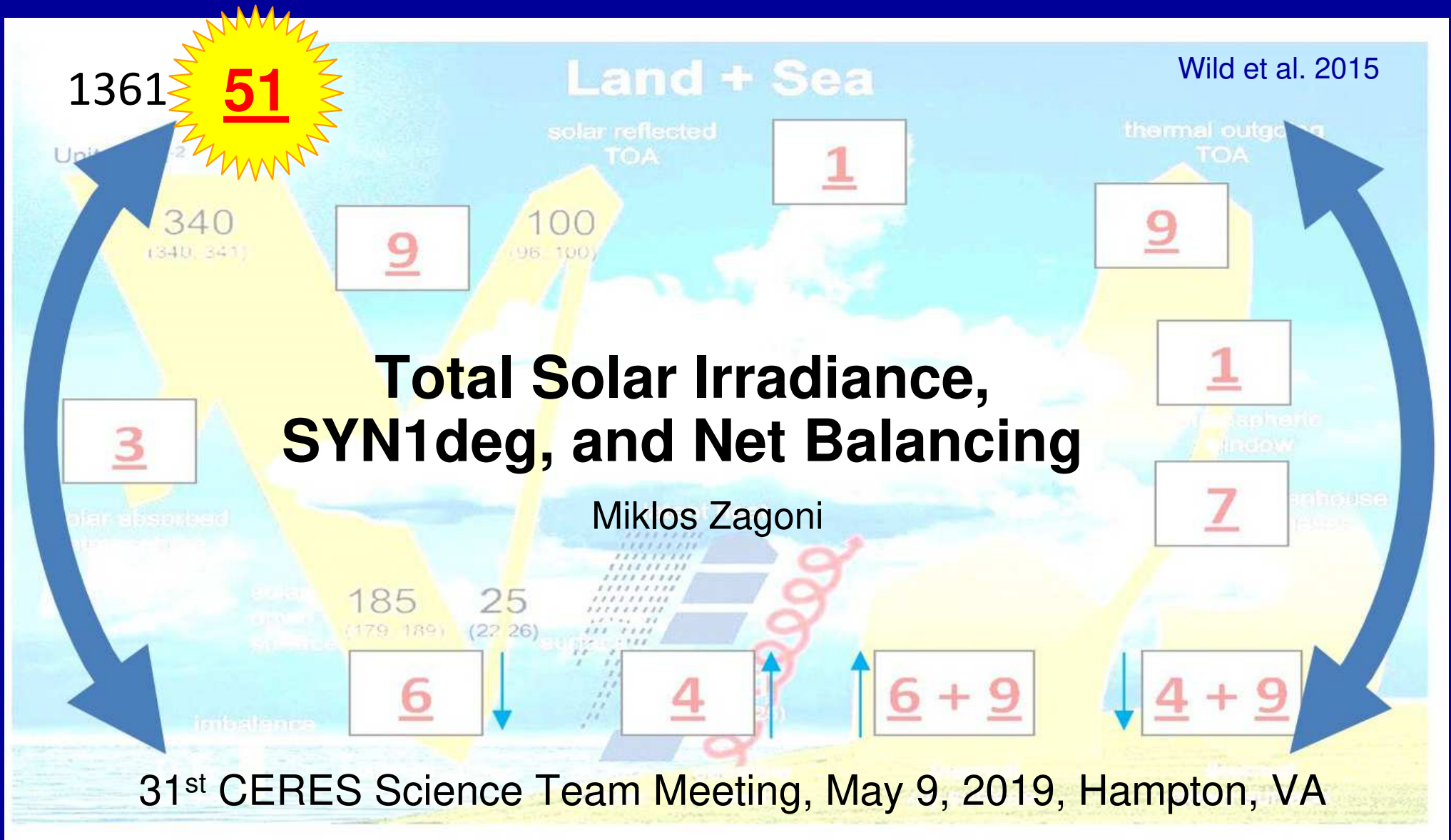


Patterns in the CERES Global Mean Data, Part 3.



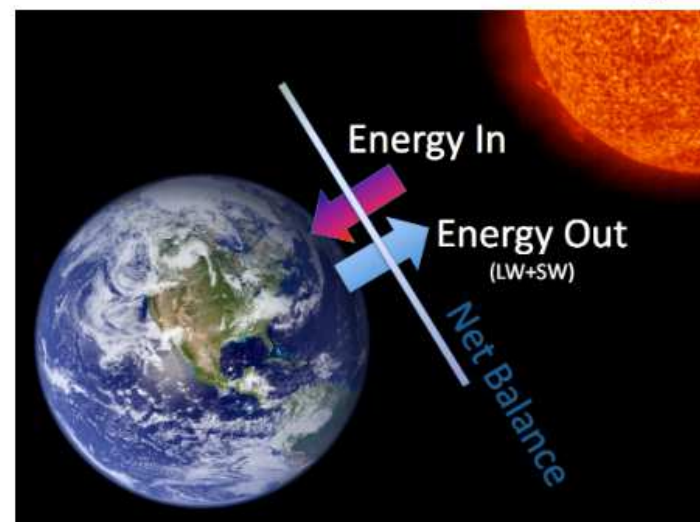
“Instead of the traditional paradigm of properties define processes, study how processes define property” — *Graeme Stephens*

DATA: CERES SYN1deg Ed4A TOA

All-sky, Oct 2000 – Sep 2018 (216 months)

