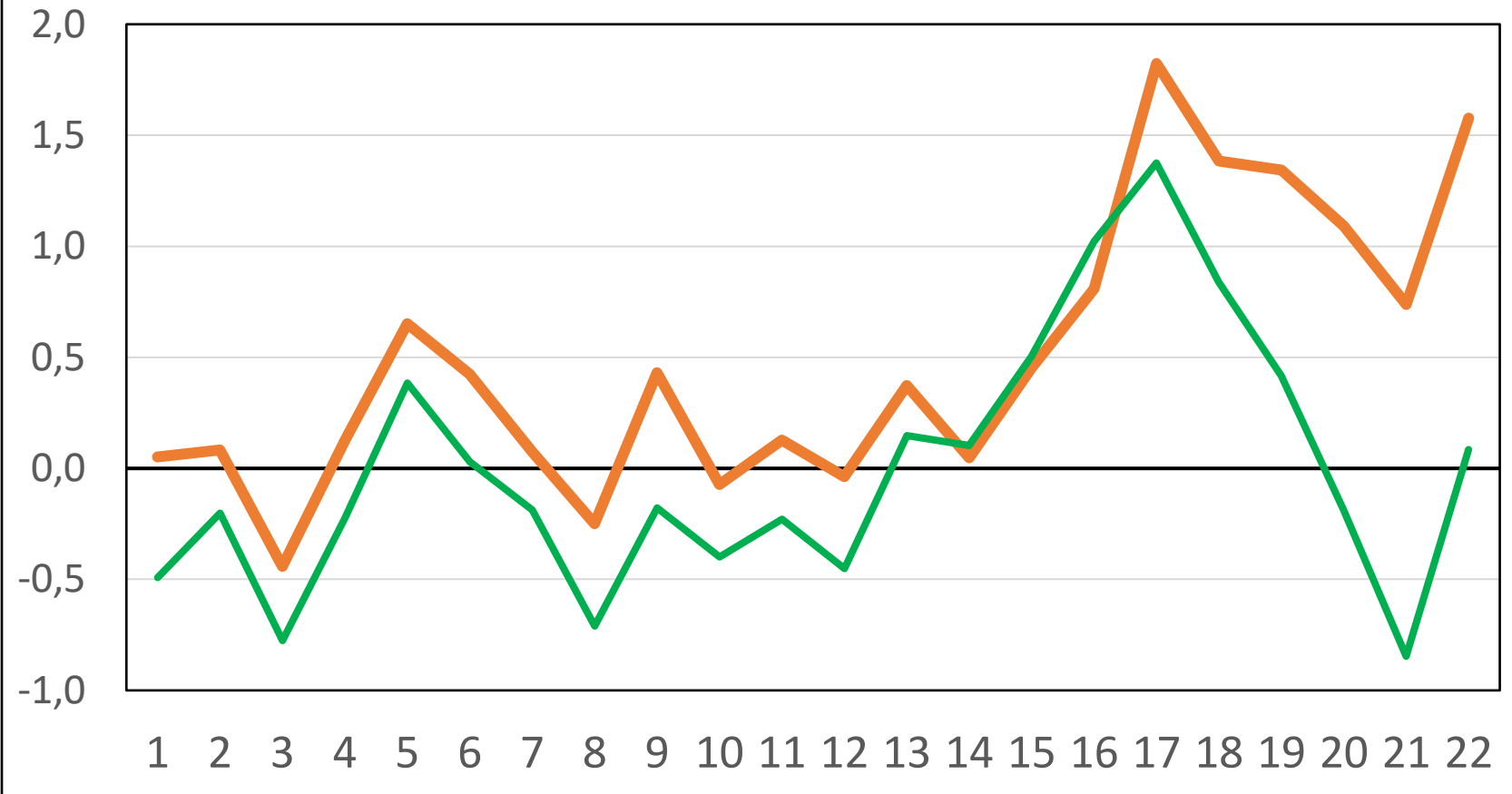
EBAF Edition 4.2

22 years (Apr 2000 – Mar 2022)

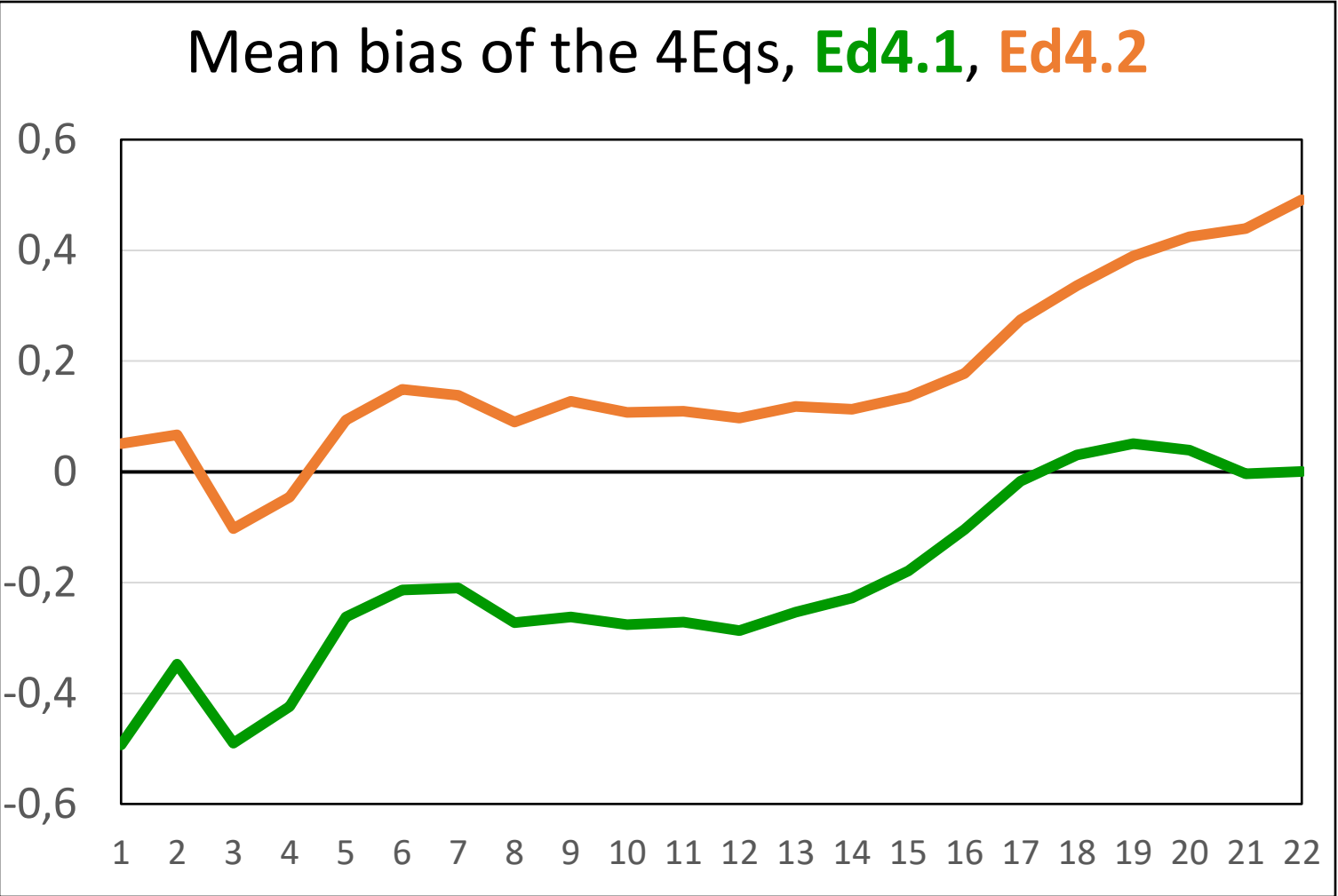
22 years (Jan 2001 – Dec 2022)

Eq. (1)	SFC SW down – SW up + LW down – LW up (clear) = TOA LW (clear)/2	Diff	
Apr-March	241.1519 – 29.7397 + 317.8570 – 398.6099 = 266.1348 /2	–2.4081	}
Jan-Dec	241.1085 – 29.7012 + 317.9809 – 398.7213 = 266.1207 /2	–2.3935	
Eq. (2)	SFC SW down – SW up + LW down (clear) = 2 × TOA LW (clear)		}
Apr-March	241.1519 – 29.7397 + 317.8570 = 2 × 266.1348	–3.0005	
Jan-Dec	241.1085 – 29.7012 + 317.9809 = 2 × 266.1207	–2.8533	–2.6234
Eq. (3)	SFC SW down – SW up + LW down – LW up (all) = [TOA LW (all) – LWCRE]/2		}
Apr-March	187.0918 – 23.4436 + 346.1147 – 398.4220 = (240.3317 – 25.8032)/2	+4.0766	
Jan-Dec	187.0941 – 23.4179 + 346.2001 – 398.5297 = (240.3606 – 25.7601) /2	+4.0463	+3.6865
Eq. (4)	SFC SW down – SW up + LW down (all) = 2 × TOA LW (all) + LWCRE		}
Apr-March	187.0918 – 23.4436 + 346.1147 = 2 × 240.3317 + 25.8032	+3.2963	
Jan-Dec	187.0941 – 23.4179 + 346.2001 = 2 × 240.3606 + 25.7601	+3.3949	+3.7206
Apr-March		Mean	+0.4911
Jan-Dec		Mean	+0.5486

Annual mean bias of the 4Eqs, **Ed4.1**, **Ed4.2**



Years



Number of years in the average

Libera Science Goals & Objectives

Overarching goals:

1) Provide seamless continuity of the ERB measurement with characteristics identical to CERES

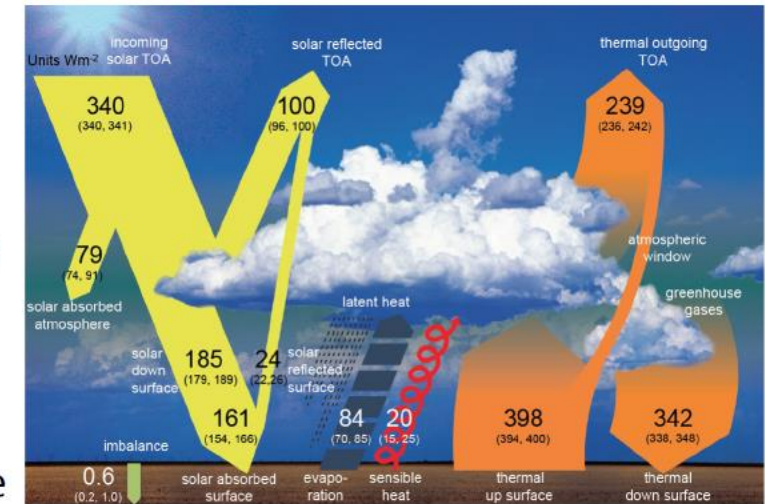
- Prevents gap in ERB data record critical for studies of global climate change
- Tied to **Science objective 1**: Use extended record to identify and quantify processes responsible for the instantaneous to decadal variability of ERB

2) Develop a self-contained, innovative, affordable observing system

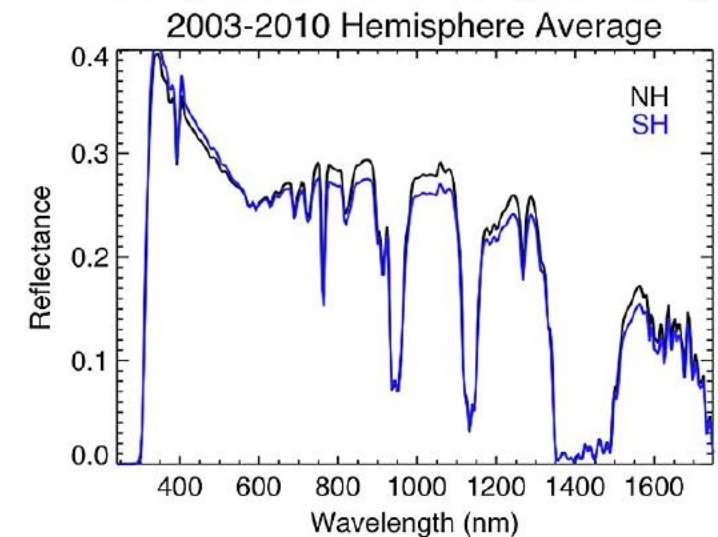
- Novel, miniaturized detectors greatly improve accuracy & stability and pave way toward smaller & cost-effective follow-on mission.
- **Science objective 2** *Libera* tests a miniature wide field-of-view camera to provide scene & angular context crucial for radiative flux retrieval

