



# Climate Sensitivities in Short and Long Time Scales

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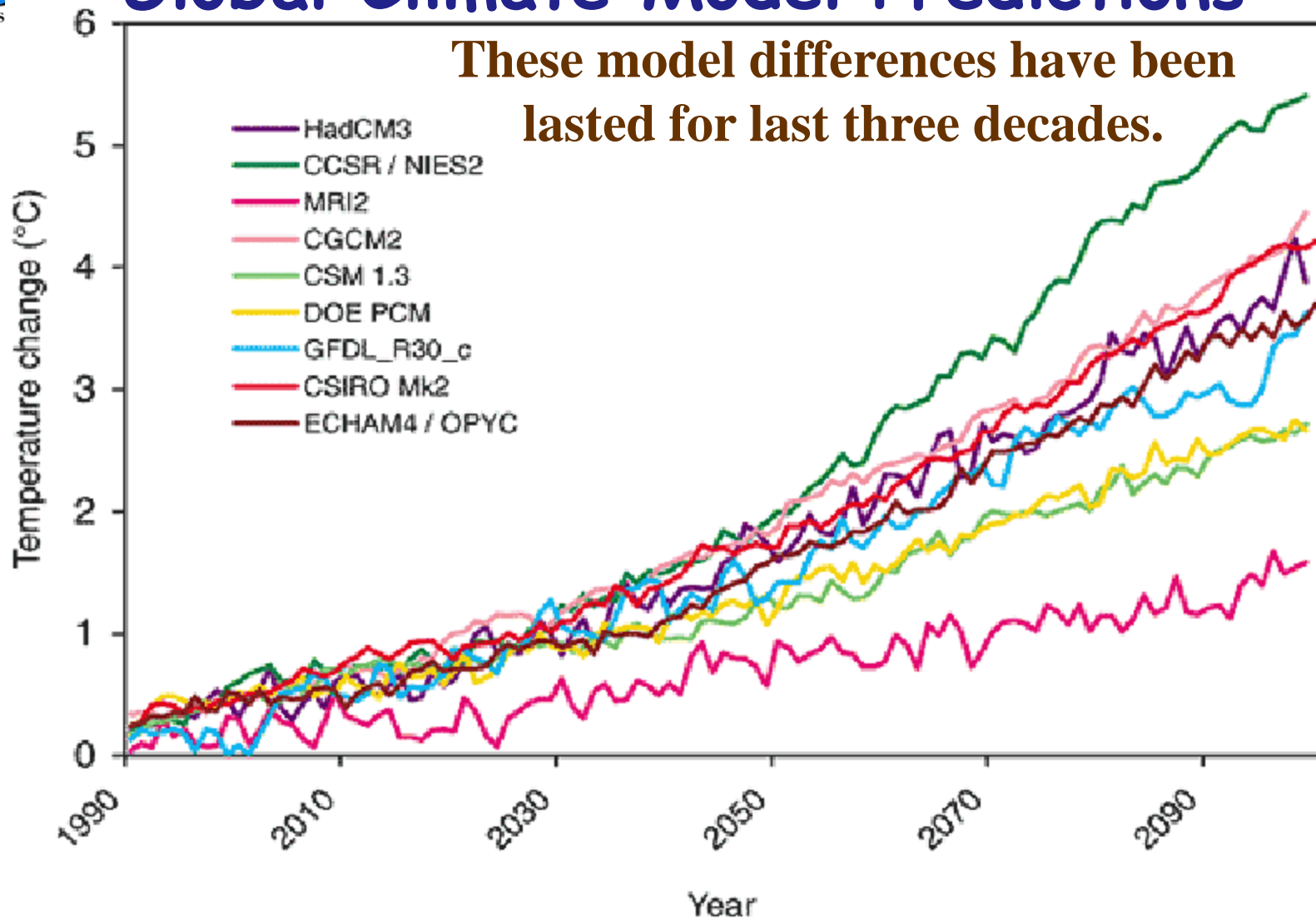
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# Large Uncertainties in Global Climate Model Predictions



**Model predictions of the time evolution of the globally averaged temperature change.**



# Introduction

- Large uncertainty in GCM climate predictions
  - ❖ clouds, precipitation, ocean, bio-/cryo-spheres

**strong nonlinear**
  
- Climate sensitivity: ??? time scale dependence
  - ❖ short-term variations of  $T_s$  and  $R_{net}$
  - ❖ long-term relationship of  $T_s$  and  $R_{net}$