- TSI = 1360.9 ± 0.5
- TOA SW in = **340.0** **EBAF Ed4.0**
- TOA LW = **238.6** **+1.5** **240.1**
- TOA SW up = **97.1** **+2.0** **99.1**
- Net = **4.3**

CERES Earth's Radiation Budget



Constraint I

TOA E in = TOA E out

Loeb et al. (2018) J Clim, Table 5

	<u>EBAF Ed2.8</u>		<u>EBAF Ed4.0</u>	
	Unadjusted	With constraint	Unadjusted	With constraint
Incoming Solar	339.8	339.8	340.0	340.0
All-sky LW	238.7	239.6	238.6	240.1
All-sky SW	97.9	99.6	97.1	99.1
All-sky net	3.2	0.63	4.3	0.71
Clear-sky LW	264.5	265.4	266.3	268.1
Clear-sky SW	51.5	52.5	52.3	53.3
Clear-sky net	23.8	21.9	21.4	18.6
LW CRE	25.8	25.8	27.7	27.9
SW CRE	−46.4	−47.1	−44.8	−45.8
Net CRE	−20.6	−21.3	−17.1	−17.9

A NEW Constraint in CERES SYN1deg Ed4A SFC + TOA Clear-sky Oct 2000 – Sep 2018

SFC SW down	=	242.65
– SFC SW up	=	– 28.40
= SFC SW net	=	214.25
SFC LW down	=	317.77
– SFC LW up	=	– 397.23
= SFC LW net	=	– 79.46
SFC SW+LW net	=	134.79
TOA LW	=	268.15
TOA LW / 2	=	134.08
Diff	=	– 0.71

Constraint II

SFC SW+LW net

= TOA LW / 2

What Does Constraint II Mean?

As an illustration, consider the case of radiative equilibrium with black bodies emitting $B^*(0)$ or $B^*(\tau_1)$ at the two boundaries. The third terms on the right-hand side of (2.144) and (2.145) are now zero and

$$F/2\pi = B(0) - B^*(0) = B^*(\tau_1) - B(\tau_1). \quad (2.146)$$

Equation (2.146) requires a discontinuity in the Planck function, implying a discontinuity of temperature, at the boundary.

The class of approximation of which (2.140) is representative is extensive and a large number of different names and terms are used to describe members of the class: the *Schwarzschild–Schuster* approximation, the *Eddington* approximations, *Chandrasekhar's first*

Discontinuity in the Planck function at the boundary = $F/2\pi$

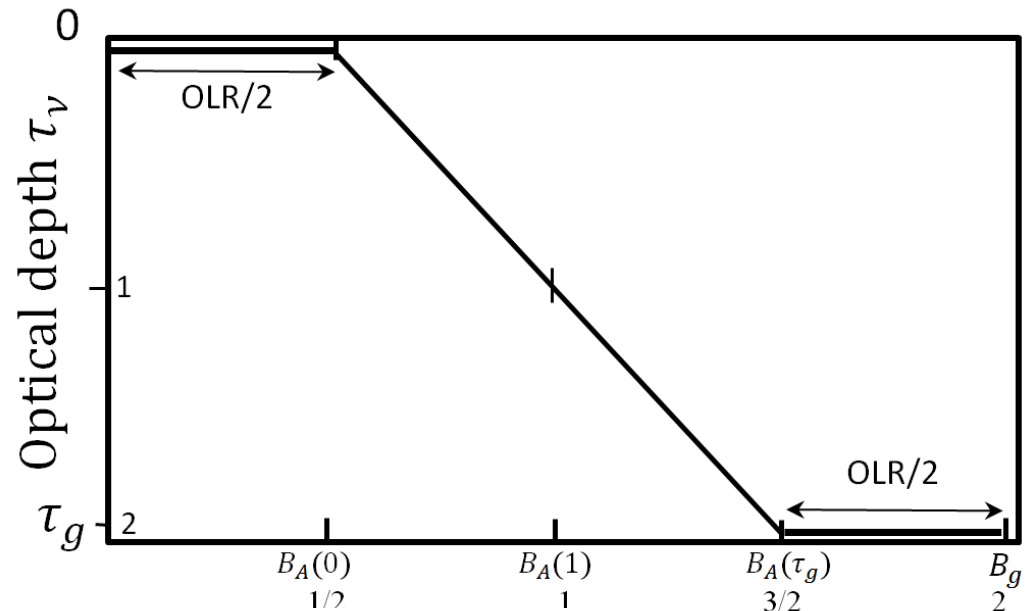
Goody and Yung (1989)

Discontinuity at the ground = $OLR/2$, independent of the optical thickness

Several textbooks, lecture notes (Grant Petty, Visconti, Chamberlain, Pierrehumbert)

$$\sigma T_A^4 = OLR(1 + \tau)/2$$

$$\sigma T_g^4 = OLR(2 + \tau)/2$$



$$\sigma T_g(\tau_g)^4 - \sigma T_A(\tau_g)^4 = OLR/2 \text{ independent of } \tau_g$$

The temperature at the bottom of the atmosphere at τ^* is given by Equation (3.47), so that we have a discontinuity between the air temperature and that of the surface

$$T_s^4 - T(\tau^*)^4 = T_e^4 / 2 \quad (3.49)$$

Discontinuity at the ground: SFC SW+LW net = $OLR/2$
Long-known theoretical requirement

Constraint II

in CERES EBAF Ed2.8 & Ed4.0

Clear-sky, CLIM YEAR

SFC SW+LW Net = 132.71

TOA LW = 265.82

(TOA LW) / 2 = 132.91

(TOA LW) / 2 – SFC Net = 0.2

SFC SW+LW Net = 130.41

TOA LW = 268.15

(TOA LW) / 2 = 134.07

(TOA LW) / 2 – SFC Net = 3.7

My Net Balancing II

Your (Constr I)