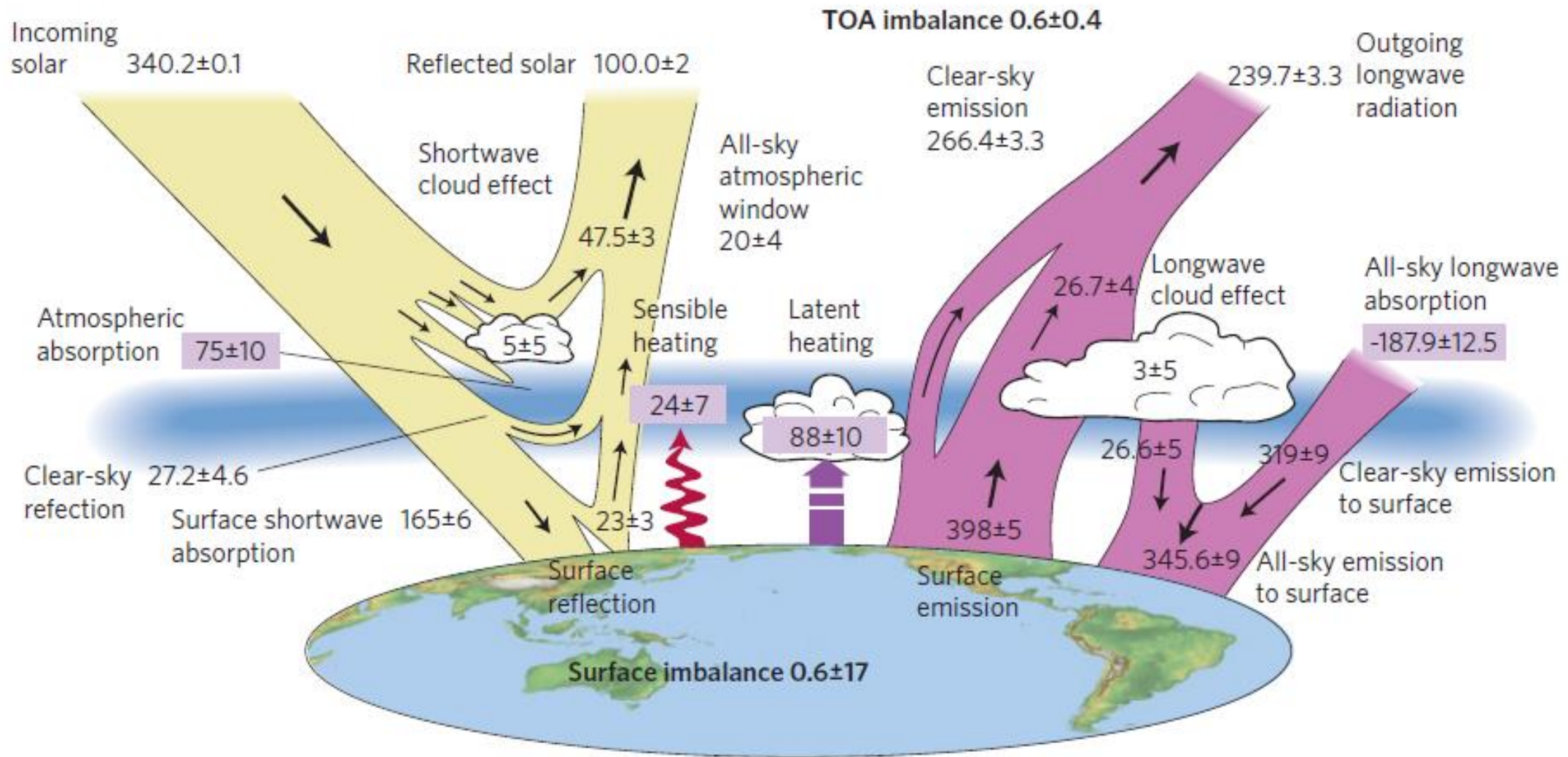
3) Provide new and enhanced capabilities that support extending ERB science goals

- Employ Split-Shortwave channel to derive SW VIS and NIR fluxes and quantify SW energy disposition
- Tied to **Science objective 3**: Revolutionize understanding of spatio-temporal variations in SW, VIS & NIR irradiance



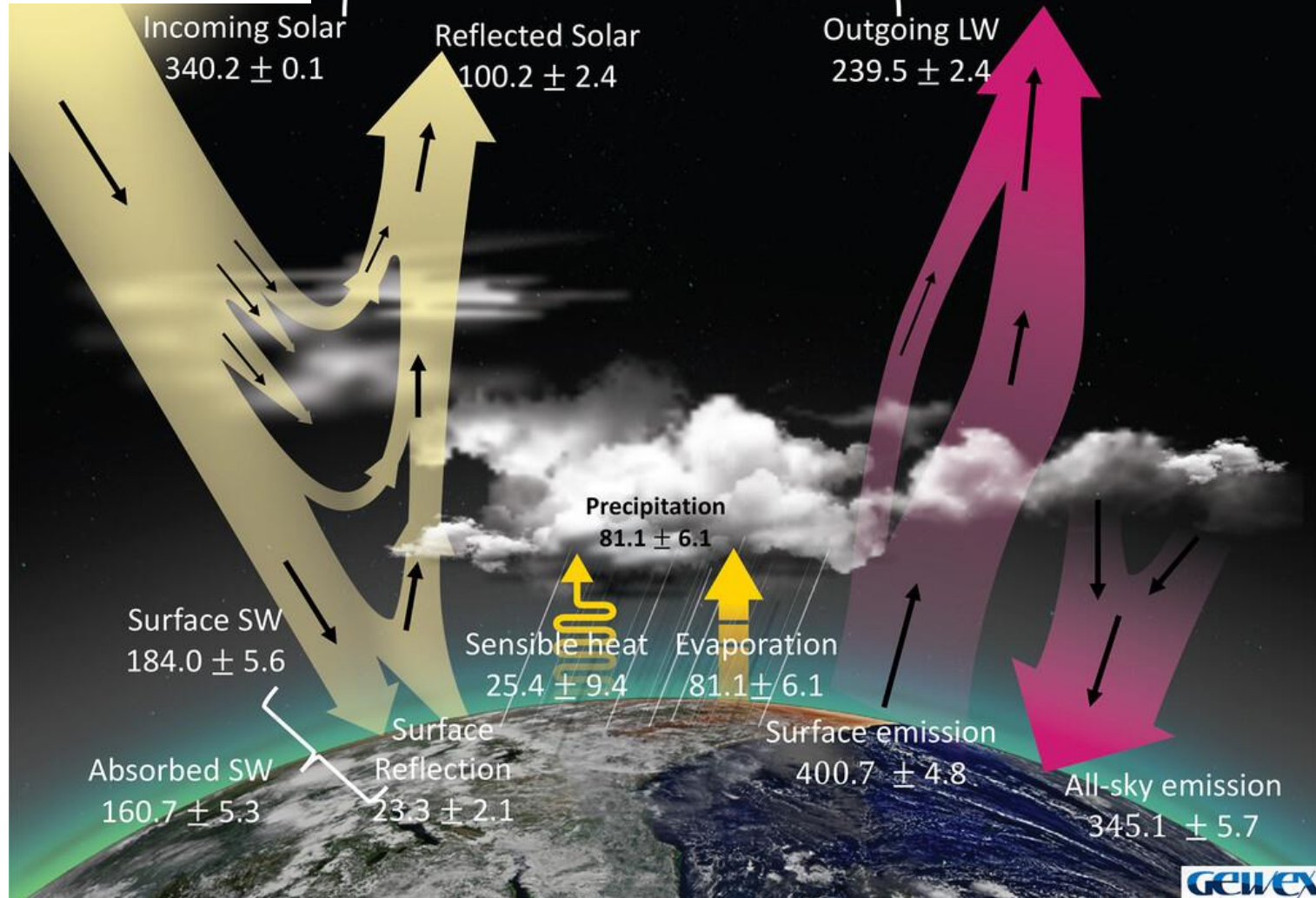
Hemispheric Albedo Symmetry?