**from weather to century time scales**
  
- Questions for observations:
  - ❖ Can we 'retrieve' (estimate) the climate sensitivity and reduce the uncertainty from measurements?
  - ❖ What is the 'retrieval model' for the feedbacks?  
Need tools and methods in the analysis



# Approaches



- **Climate sensitivity estimations**
  - complex enough for fundamental physics
  - simple enough to understand processes
  - observational-driven model studies
- **Energy balance & perturbation**
- **Key forcing: atmospheric radiation**
- **Short- and long-term relationships**



# Climate perturbation

$$C_p \frac{dT_s}{dt} = (1 - \alpha) S_0 - \varepsilon \sigma T_s^4$$

equilibrium state:  $\Delta\alpha = \Delta\varepsilon = 0$

$$\begin{aligned} C_p \frac{d\Delta T_s}{dt} &= -\frac{4\varepsilon\sigma T_s^4}{T_s} \Delta T_s \\ &= -\frac{4 \times 237}{288} \Delta T_s = -3.3 \Delta T_s \end{aligned}$$

define:  
 $\Delta T_s = T$

$$f_n = -3.3 \text{ W/K/m}^2$$

This is only for the equilibrium state of the climate.  
At short time scales, this feature cannot be found.



# History



$$C_p \frac{dT}{dt} = -f_n T$$

short-time scale  
feedbacks

$$C_p \frac{dT}{dt} = F - f_n T + f T = F - f_s T$$

long-term feedbacks  
potentially exist

For steady state with small perturbation:

$$T = T_0 e^{-t/\tau} \quad \tau = C_p / f_n$$

For forced small perturbation:

$$T = F(1 - e^{-t/\tau}) / f_s \quad \tau = C_p / f_s$$



# History (conti.)



Hansen et al. 1984 (Geophys. Monograph); Manabe 1990 (JPO)

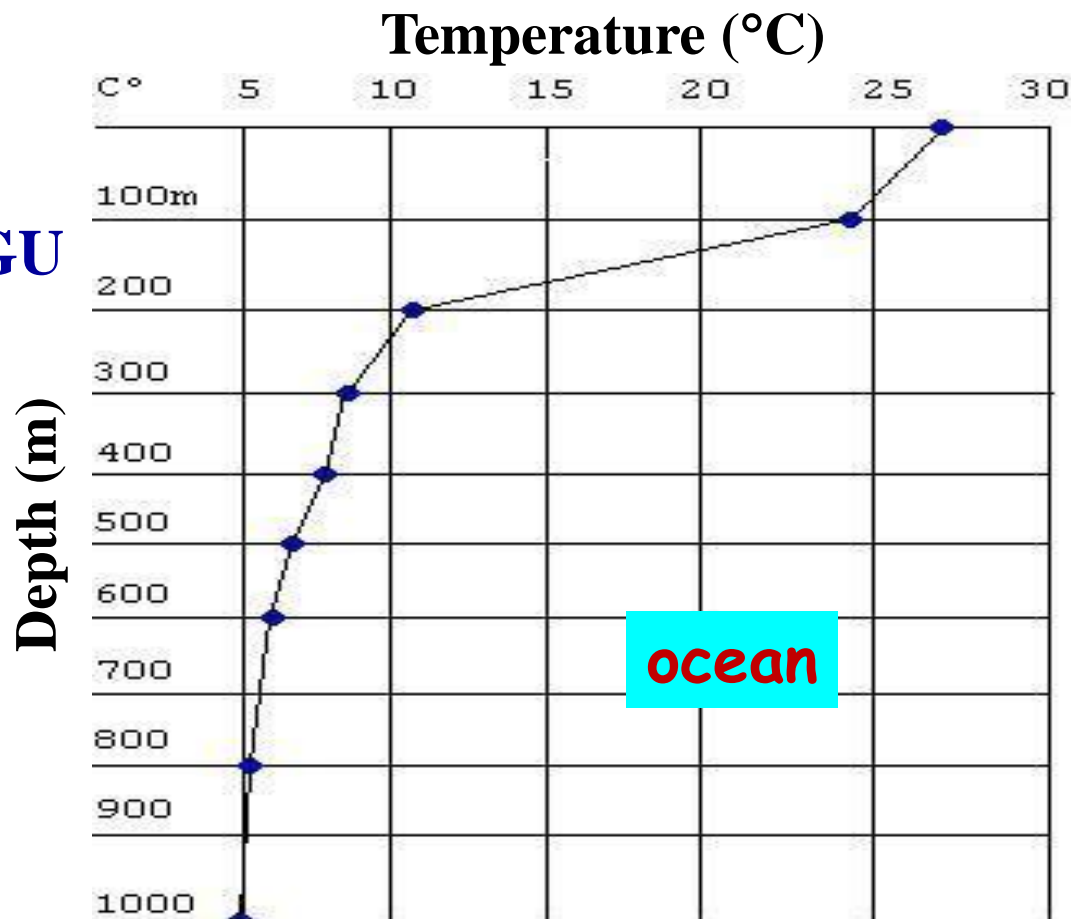
- Estimate total feedback coefficient  $f_{tot}$  (actually  $f_s$ )
- Huge heat capacity due to oceans, thus “wait and see”