- SW gain = 1.7
- LW gain = 2.5

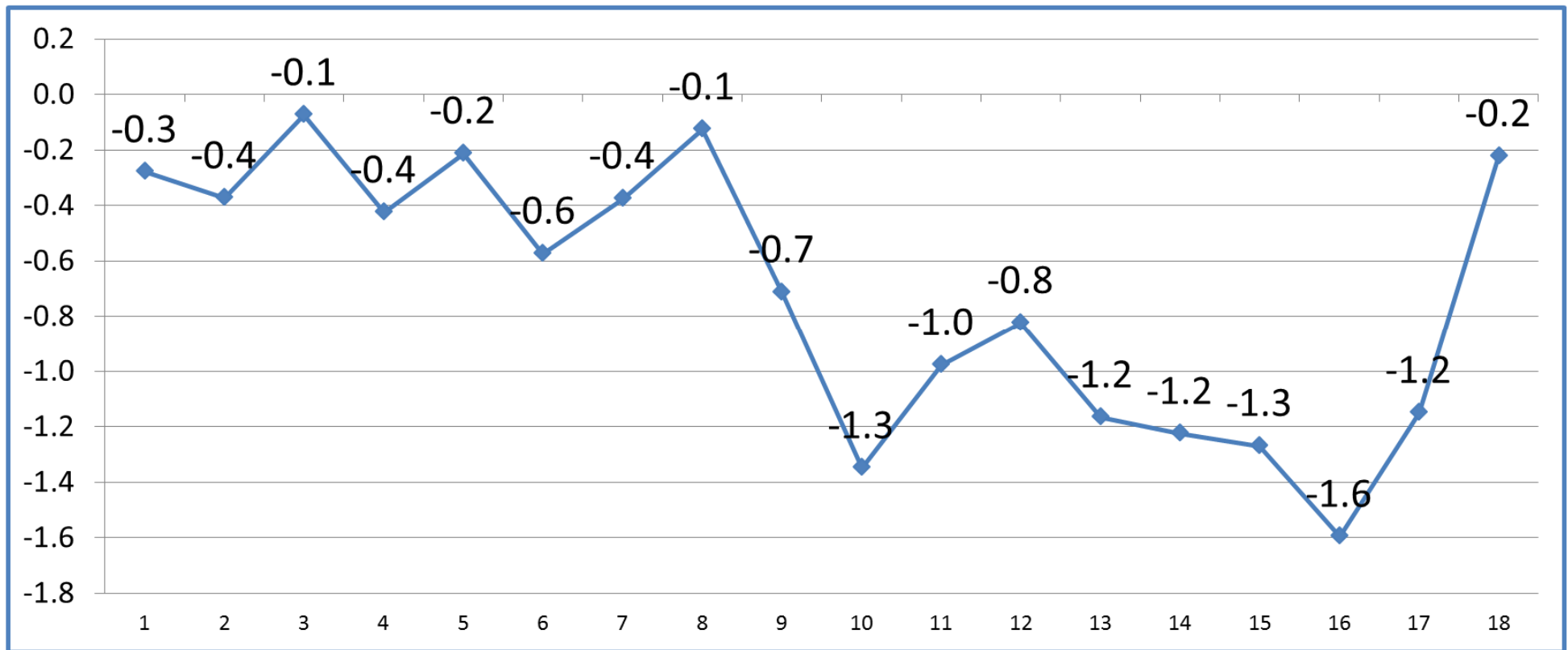
Parameter	TOA Flux adjustment (W/m ²)
Total SW	1.7
Total LW	2.5
Total Net	-4.2

Mine (Constr II)	SYN	My	EdMZ	Integers
SFC SW net	= 214.25	- 0.81	= 213.44	8
SFC LW net	= -79.46	- 0.58	= - 80.04	- 3
SFC SW+LW net	= 134.79	- 1.39	= 133.40	5
TOA LW	= 268.15	- 1.35	= 266.80	10
TOA LW/2	= 134.08	- 0.68	= 133.40	5
Diff	= - 0.71		0.0	