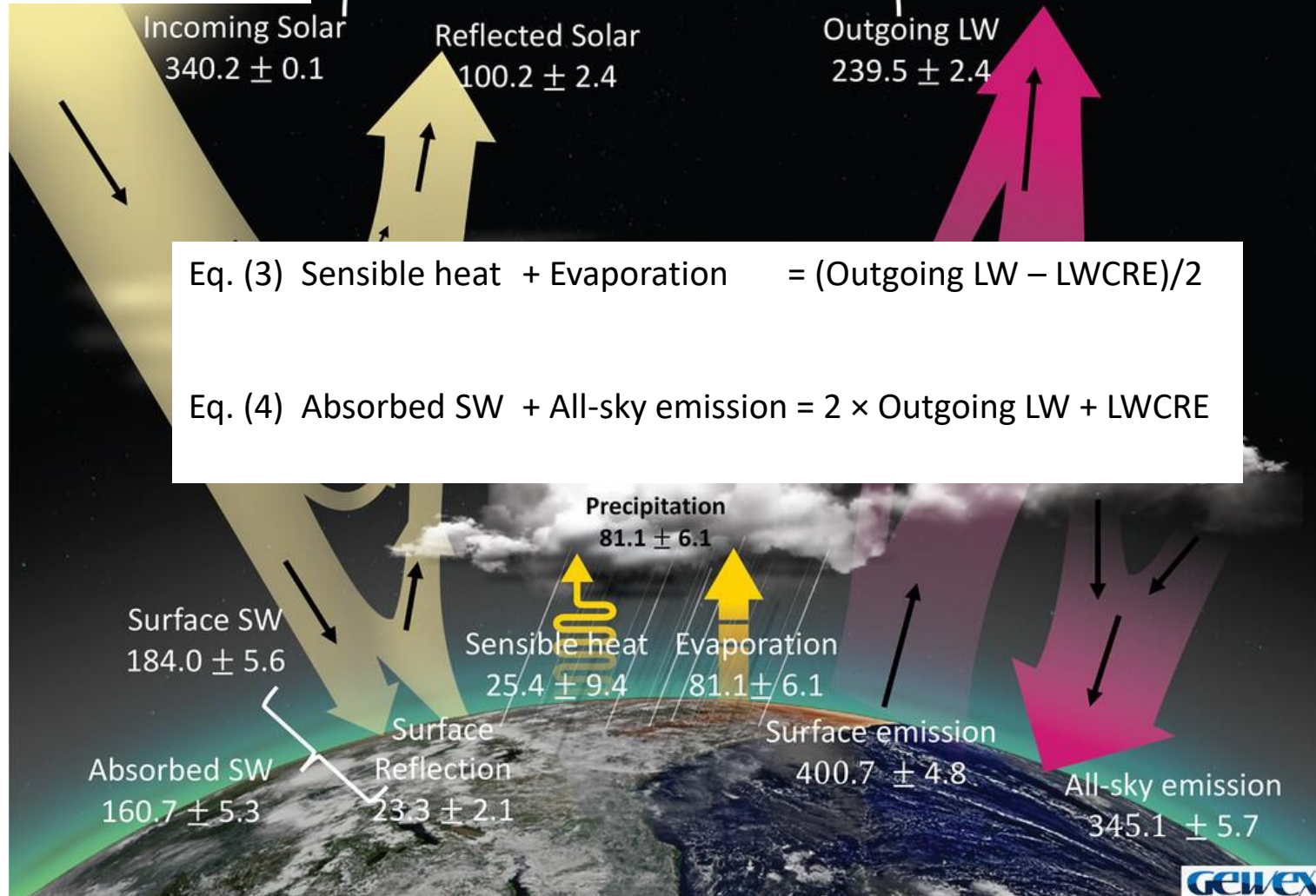
Stephens et al.
(2023) BAMS

Earth Energy Imbalance (EEI) = 0.54 ± 0.3



Stephens et al.
(2023) BAMS

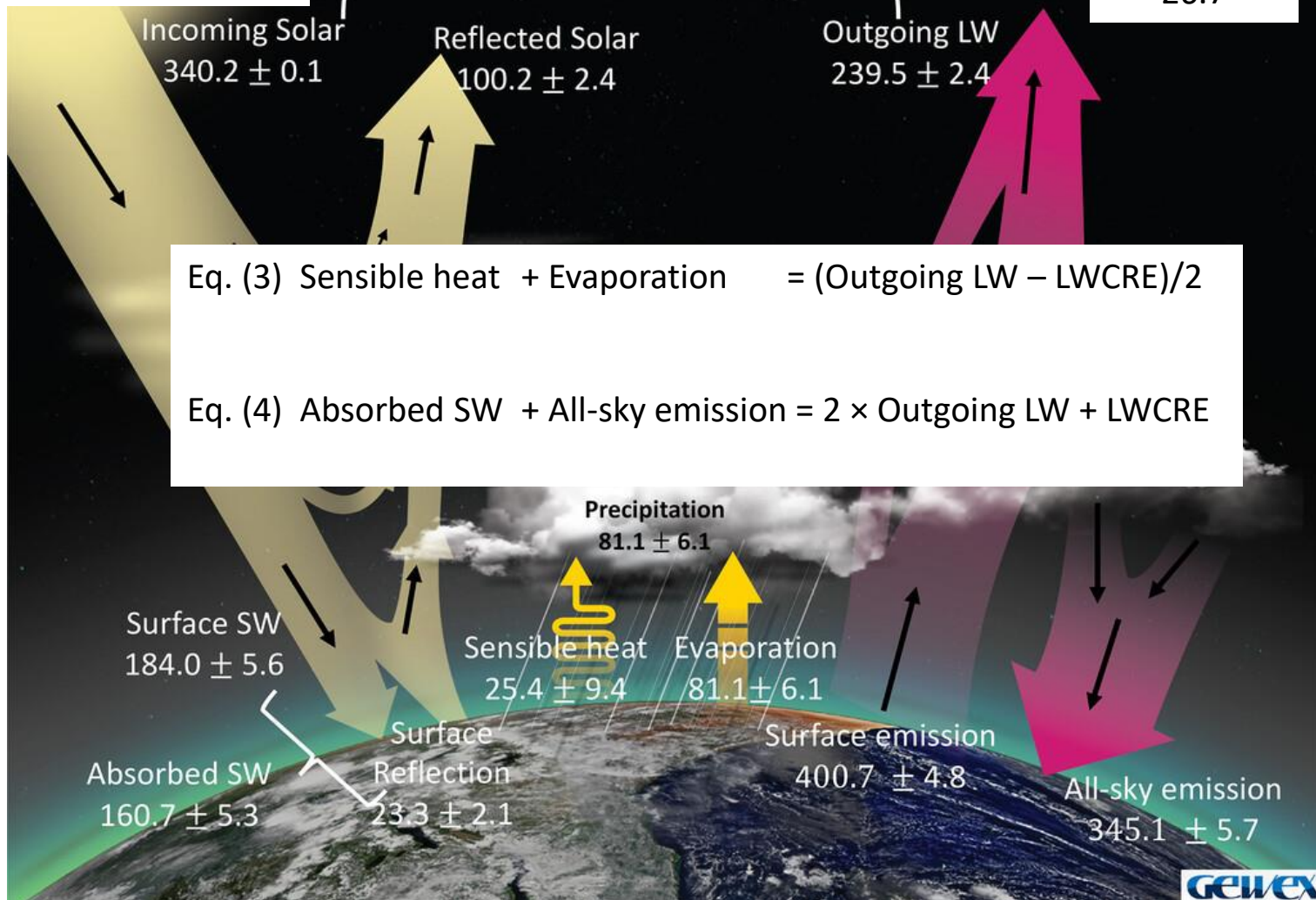
Earth Energy Imbalance (EEI) = 0.54 ± 0.3



Stephens et al.
(2023) BAMS

Earth Energy Imbalance (EEI) = 0.54 ± 0.3

LWCRE
26.7



Eq. (3) Sensible heat + Evaporation = $(\text{Outgoing LW} - \text{LWCRE})/2$

Eq. (4) Absorbed SW + All-sky emission = $2 \times \text{Outgoing LW} + \text{LWCRE}$

26.7 ± 4 Longwave cloud effect

Stephens et al. 2012

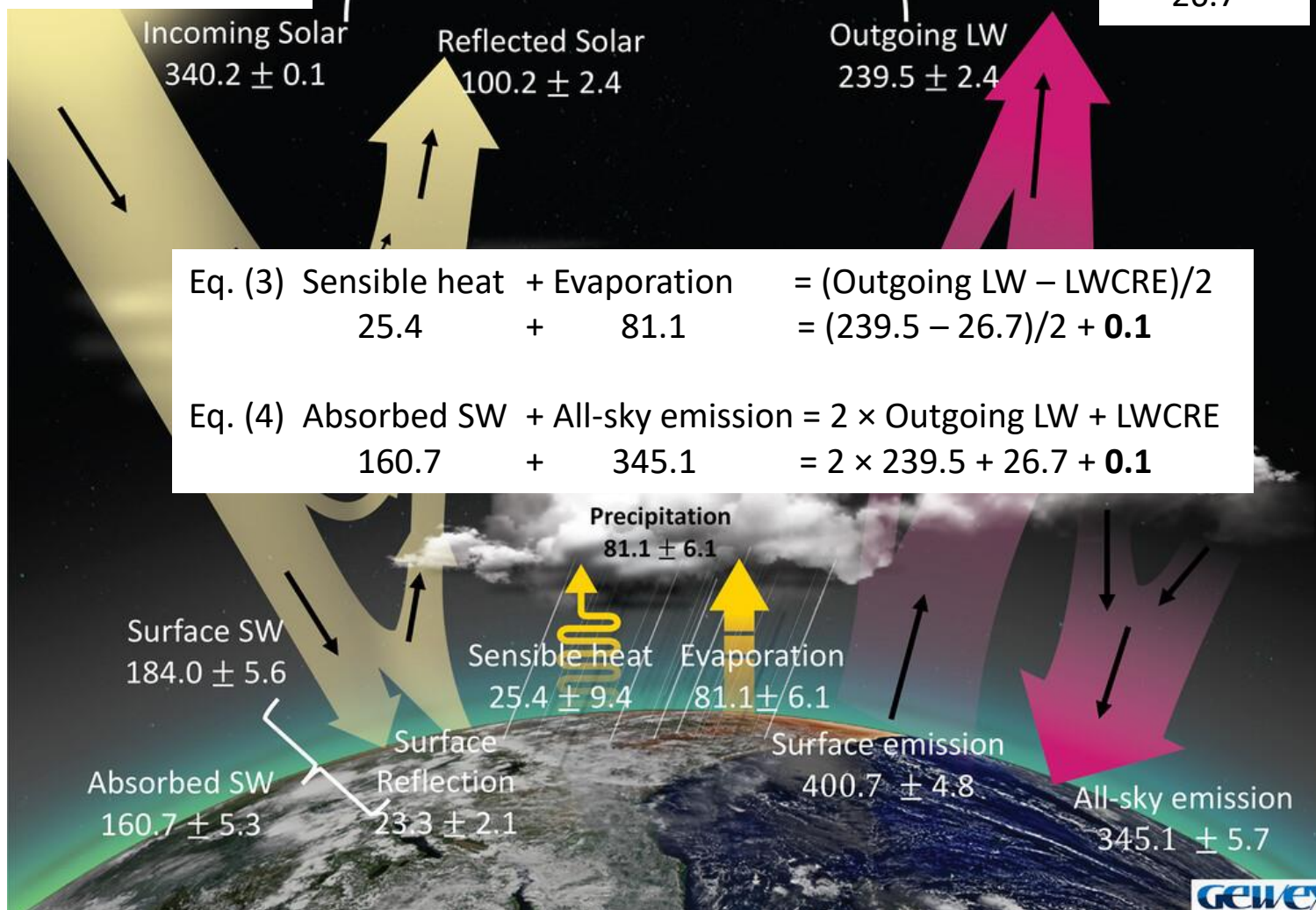
Stephens et al.
(2023) BAMS

Earth Energy Imbalance (EEI) = 0.54 ± 0.3

LWCRE
26.7

26.7 ± 4 Longwave
cloud effect

Stephens et al. 2012



Eq. (3) Sensible heat + Evaporation = (Outgoing LW - LWCRE)/2
 $25.4 + 81.1 = (239.5 - 26.7)/2 + 0.1$

Eq. (4) Absorbed SW + All-sky emission = 2 × Outgoing LW + LWCRE
 $160.7 + 345.1 = 2 \times 239.5 + 26.7 + 0.1$

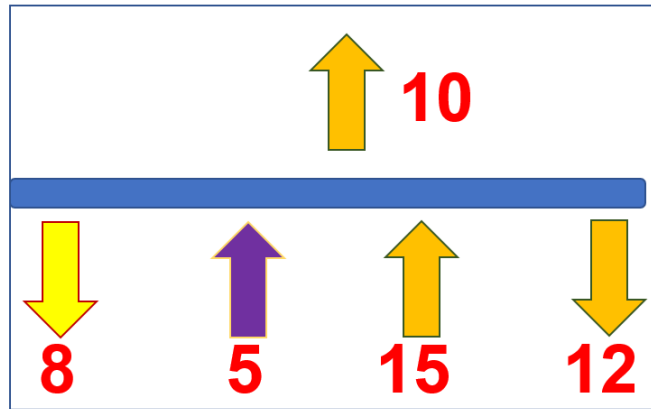
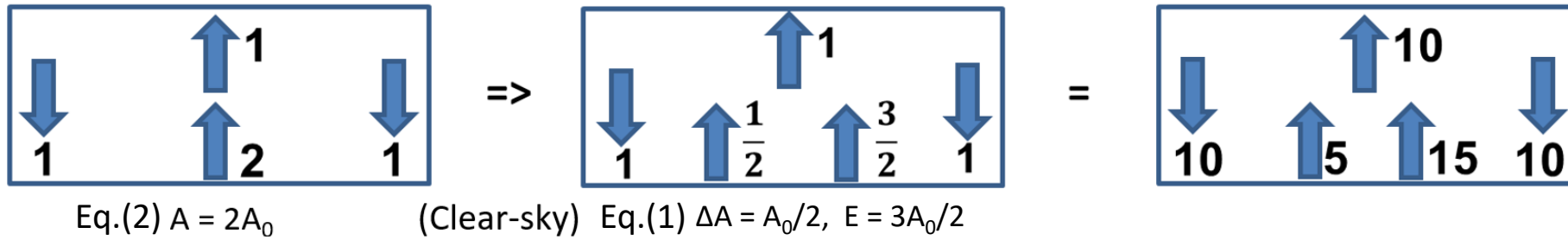
Eqs. (3) and (4) express fundamental physical requirements, verified by 30 years of GEWEX.

Any future global energy flow estimate, climate report, sensitivity study, water change prediction, cloud forcing and CRE-feedback assessment should strictly satisfy these constraints with this exemplary accuracy.



The **N**-numbers, as solution of the equations

Pure geometry, no reference to GHGs



$$8 + 12 - 15 = 10 / 2$$

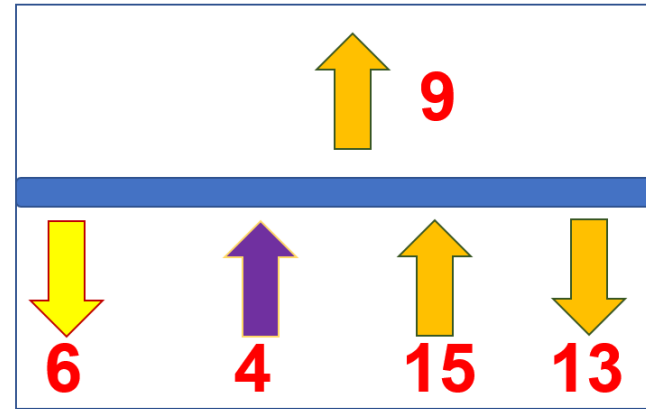
$$8 + 12 = 10 \times 2$$

Eq. (1) SFC Net = $A_0/2$

Eq. (2) SFC Tot = $2A_0$

Clear-sky

$L = 1$
 \Rightarrow



$$6 + 13 - 15 = (9 - 1)/2$$

$$6 + 13 = 9 \times 2 + 1$$

Eq. (3) SFC Net = $(A_0 - L)/2$

Eq. (4) SFC Tot = $2A_0 + L$

All-sky

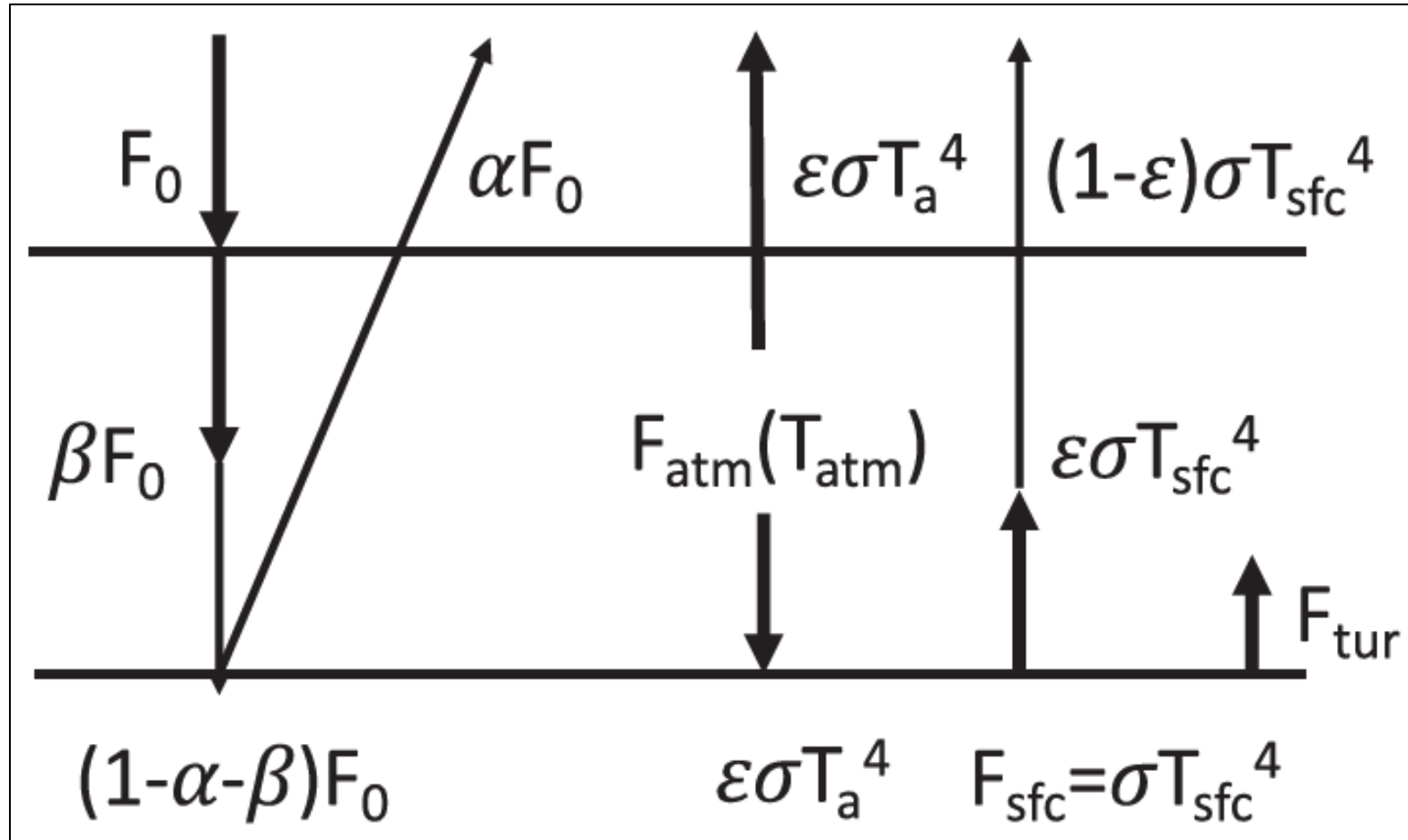
Ed4.2 is better (closer to **N**) in most flux components in the clear-sky