Recent Progress:

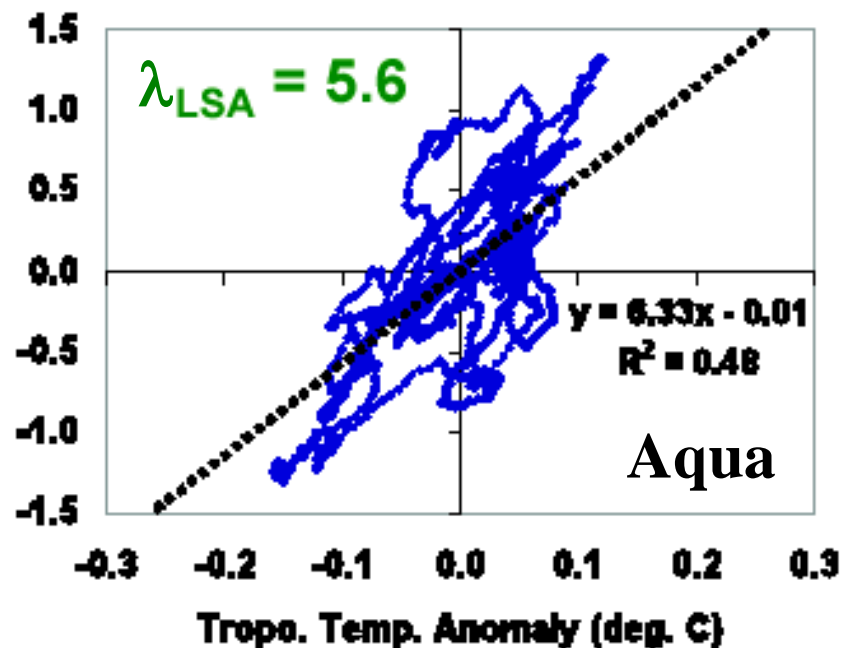
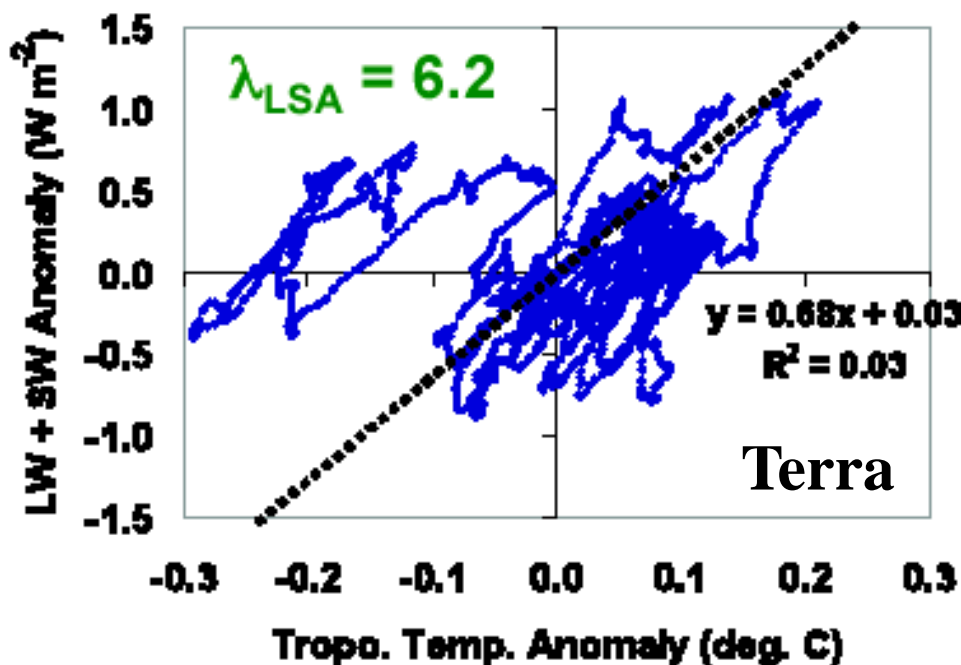
Schwartz 2007 JGR