Earth's Energy Imbalance of the Second Kind

$$EEI_2 = TOA\ LW/2 - SFC\ SW+LW\ net$$

18 years, Oct 2000-Sep 2018

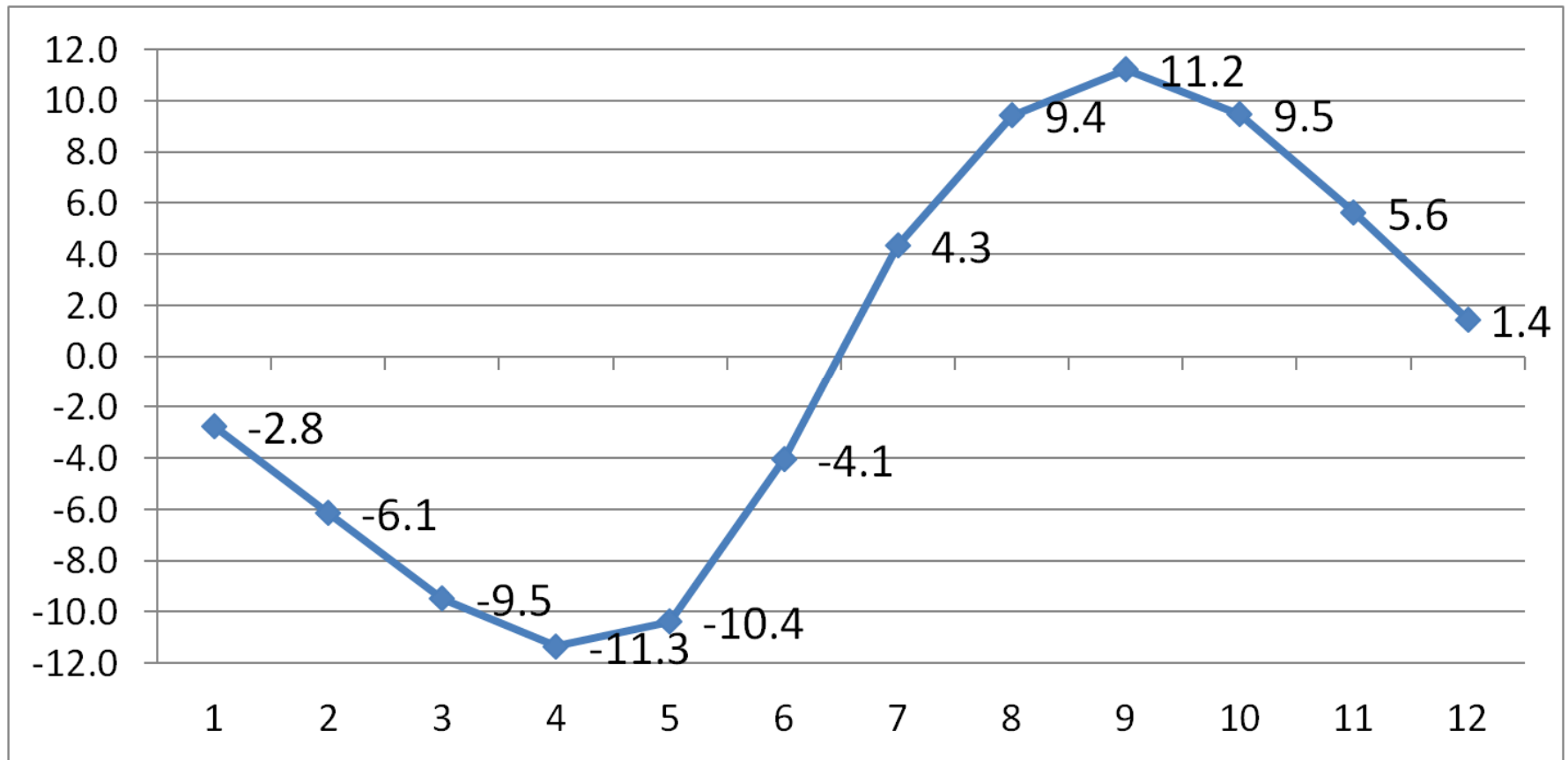


SYN1deg Ed4A 18-years

max -0.07 , min -1.60 , mean = -0.72 Wm^{-2}

$$EEI_2 = TOA\ LW/2 - SFC\ SW+LW\ net$$

12 months, Oct 2017-Sep 2018



SYN1deg Ed4A 12-months

max 11.21, min -11.34, mean = -0.22 Wm⁻²

$$EEI_2 = TOA \text{ LW}/2 - \text{SFC SW+LW net}$$

Area-weighted zonal means from N Pole to the Equator

Degree	SW net	LW net	SW + LW net	TOA LW	TOA LW/2	Area-weighted difference
80 – 90	6.3	– 12.9	– 6.7	35.6	17.8	24.5
70 – 80	16.3	– 26.6	– 10.3	72.6	36.3	46.6
60 – 70	54.4	– 39.3	15.1	111.8	55.9	40.8
50 – 60	112.3	– 53.1	59.2	153.6	76.8	17.6
40 – 50	159.7	– 66.9	92.8	196.2	98.1	5.4
30 – 40	204.5	– 79.5	125.0	238.2	119.1	– 5.9
20 – 30	239.8	– 80.1	159.7	273	136.5	– 23.2
10 – 20	264.4	– 71.7	192.7	289.4	144.7	– 48.0
0 – 10	270.6	– 61.3	209.3	286.6	143.3	– 66.0
Hemispheric mean	213.7	– 79.1	134.6	266.6	133.3	– 1.3

A THIRD constraint
in CERES SYN1deg Ed4A SFC + TOA
Clear-sky Oct 2000 – Sep 2018

SFC SW down	=	242.65
– SFC SW up	=	– 28.40
= SFC SW net	=	214.25
+ SFC LW down	=	317.77
= SFC SW+LW abs	=	532.02
TOA LW	=	268.15
2 × (TOA LW)	=	536.30
Diff	=	4.28