	Clear-sky	N	N × Unit	Ed4.1	Diff	Ed4.2	Diff
TOA	LW	10	266.80	266.01	-0.79	266.13	-0.67
Surface	SW Net	8	213.44	211.80	-1.64	211.41	-2.03
	LW down	12	320.16	317.40	-2.76	317.86	-2.30
	LW up	15	400.20	398.52	-1.68	398.61	-1.59
	LW Net	-3	-80.04	-81.12	-1.08	-80.75	-0.71
	TOT Net	5	133.40	130.68	-2.72	130.66	-2.74

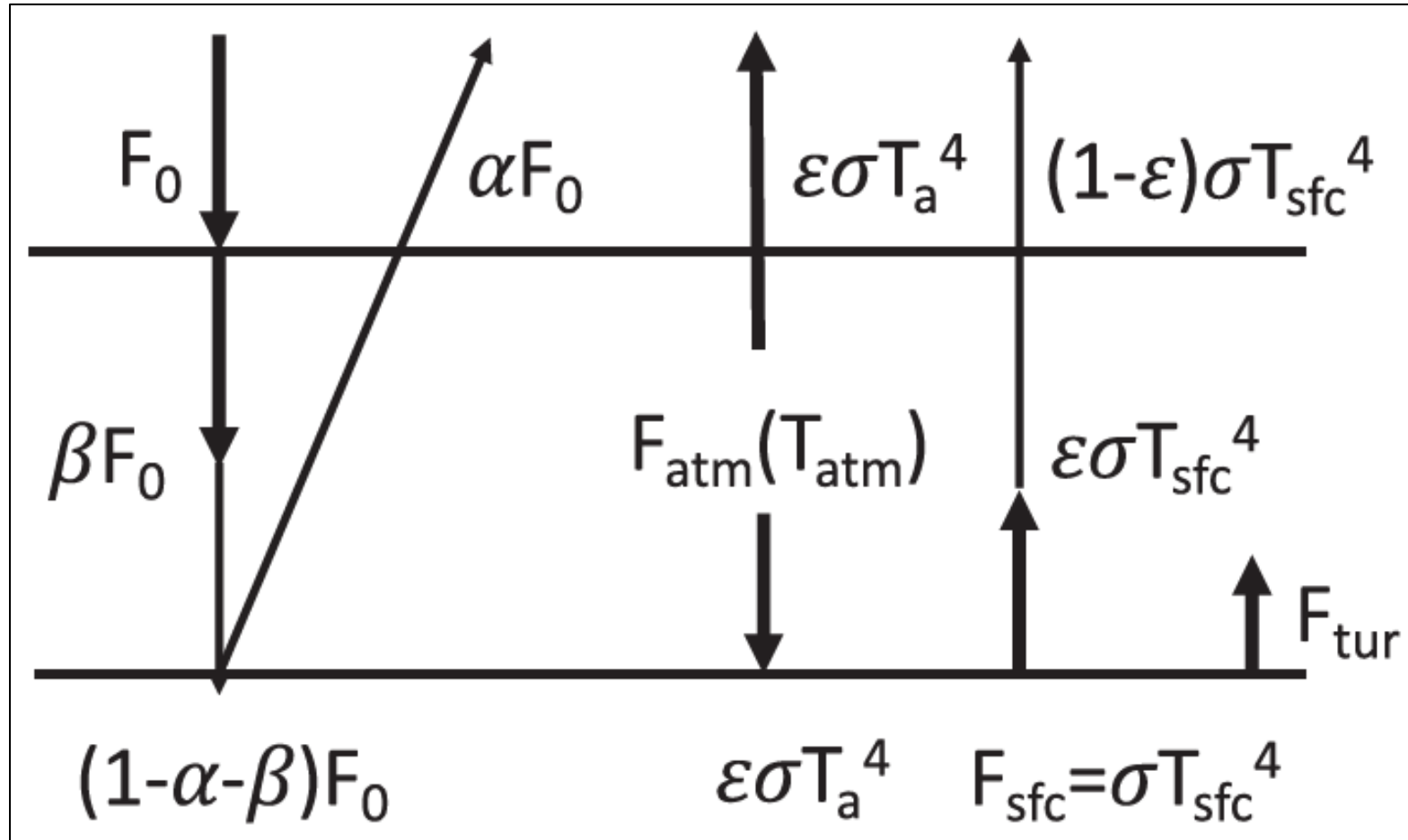
No significant difference, Ed4.1 is a bit better

	All-sky	N	N × Unit	Ed4.1	Diff	Ed4.2	Diff
TOA	LW	9	240.12	240.25	0.13	240.33	0.21
Surface	SW Net	6	160.08	163.69	3.61	163.65	3.57
	LW down	13	346.84	345.01	-1.83	346.11	-0.73
	LW up	15	400.20	398.75	-1.45	398.42	-1.78
	LW Net	-2	-53.36	-53.74	-0.38	-52.31	1.05
	TOT Net	4	106.73	109.95	3.22	111.34	4.61
	LW CRE	1	26.68	25.77	-0.91	25.80	-0.88

But what about α and β ?



Starting point: The simplest greenhouse model



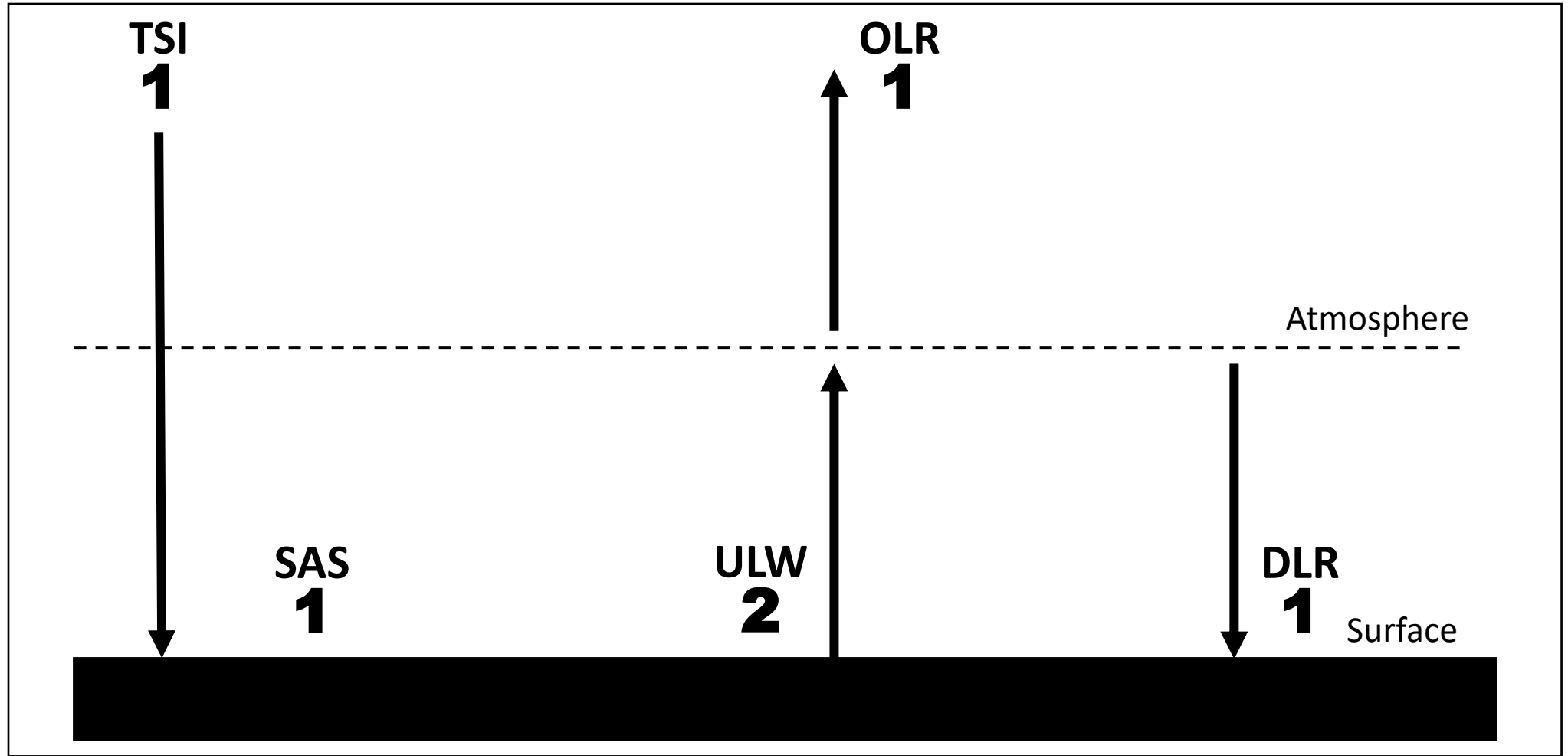
$$\alpha = \beta = 0$$

$$\epsilon = 1$$

$$\sigma T_{\text{sfc}}^4 = 2\sigma T_a^4$$

$$F_{\text{tur}} = 0$$

Starting point: The simplest greenhouse model

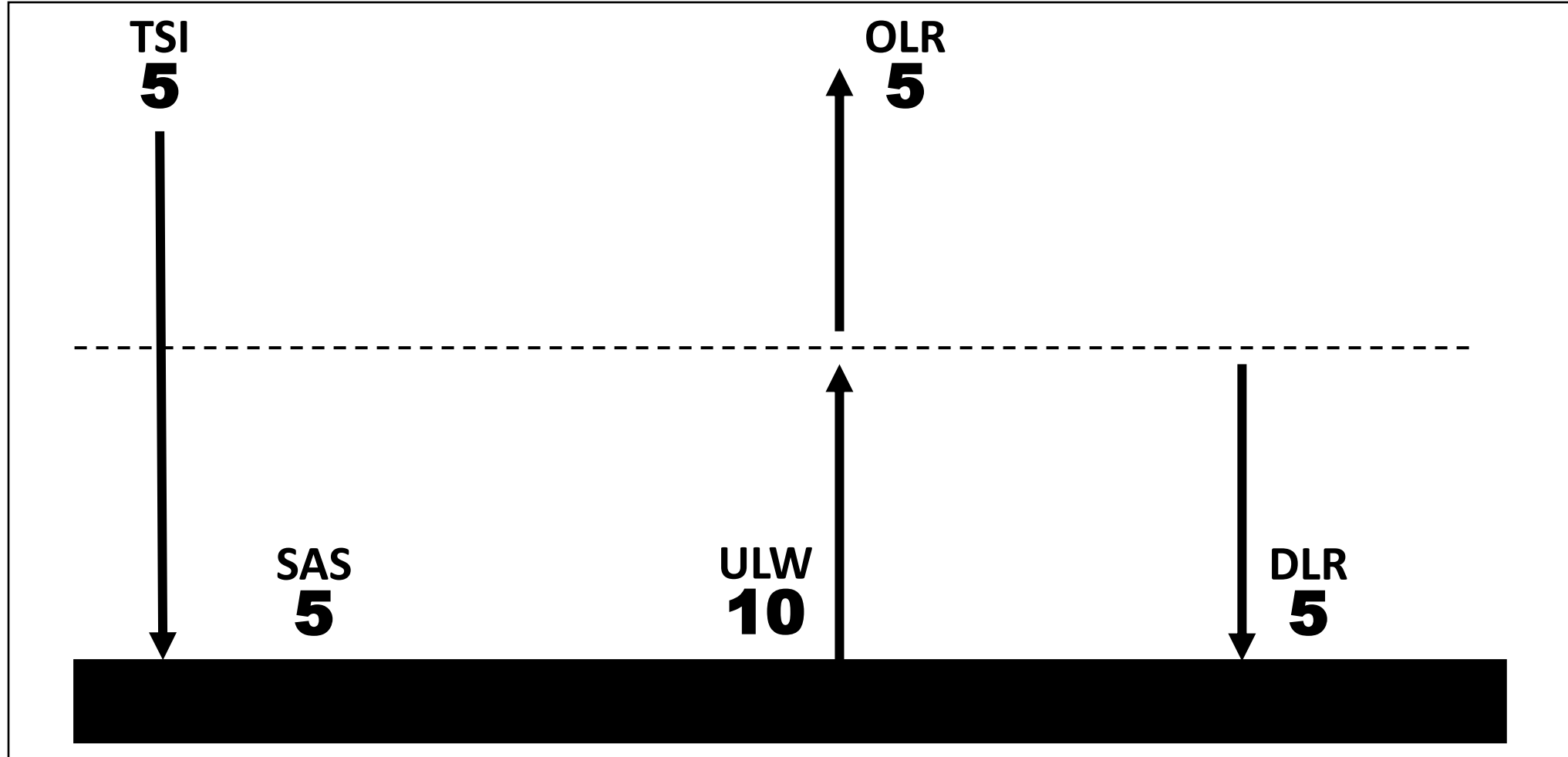


Solar Absorbed Surface (SAS)