Spencer and Braswell 2009 AGU

$$C_p \frac{dT}{dt} = F - f_{tot}T$$



# short-term relation



**Global Oceanic LW+SW Anomaly**  
**Total Feedback Parameter of  $\sim 6.0 \text{ W m}^{-2} \text{ K}^{-1}$**





# Observation Explanation



## Perturbation model: energy balance

$$C_p \frac{dT}{dt} = F + f_{tot}T + N + S$$

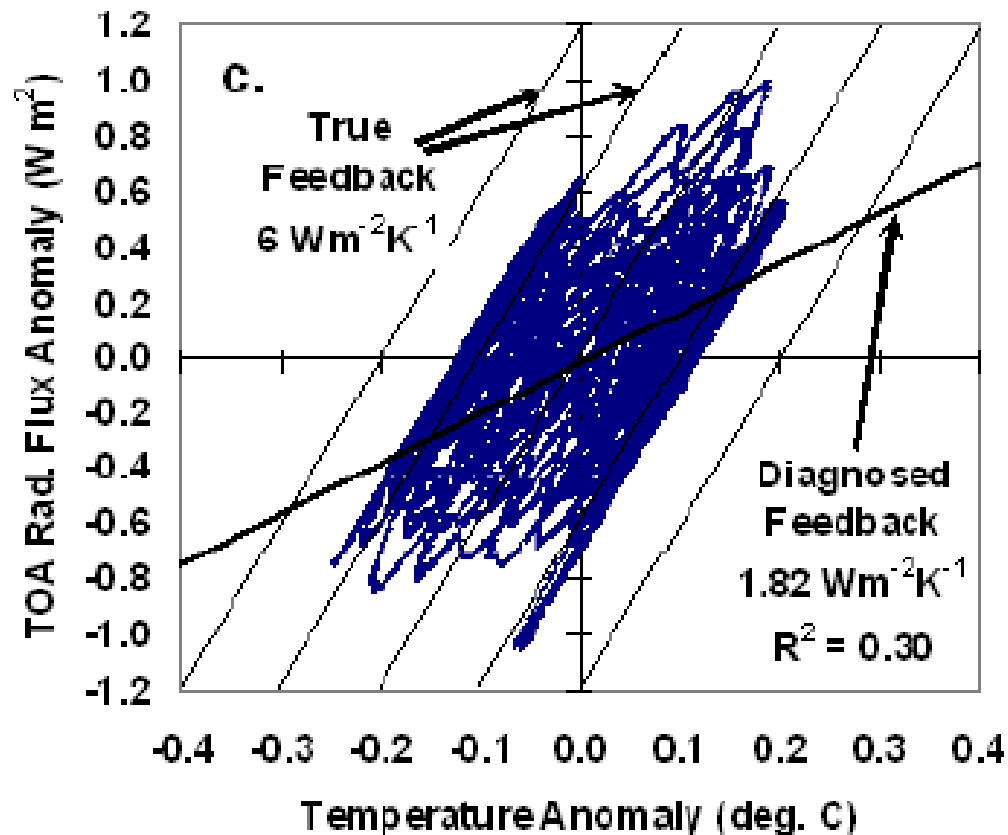
***N***: non-radiative heating (daily)