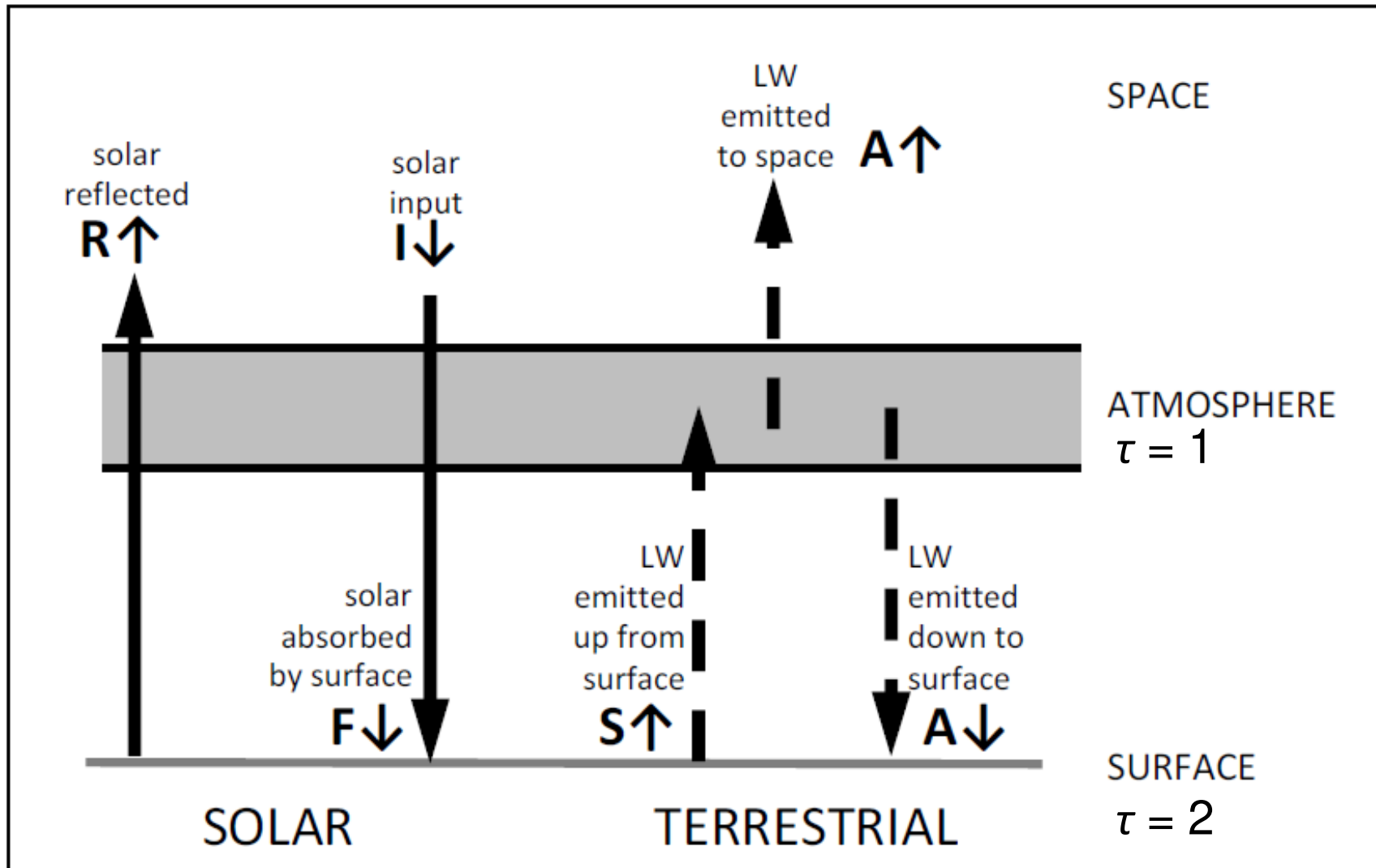
Constraint III

SFC SW+LW abs

= 2 TOA LW

Same confidence as
Constraint I.

What Does Constraint III Mean?



$$S = 2A = 2F$$

Modified from
Marshall-Plumb (2008)

Liou (1980)

Fig. 8.20, we may write down the energy balance equations at the top of the atmosphere and the surface, respectively, in the forms

$$Q(1 - \bar{r}) - \bar{\epsilon}\sigma T_a^4 - (1 - \bar{\epsilon})\sigma T^4 = 0, \quad (8.31)$$

$$Q(1 - \bar{r} - \bar{A}) + \bar{\epsilon}\sigma T_a^4 - \sigma T^4 = 0, \quad (8.32)$$

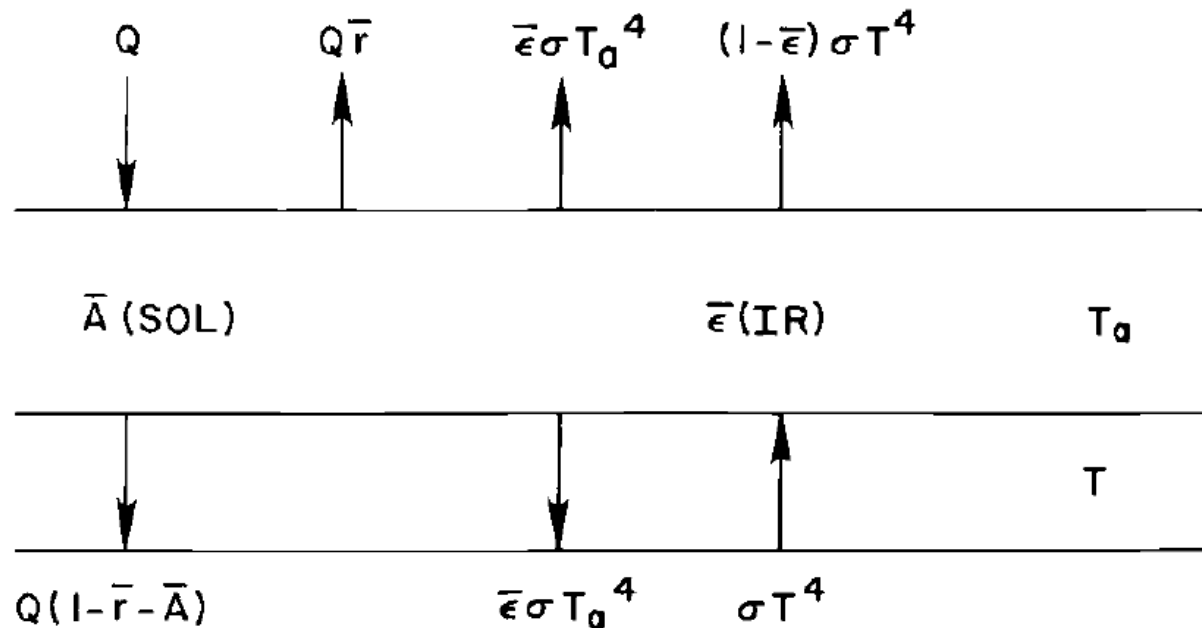


Fig. 8.20 Two-layer global radiative budget model.