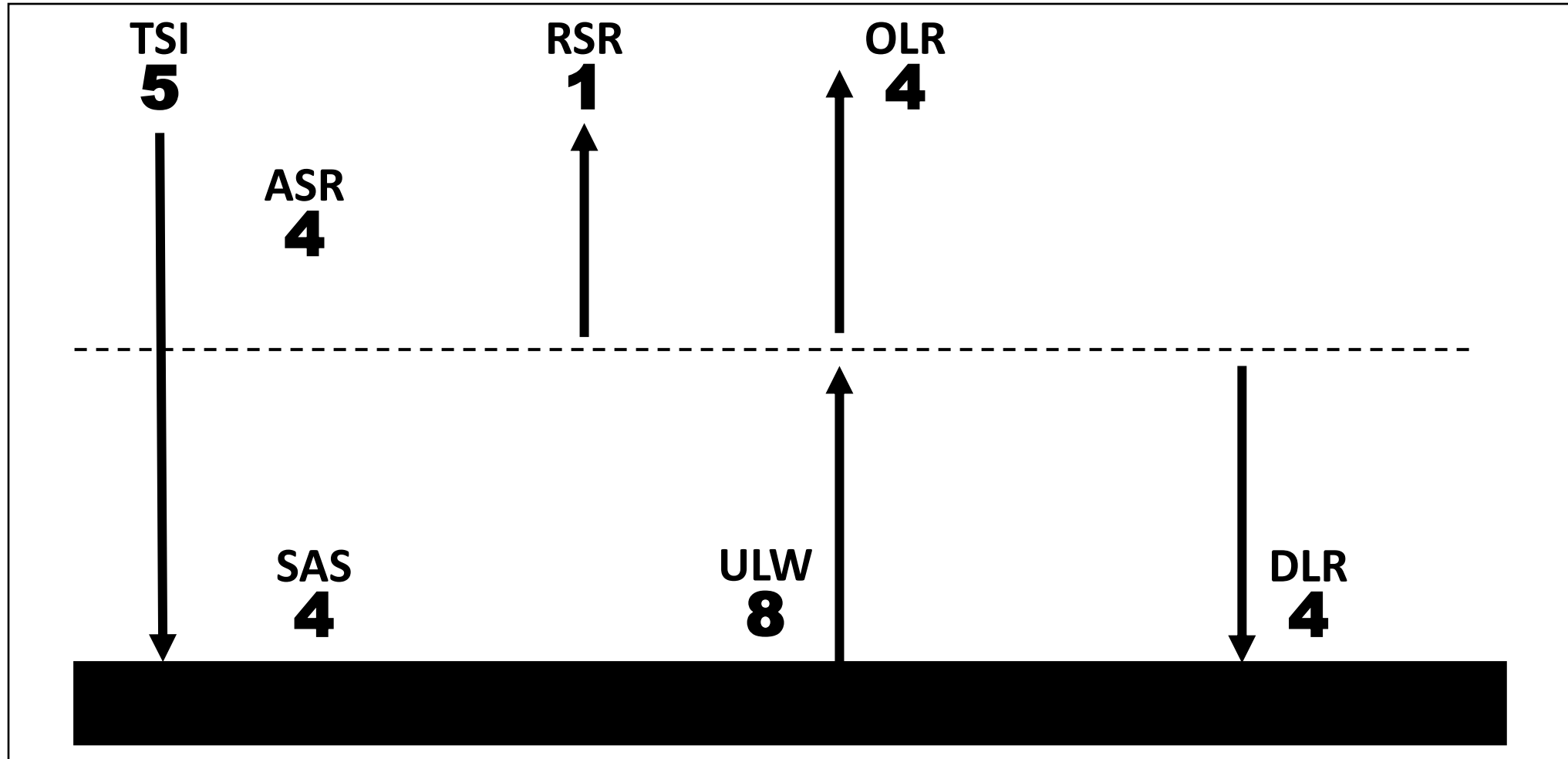
Upward LongWave (ULW)

Downward Longwave Radiation (DLR)

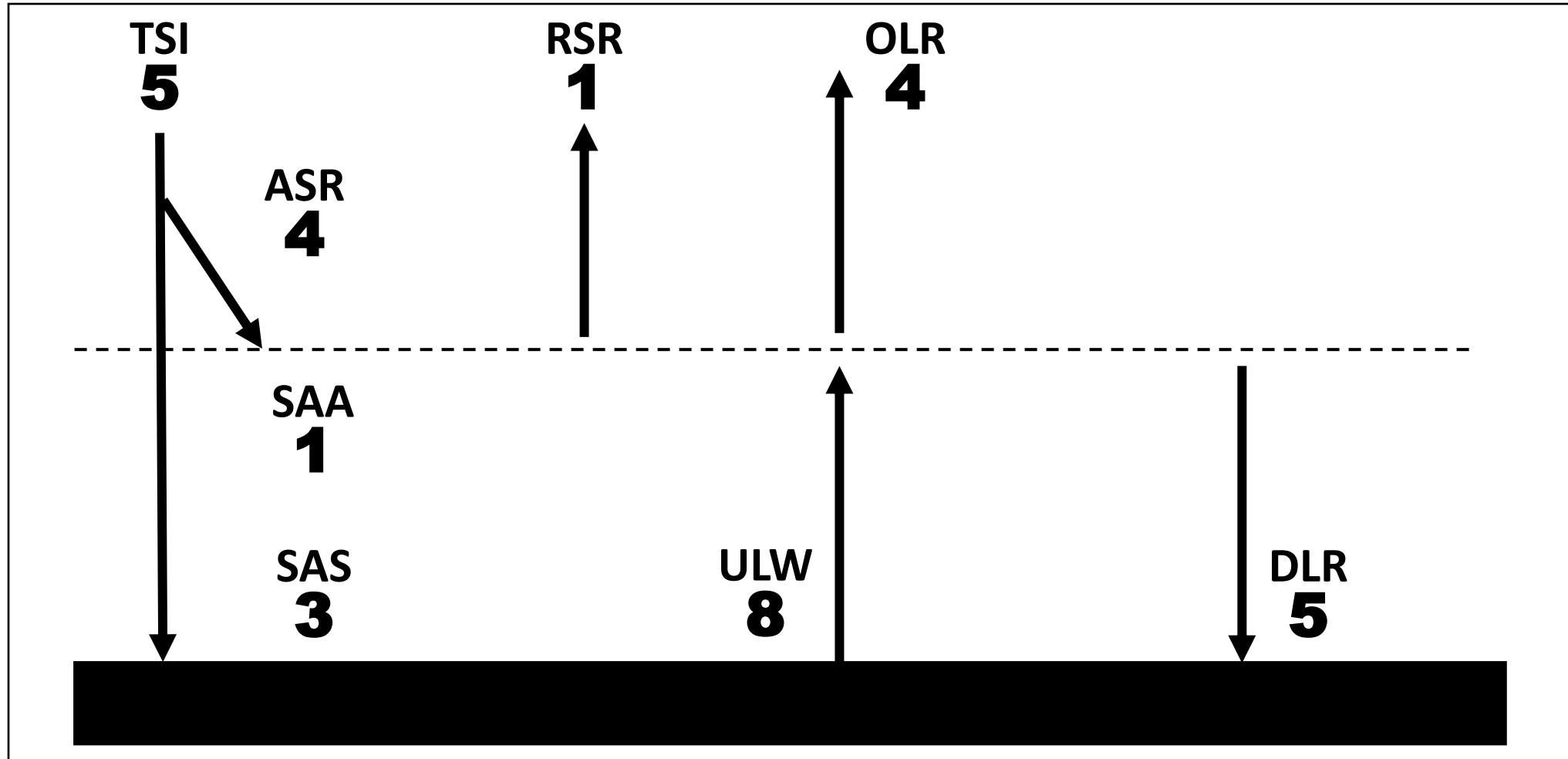
Multiply by 5



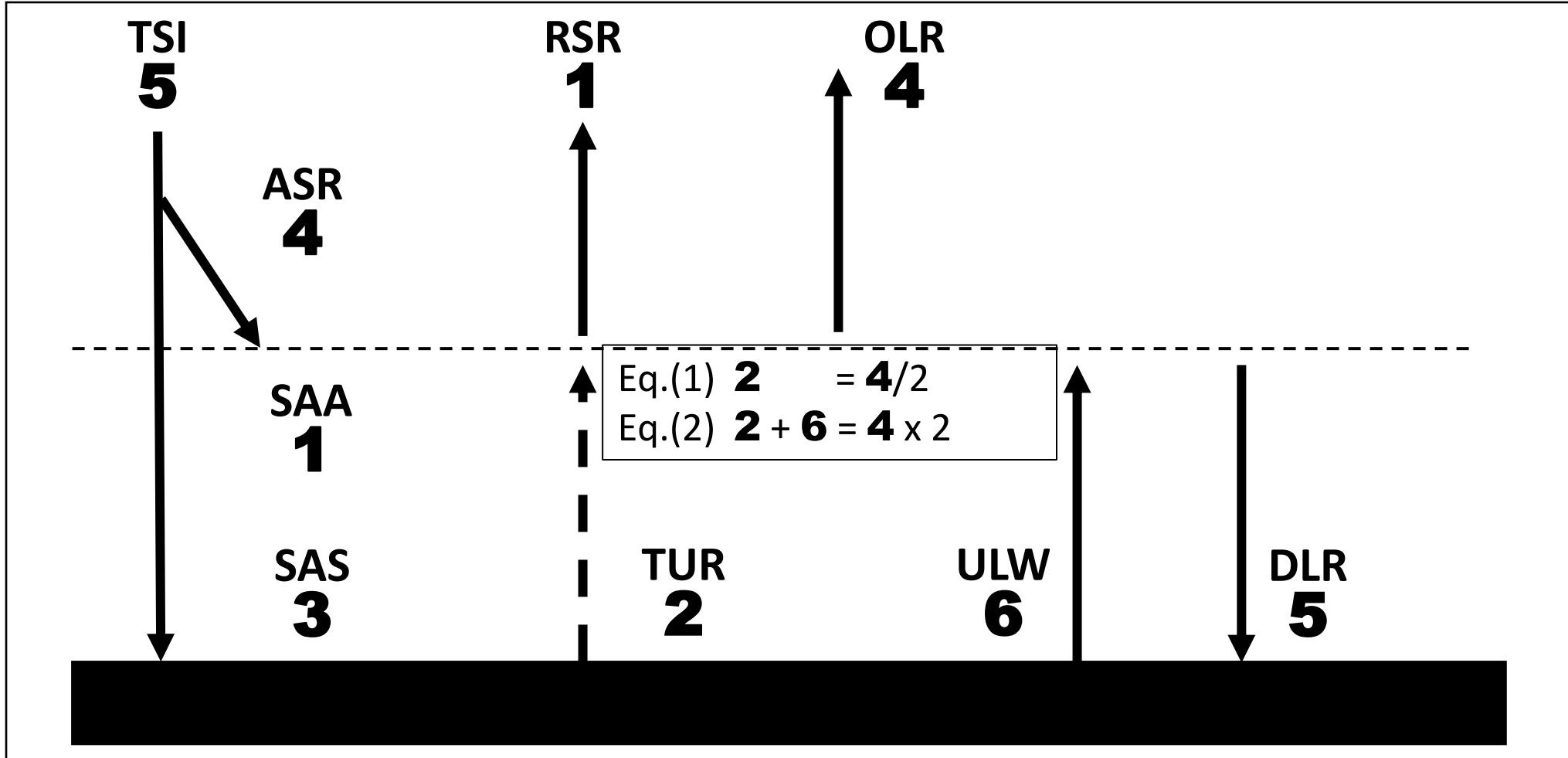
Introduce **1** unit RSR at TOA; $\alpha = 1/5$