***S***: non-feedback natural radiative variability (5-yr cyc)

$$f_{tot}: f_n + f = -6 \text{ Wm}^{-2}\text{K}^{-1}$$

***F***:  $F = 0$  or removed

***C<sub>p</sub>***: 50 m water





# Modeling Considerations



Perturbation theory: energy balance model

$$C_p \frac{dT}{dt} = F + f_s T + N + S + \frac{f_m}{t_0} \int_{t-t_0}^t T dt'$$

**$N$** : non-radiative heating (daily)  $\leftrightarrow$  avg  $N = 0$

**$S$** : non-feedback natural radiation (5-yr cycle)  $\leftrightarrow$  avg  $S = 0$

**$f_s$** :  $f_s = f_n + f = -6 \text{ Wm}^{-2}\text{K}^{-1}$  ;  $f = -2.7 \text{ Wm}^{-2}\text{K}^{-1}$

**$f_{tot}$** :  $f_{tot} = f_s + f_m$

**$F$** :  $F = 0$  or removed

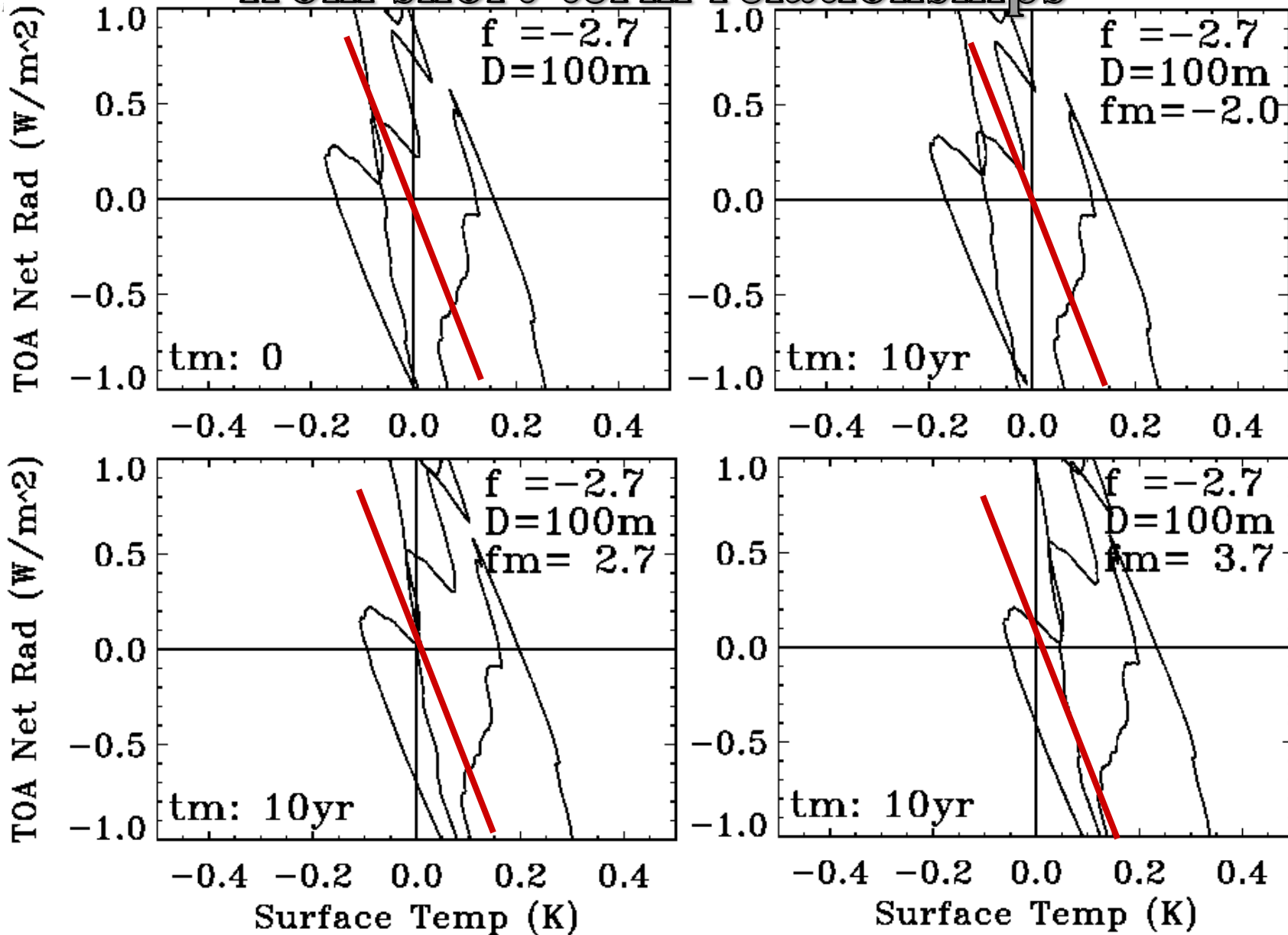
**$t_0$** : memory length  $\leftrightarrow$  minimal (1 year); other lengths also tested