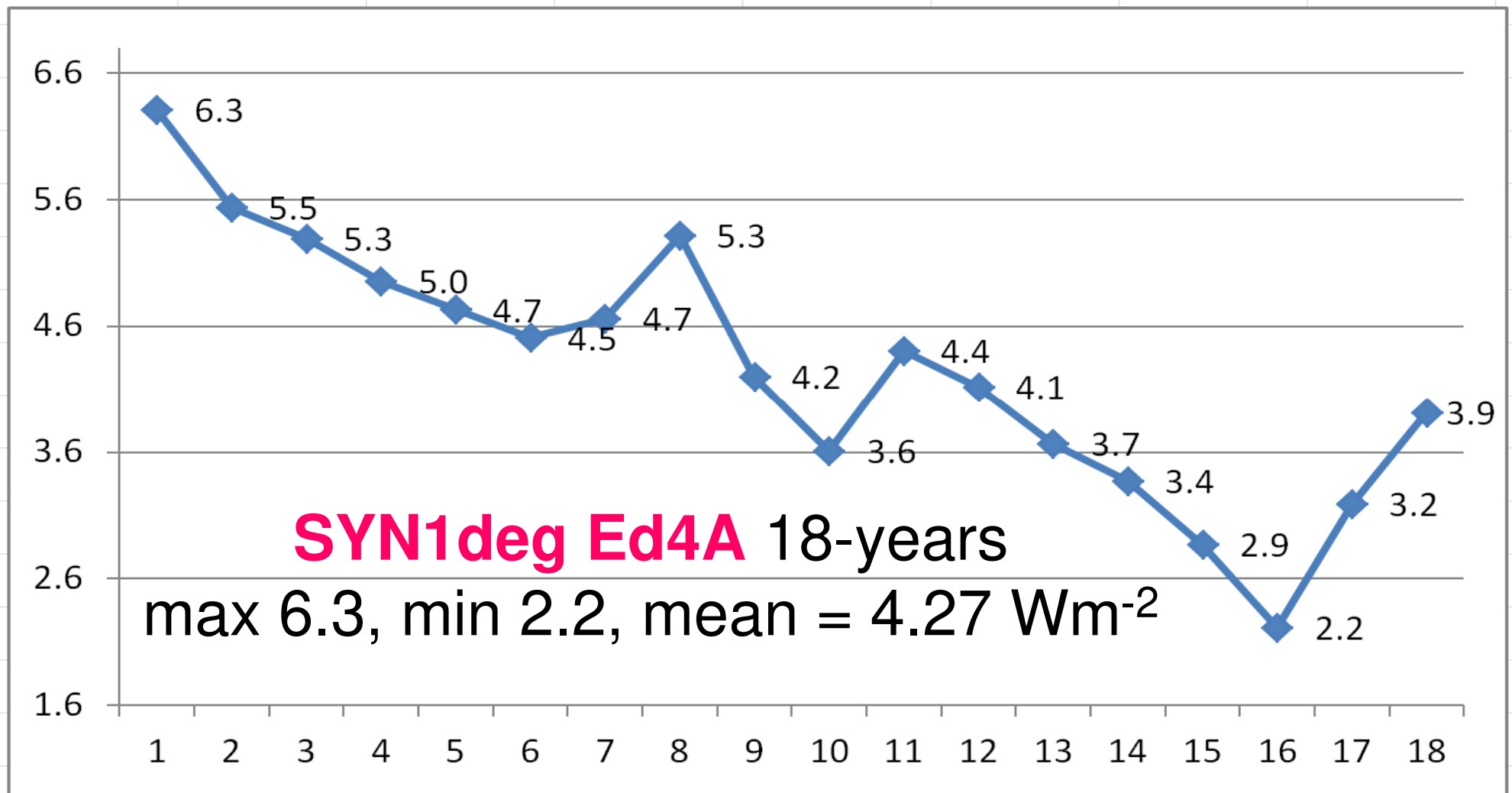
Trivial solution to the radiative transfer problem