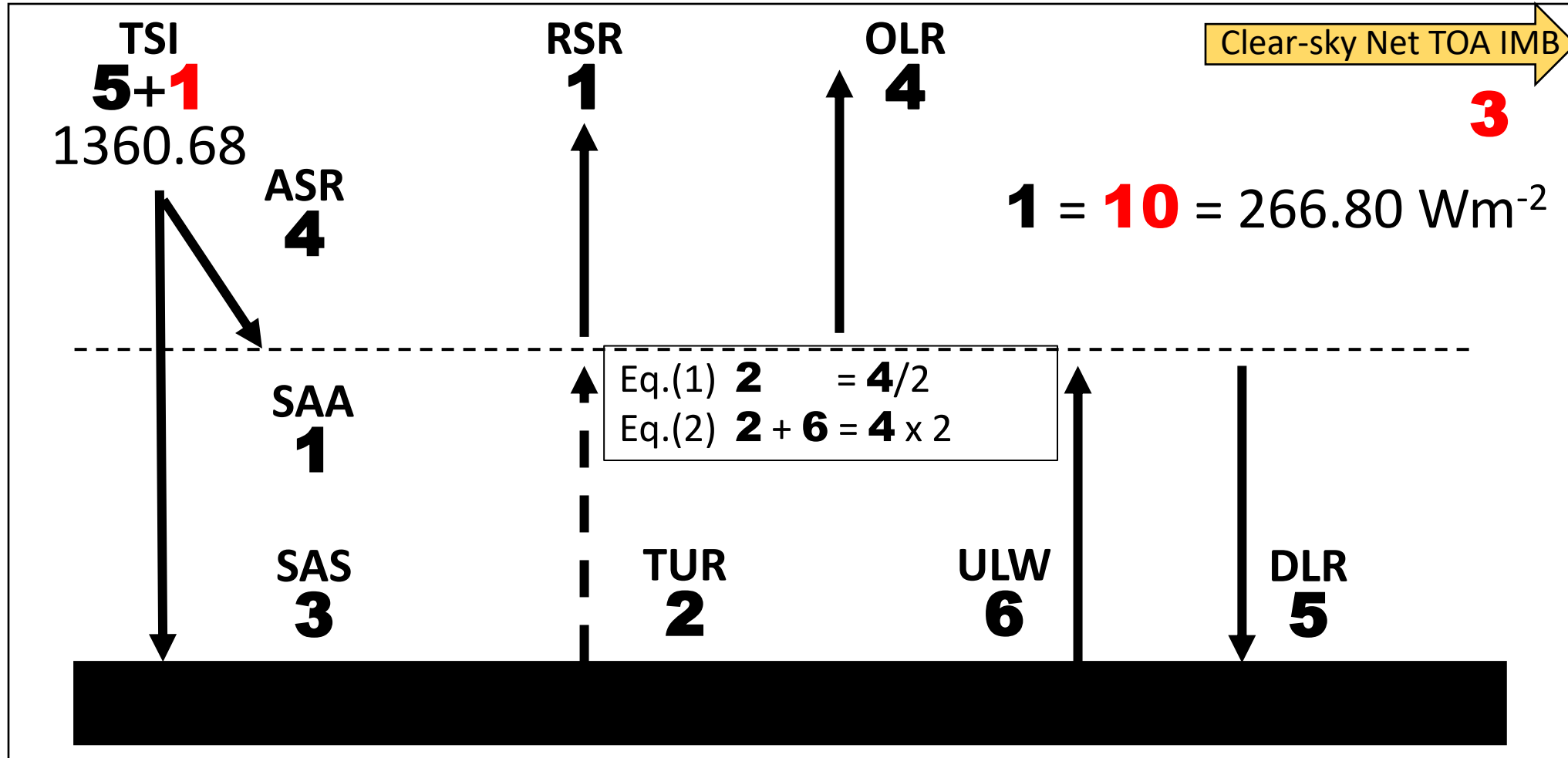
Allow **1** unit solar absorption in atmosphere; $\beta = 1/5$



Add **2** units turbulence to satisfy Eqs. (1) and (2)