**$C_p$** : 100 m mixed layer ocean (slab ocean)

last 10-year results of 100-year run

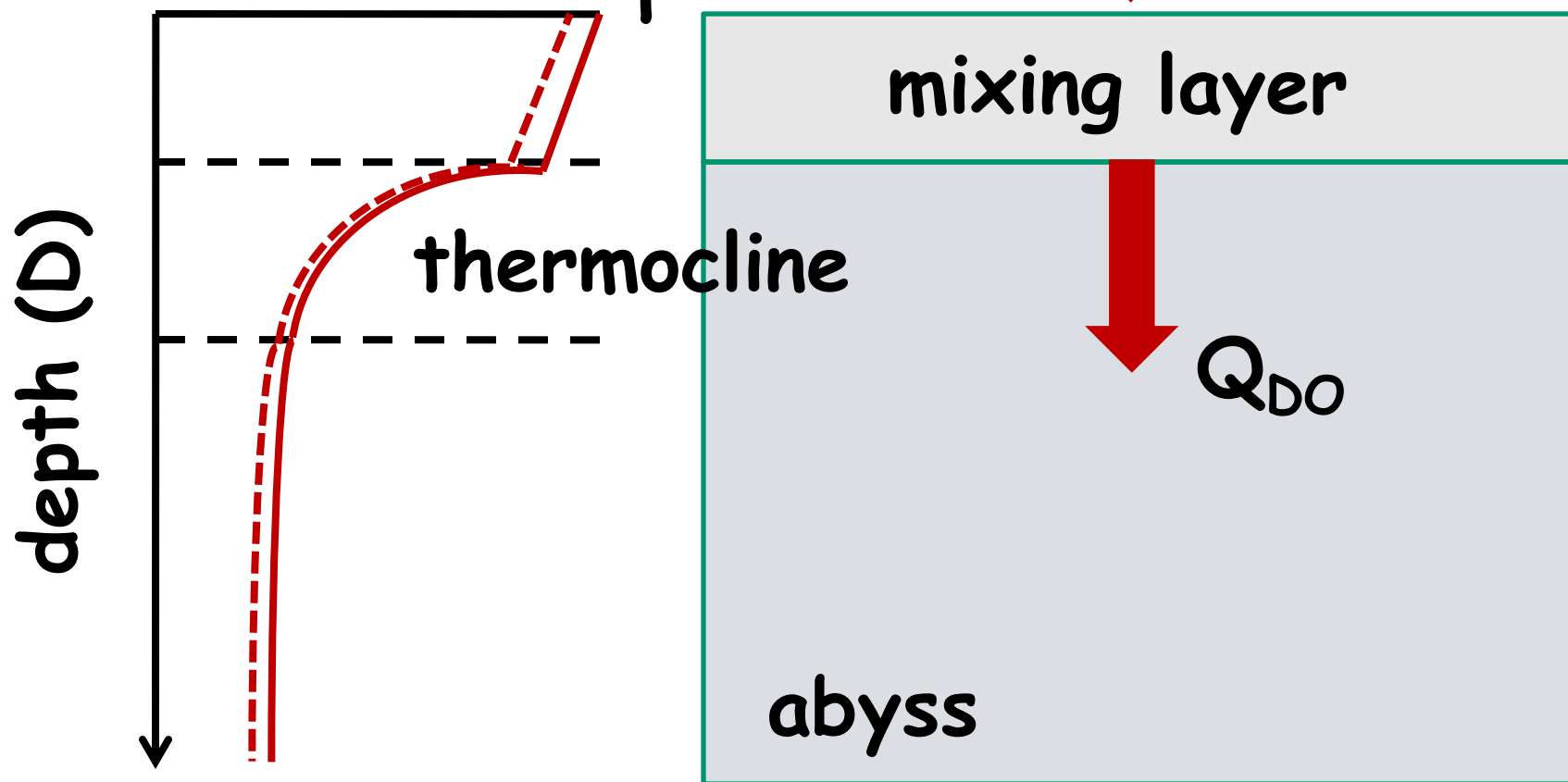


# May not determine total feedback from short-term relationships



# Issues

only  $dT_{ML} \propto dT_s$



1. Solving boundary conditions instead of initial conditions
2. D limits or deep ocean heat transport -- much longer time scale
3. Climate system memory – generalized feedback (e.g., ice sheets)