with $\bar{A} = 0$ and $\bar{\epsilon} = 1$, $\sigma T^4 = 2\sigma T_a^4$

Earth's Energy Imbalance of the Third Kind

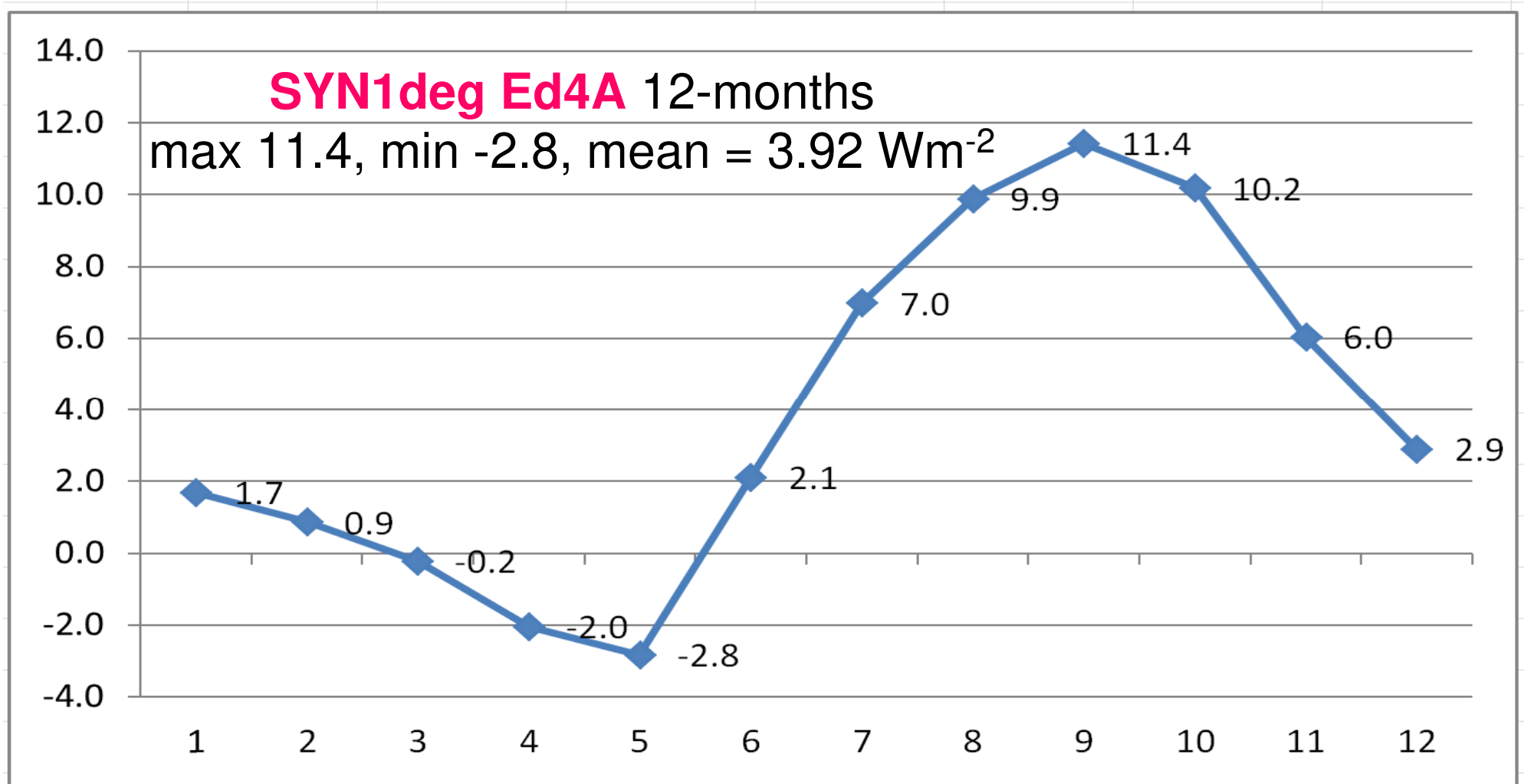
$$EEI_3 = 2TOA \text{ LW} - SFC \text{ SW} + LW$$

18 years, Oct 2000-Sep 2018



$$EEI_3 = 2TOA \text{ LW} - \text{SFC SW+LW}$$

12 months, Oct 2017-Sep 2018



Constraint III

in CERES EBAF Ed2.8

Clear-sky, CLIM YEAR

	SYN1deg		EBAF Ed2.8
SFC SW net	214.25	+ 0.09	= 214.34
SFC LW down	317.77	– 1.49	= 316.28
SW+LW gross	532.02	– 1.40	= 530.62
TOA LW	268.15	– 2.55	= 265.60
2(TOA LW)	536.30	– 5.10	= 531.20
DIFF	4.28		0.58

Constraint III

in CERES EBAF Ed4.0

Clear-sky, CLIM YEAR

	Ed4.0	SYN	My	EdMZ	N
SFC SW net	= 213.99 + 0.26	<= 214.25	− 0.81	= 213.44	8
SFC LW down	= 314.02 + 3.75	<= 317.77	+ 2.39	= 320.16	12
SW+LW abs	= 528.01 + 4.01	<= 532.02	+ 1.58	= 533.60	20
TOA LW	= 268.04 + 0.11	<= 268.15	− 1.35	= 266.80	10
2(TOA LW)	= 536.08 + 0.22	<= 536.30	− 2.70	= 533.60	20
DIFF	= 8.1	4.28		0.0	