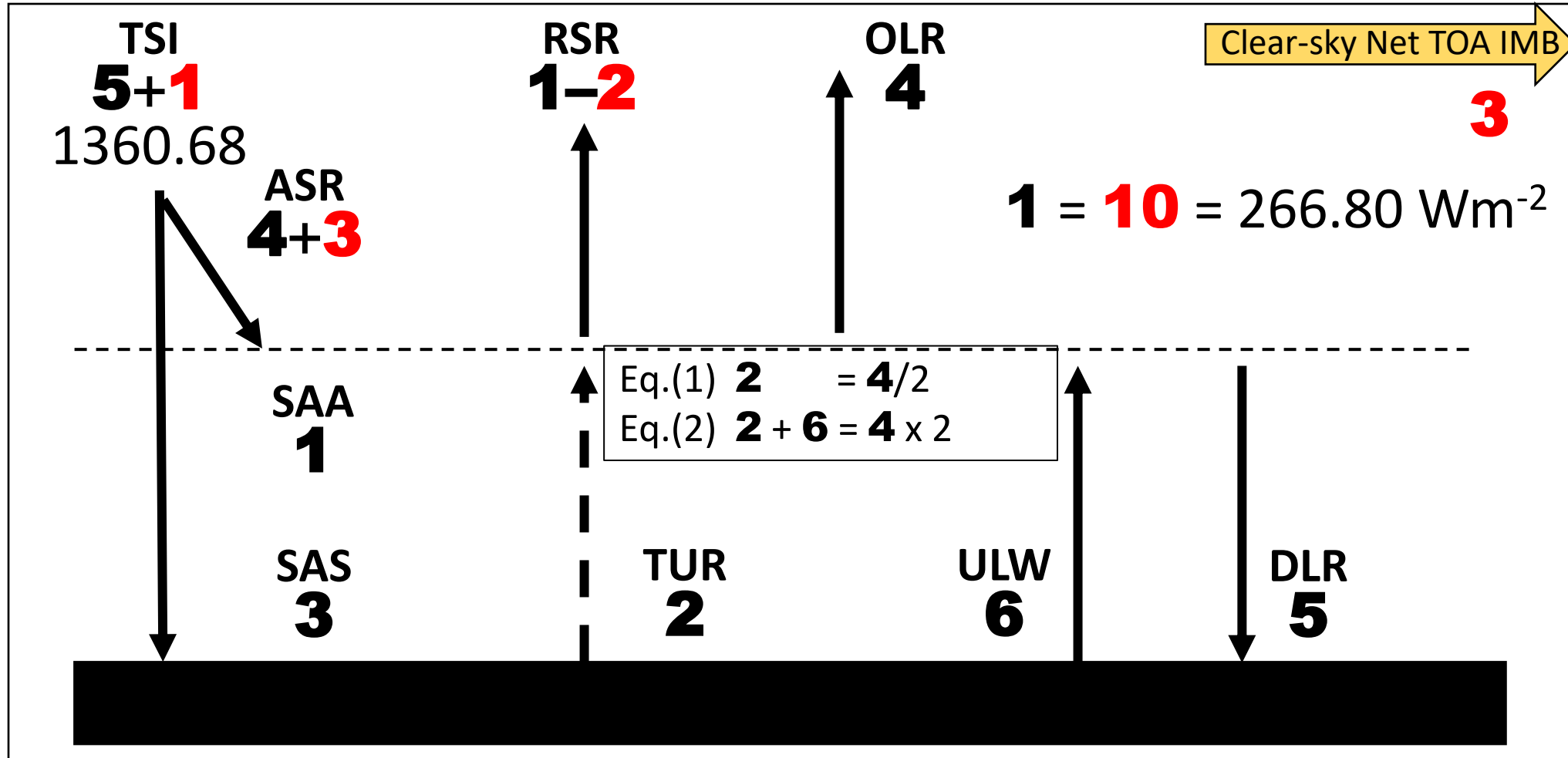


Calibrate to TSI: **1** (black) unit is **10** (red) units



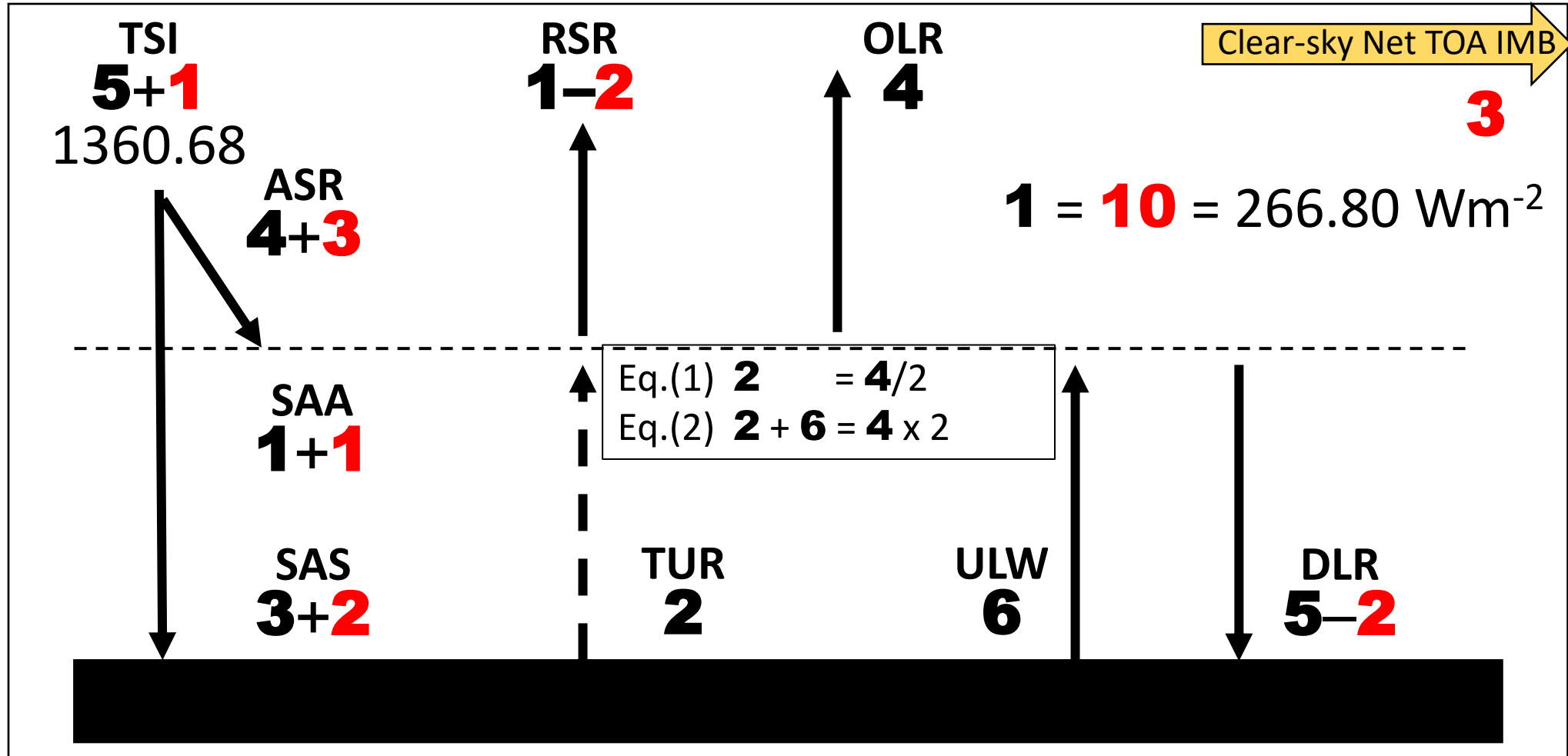
I created **2** (red) units hiatus

Solution: Reflect **2** (red) units less



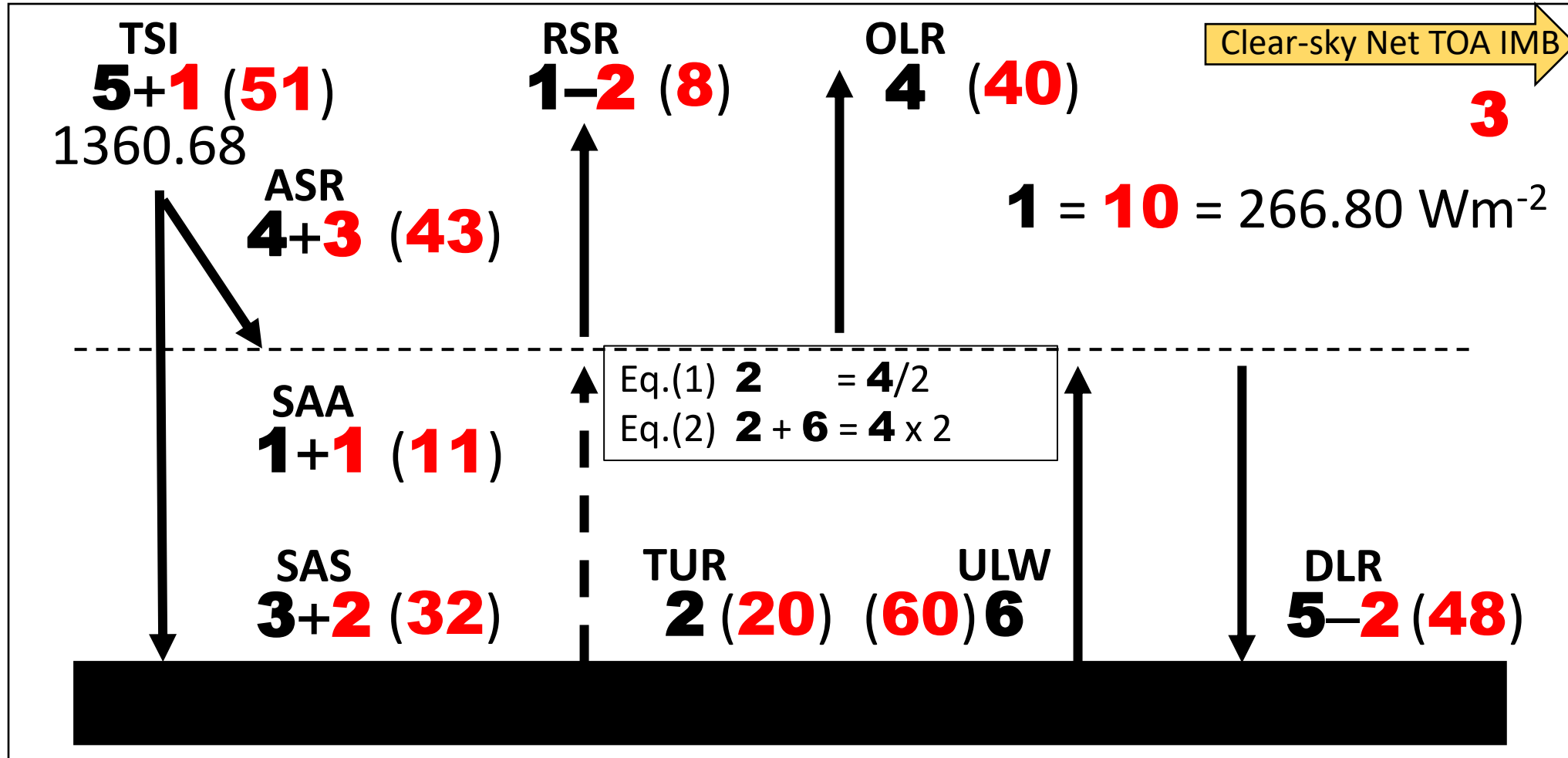
Absorption will be **3** (red) units more

Re-distribute the absorption: **1** in ATM, **2** at SFC



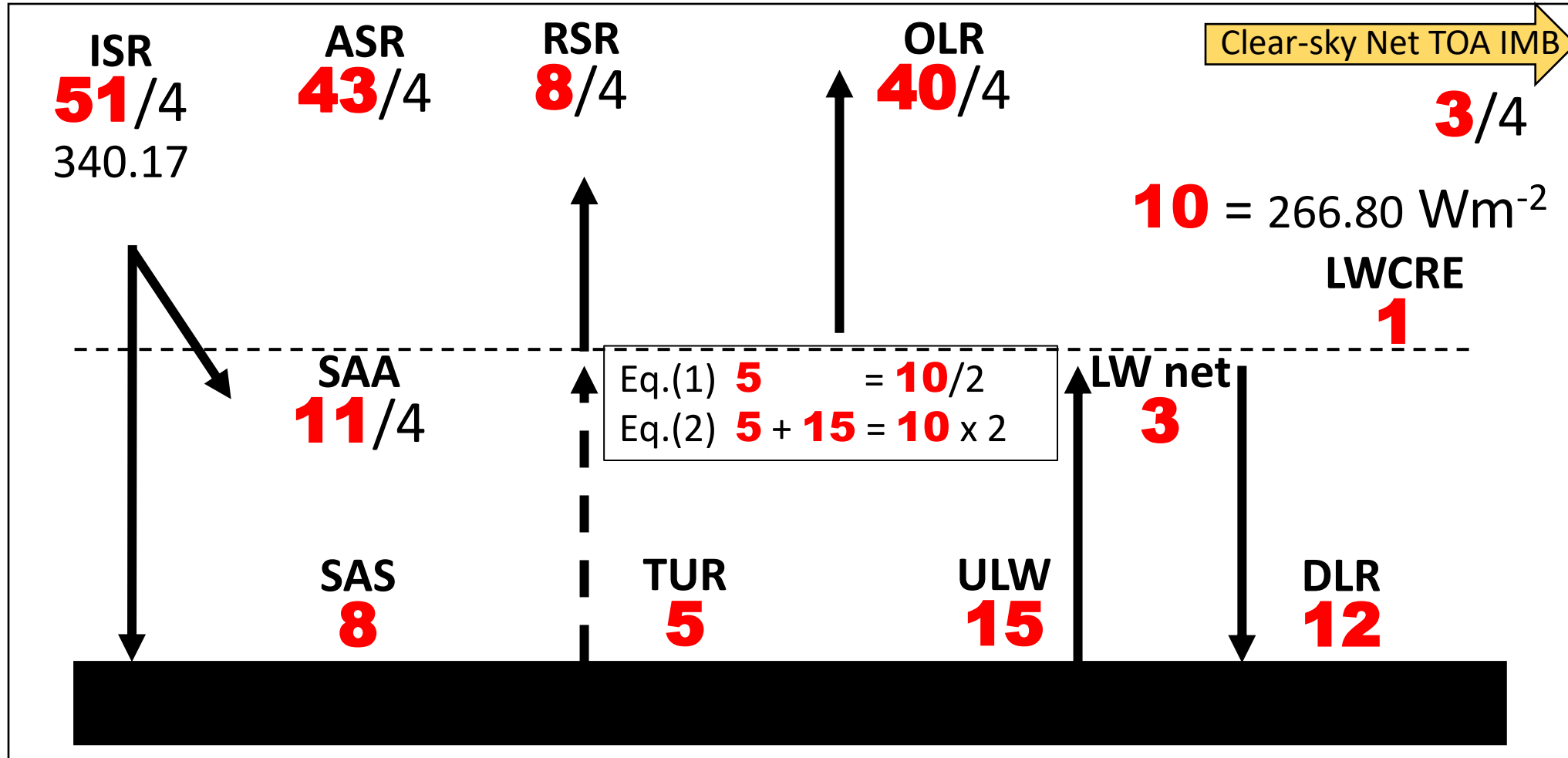
Ready. My clear-sky on the disk.

Transform to red units



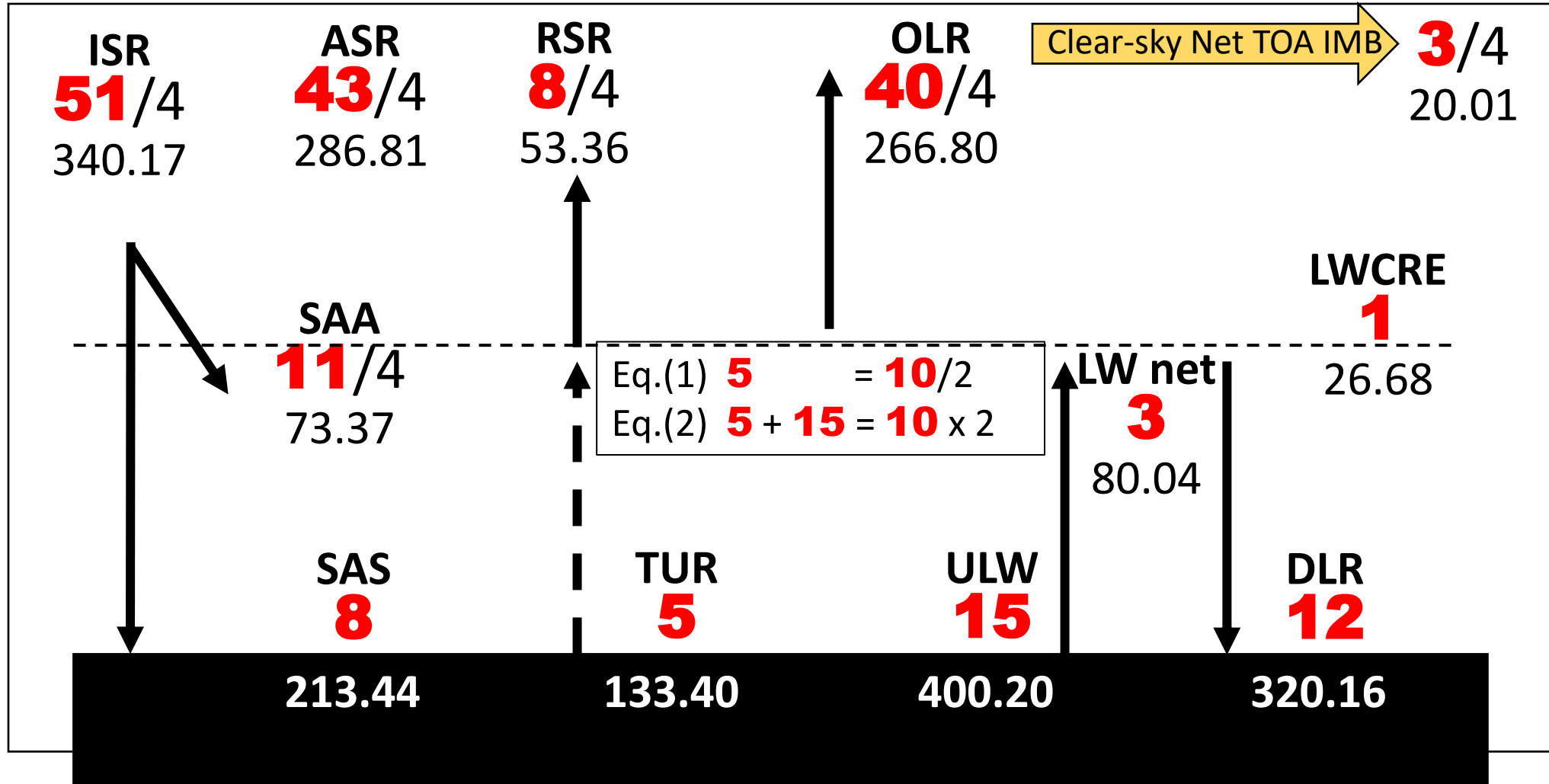
The only input parameter is TSI

Divide by 4

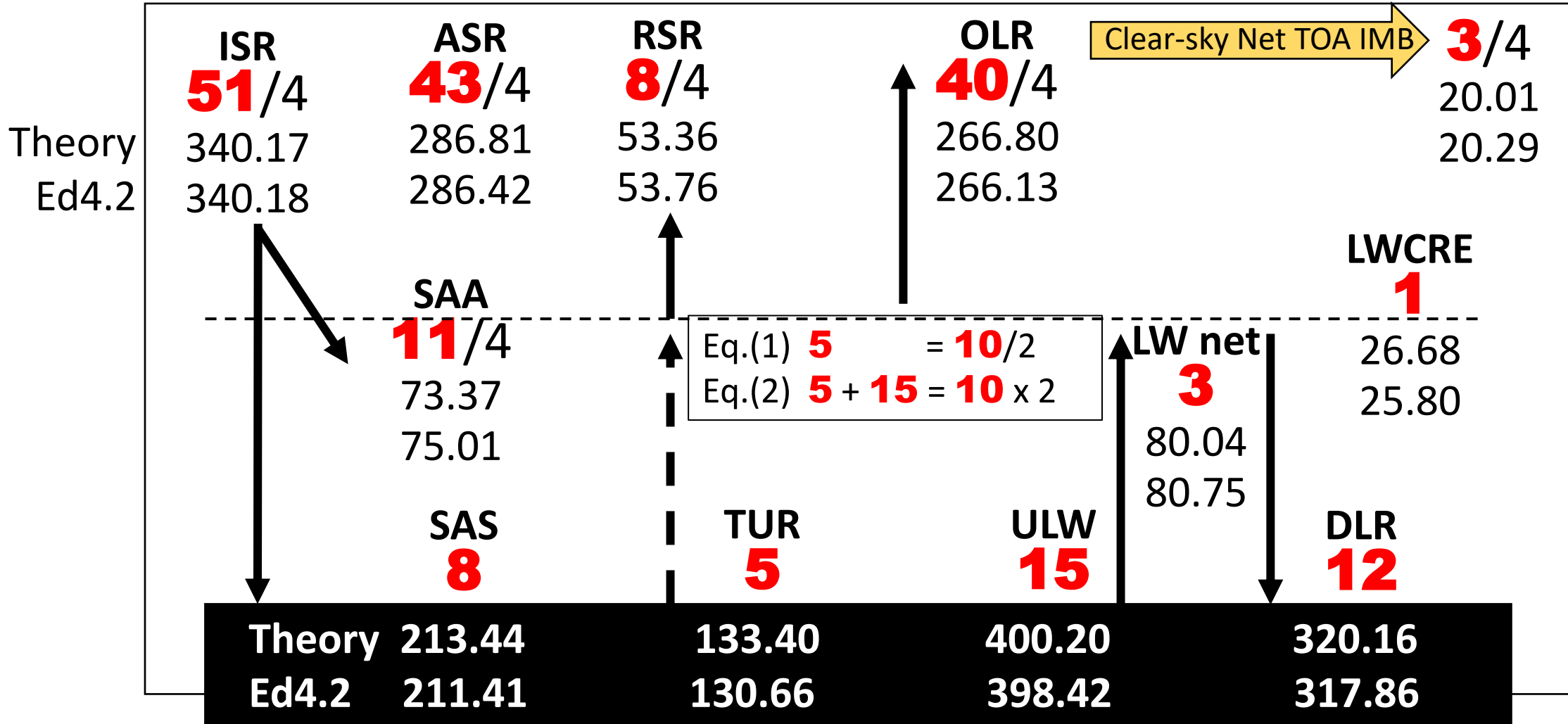


My clear-sky on the sphere.