The Three Musketeers: Truth, Law and Order

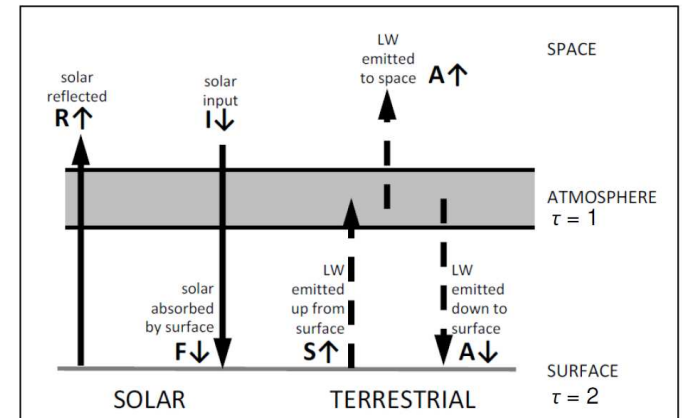
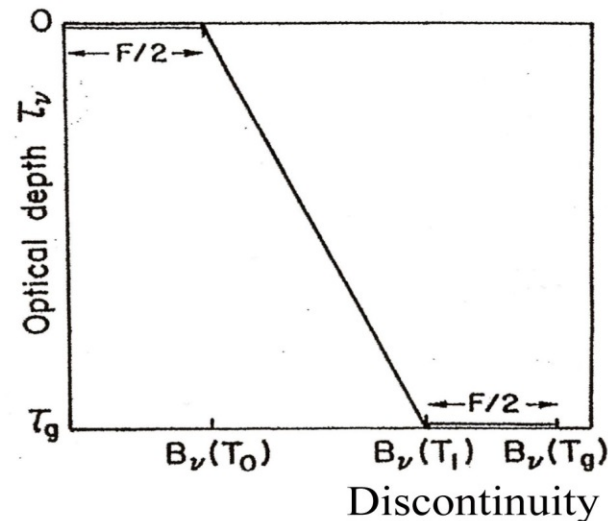
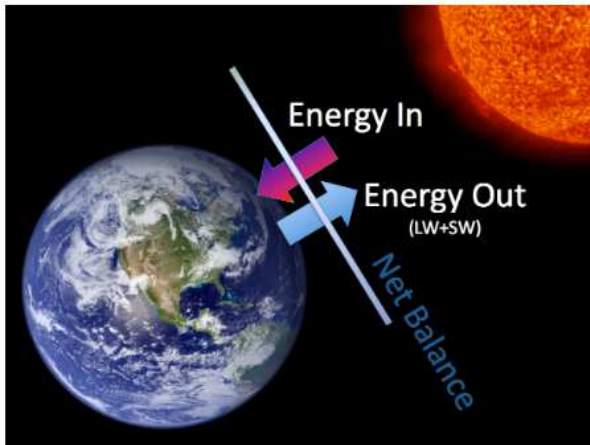
The One, The Half and The Double

$$\text{ASR} \\ = \text{OLR}$$

$$\text{SFC Net} \\ = \text{OLR}/2$$

$$\text{SFC Gross} \\ = 2\text{OLR}$$

CERES Earth's Radiation Budget



Universal necessity

Theoretical requirement

Simplest geometry

One for all, all for one

My Net Balancing I

Total Solar Irradiance = **1360.68** Wm⁻² = **51** units

1 unit = TSI / **51** = **26.68** Wm⁻²

Reflected all-sky, cross-section disk = **15** units

Absorbed all-sky, cross-section disk = **36** units

Reflected SW **clear-sky**, disk = **8** units

Absorbed SW **clear-sky**, disk = **43** units

Incoming Solar Radiation, sphere = **51** / 4 = **340.17**

Reflected SW all-sky, sphere = **15** / 4 units = **100.05**

Absorbed SW all-sky, sphere = **36** / 4 = **9** units = **240.12**

Emitted LW all-sky, sphere = **36** / 4 = **9** units = **240.12**

Reflected SW clear-sky, sphere = **8** / 4 = **2** units = **53.36**

Absorbed SW clear-sky, sphere = **43** / 4 units = **286.81**

Emitted LW clear-sky, sphere = **40** / 4 = **10** units = **266.80**

TOA net CRE = **-3** / 4 units = **-20.01**

My Net Balancing I-II-III & CRE

1 UNIT = 26.68 Wm⁻²	SYN	My	N × UNIT	N
Total Solar Irradiance	= 1360.9	− 0.22	= 1360.68	51
TOA SW up all	= 97.32	+ 2.73	= 100.05	15 / 4
TOA LW up all	= 238.63	+ 1.49	= 240.12	36 / 4
TOA SW up clr	= 51.38	+ 1.98	= 53.36	8 / 4
TOA LW up clr	= 268.15	− 1.35	= 266.80	40 / 4
<hr/>				
SFC SW+LW net clr	= 134.79	− 1.39	= 133.40	5
(TOA LW)/2 clr	= 134.08	− 0.68	= 133.40	5
<hr/>				
SFC SW net clr	= 214.25	− 0.81	= 213.44	8
SFC LW down clr	= 317.77	+ 2.39	= 320.16	12
SFC SW+LW abs clr	= 532.02	+ 1.58	= 533.60	20
2 × (TOA LW) clr	= 536.30	− 2.70	= 533.60	20
<hr/>				
LW CRE SFC, TOA	= 29.52	− 2.84	= 26.68	1
SW CRE SFC	= − 52.60	− 0.76	= − 53.36	2
SW CRE TOA	= − 45.93	− 0.76	= − 46.69	7 / 4

Bonus: The Greenhouse Effect

$$G = \text{SFC LW up} - \text{TOA LW}$$



SYN1deg

	SYN	My	EdMZ	N
SFC LW up all-sky	397.96	+ 2.24	400.20	15
TOA LW all-sky	238.63	+ 1.49	240.12	9
G all-sky	159.33	+ 0.75	160.08	6
SFC LW up clear-sky	397.23	+ 2.97	400.20	15
TOA LW clear-sky	268.15	– 1.35	266.80	10
G clear-sky	129.08	+ 4.32	133.40	5

Understanding how the Sun's energy drives Earth's climate system