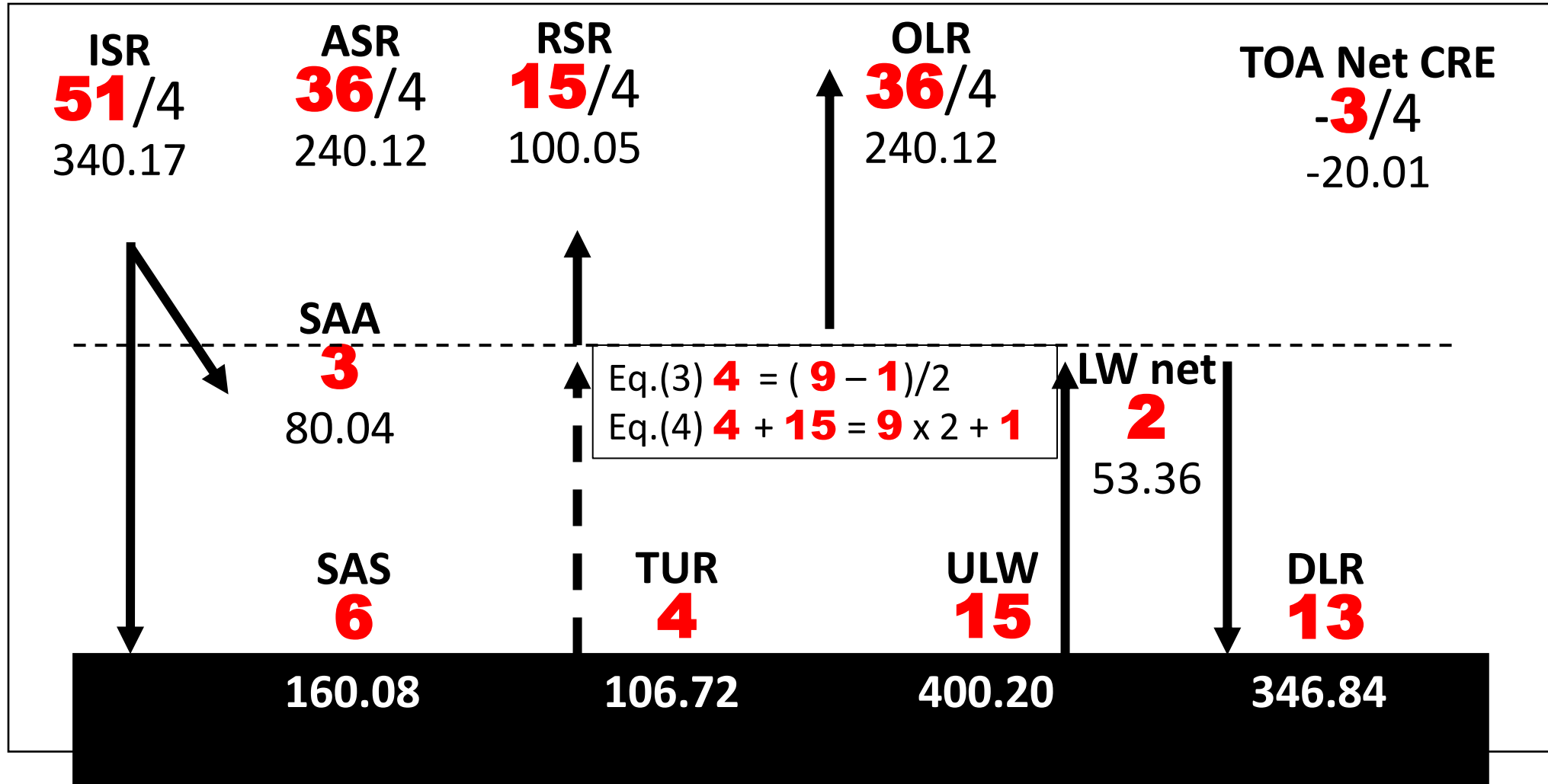
The only input parameter is TSI



Theory vs EBAF Ed4.2, clear-sky



OLR **10** → **9**, My all-sky system on the sphere



The only input parameter is TSI

Theory vs Ed4.2, all-sky, $\alpha = 15/51 = 5/17$, $\beta = 12/51 = 4/17$

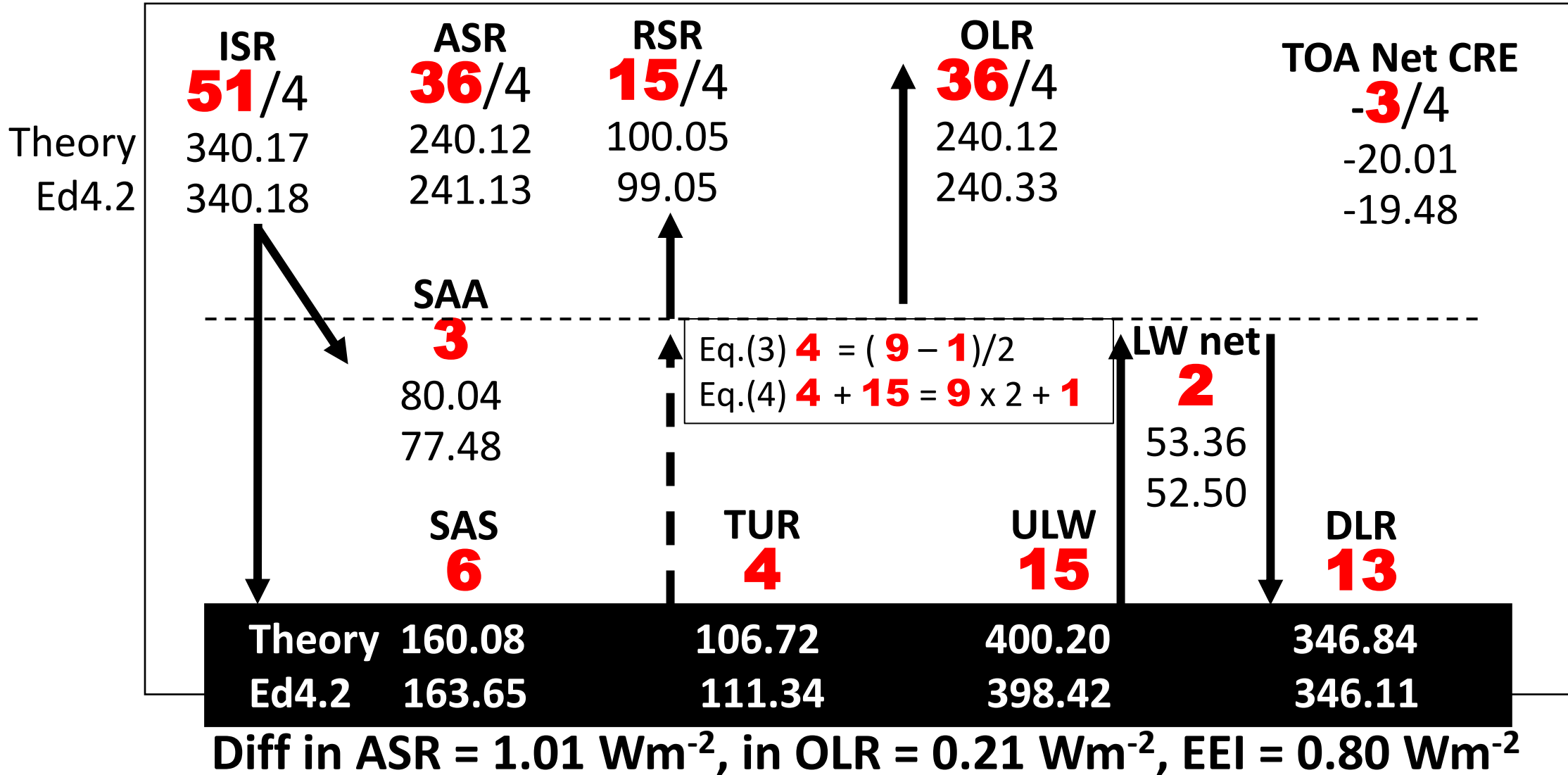


Table 2-1. Theory vs observation for global mean clear-sky fluxes for April 2000-March 2022 (W m^{-2})

	Clear-sky	N	N × Unit	EBAF Ed4.2	Difference
Clear-Sky TOA	SW insolation	51 /4	340.17	340.18	0.01
	LW	40 /4	266.80	266.13	-0.67
	SW	8 /4	53.36	53.76	0.40
	Net	3 /4	20.01	20.29	0.28
Clear-sky Surface	LW down	12	320.16	317.86	-2.30
	LW up	15	400.20	398.61	-1.59
	LW Net	-3	-80.04	-80.75	-0.71
	SW Net	8	213.44	211.41	-2.03
	SW + LW Net	5	133.40	130.66	-2.74

Table 4-1. Theory vs observation for global mean TOA and surface fluxes and CREs for EBAF Edition 4.2 for April 2000 to March 2022 (W m^{-2}).

	All-sky	N	N × Unit	EBAF Ed4.2	Diff
TOA	SW insolation	51 /4	340.17	340.18	0.01
	SW up	15 /4	100.05	99.05	-1.00
	LW up	36 /4	240.12	240.33	0.21
	TOT Net	0	0	0.8	0.80
Surface	SW Net	6	160.08	163.65	3.57
	LW down	13	346.84	346.11	-0.73
	LW up	15	400.20	398.42	-1.78
	LW Net	-2	-53.36	-52.31	1.05
	TOT Net	4	106.72	111.34	4.62
	CRE				
TOA	SW	-7 /4	-46.69	-45.28	1.41
	LW	1	26.68	25.80	-0.88
	Net	-3 /4	-20.01	-19.48	0.53

Concluding

- My talk: TOA SW Up is part of the **N**-system
- EEl: Not only ASR – OLR, but $\Delta\text{ASR}(\mathbf{N}) - \Delta\text{OLR}(\mathbf{N})$
- The meeting: EBAF Ed4.2 is closer to **N** in most components
- Earth Energy Budget: Eqs. (1) — (4) are compulsory

Last minute: extras, comments

EBAF-TOA Edition 4.2

23 years (March 2000 – February 2023)

- Observed :
- ISR = 340.19 Wm⁻²
- TSI = 4.0034 × 340.19 = 1361.92 Wm⁻²

- Theory with geodetic weighting:
- LWCRE = TSI/51 × (4/4.0034) = **1** = 26.68 Wm⁻²
- LWCRE (with spherical weighting) = 26.70 Wm⁻²

It is frequently stated that

Net CRE = SW CRE + LW CRE

Yes, but by def.:

- TOA Net CRE \equiv RSR(clear) – RSR(all) + OLR(clear – OLR(all) =
- TOA Net CRE = ISR – ASR(clear) – [ISR – ASR(all)] + LWCRE =
- TOA Net CRE = ASR(all) – ASR(clear) + [OLR(clear) – OLR(all)] =
- TOA Net CRE = – [ASR(clear) – OLR(clear)] + EEI(all) = EEI(all) – EEI(clear).

In equilibrium (EEI (all) = 0):

- TOA net CRE = – EEI(clear) = – $3/4$ = – 20.01 Wm⁻²
- TOA clear IMB = EEI(clear) = ASR – OLR = $43/4$ – $40/4$ = $3/4$ = 20.01 Wm⁻²

To understand the global character of TOA Net CRE, no clouds are needed.

It depends only on clear-sky values: SW absorption and LW emission (and EEI(all)).

Clear-Sky Greenhouse Effect at GFDL

$$\text{LWCRE (theory)} = \mathbf{1} = 26.68 \pm 0.01 \text{ Wm}^{-2}$$

$$G (\text{clear, theory}) = \mathbf{15} - \mathbf{10} = \mathbf{5} = 133.40 \pm 0.05 \text{ Wm}^{-2}$$

$$G (\text{GFDL AM4}) = 133.4 \pm 0.6 \text{ Wm}^{-2}$$

Quantifying the Drivers of the Clear Sky Greenhouse Effect, 2000–2016

Shiv Priyam Raghuraman ✉, David Paynter, V. Ramaswamy (JGR 2019)

Table 2

Global Mean and Time Mean G Comparison Between Observational, Reanalysis, and Modeling Data Sets Over March 2000 to August 2016

Quantity	ERBE	CE 4.1 “c”	CE 4.1 “t”	ERA-Interim	GFDL AM4
G_{Oceans}	146 ± 7	131.3 ± 0.5	134.1 ± 0.5	134.8 ± 0.6	135.0 ± 0.5
G	–	129.7 ± 0.6	132.4 ± 0.6	133.1 ± 0.7	133.4 ± 0.6

Overall conclusion

This is not a 'just-so' world.

Not "If this goes up, than that goes down" world.

This is a principled world.