# Perturbed Climate System



**More general conditions are considered in this study**

1. Boundary condition approach
2. System has memory with memory length  $t_0$  (could be multi-cycles)
3. There is a deep ocean heat transport

$$C_p \frac{dT}{dt} = F - f_s T + \frac{f_m}{t_0} \int_{t-t_0}^t T dt' - O$$

$$O = \mu \left( F - f_s T + \frac{f_m}{t_0} \int_{t-t_0}^t T dt' \right)$$

$$f_{tot} = f_s - f_m$$



# Analytic System

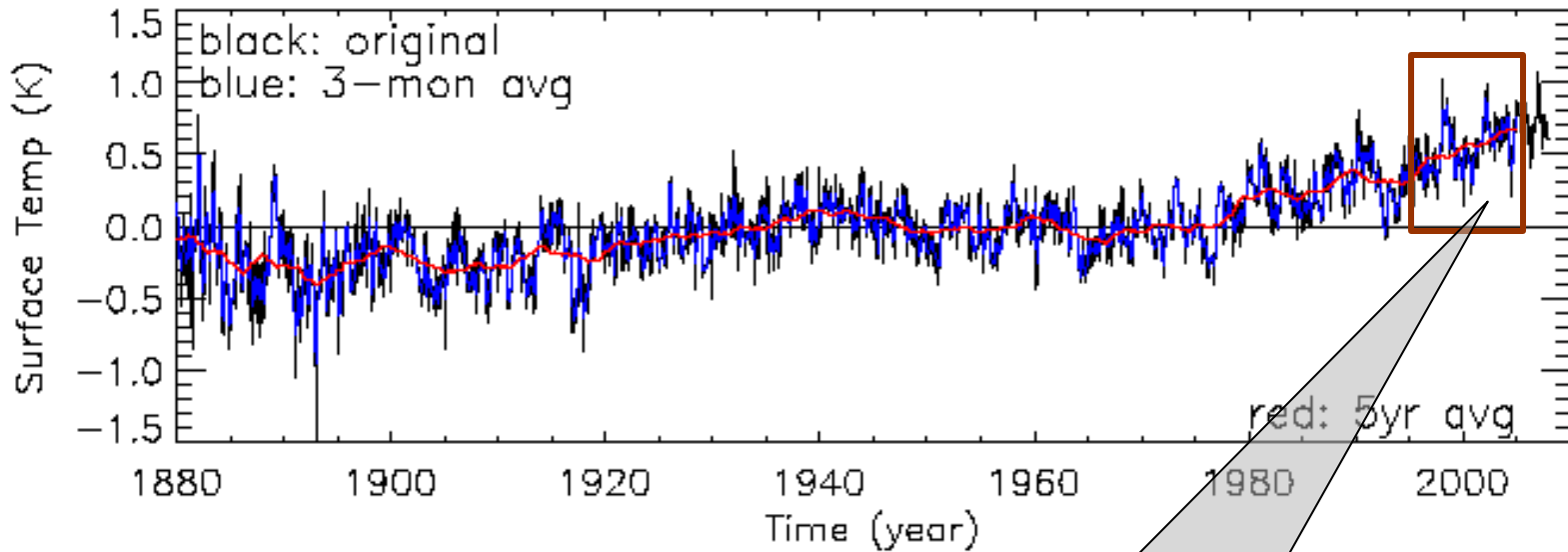
$$Cp' \frac{dT}{dt} = F - f_s T + \frac{f_m}{t_0} \int_{t-t_0}^t T dt'$$

1. Avoid the difficulty on deep ocean heat storage
2. Solution is not specifically dependent on mixing layer depth, only the ratio of  $D/\eta$
3. Forcing:  $F = \gamma t$  ( $F(t=0) = 0$ ;  $F(t=120\text{yr}) = 1.8\text{W/m}^2$ )
4.  $f_s = f_n + f = 6 \text{ W/m}^2/\text{K}$ ; Thus,  $f_{\text{TOT}} = f_s - f_m$

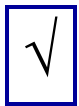
## Reduced forms:

- 1)  $t_0$  approaches 0; & 2) Ocean heat transport = 0  
→ 1<sup>st</sup> order ODE of Hansen, Manabe, Schwartz etc

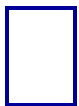
# Current solution



**$T = 0.65 \text{ K}; Q_{\text{net}} = 0.85 \text{ W/m}^2$**   
**constraints for the means of last 10 yrs**

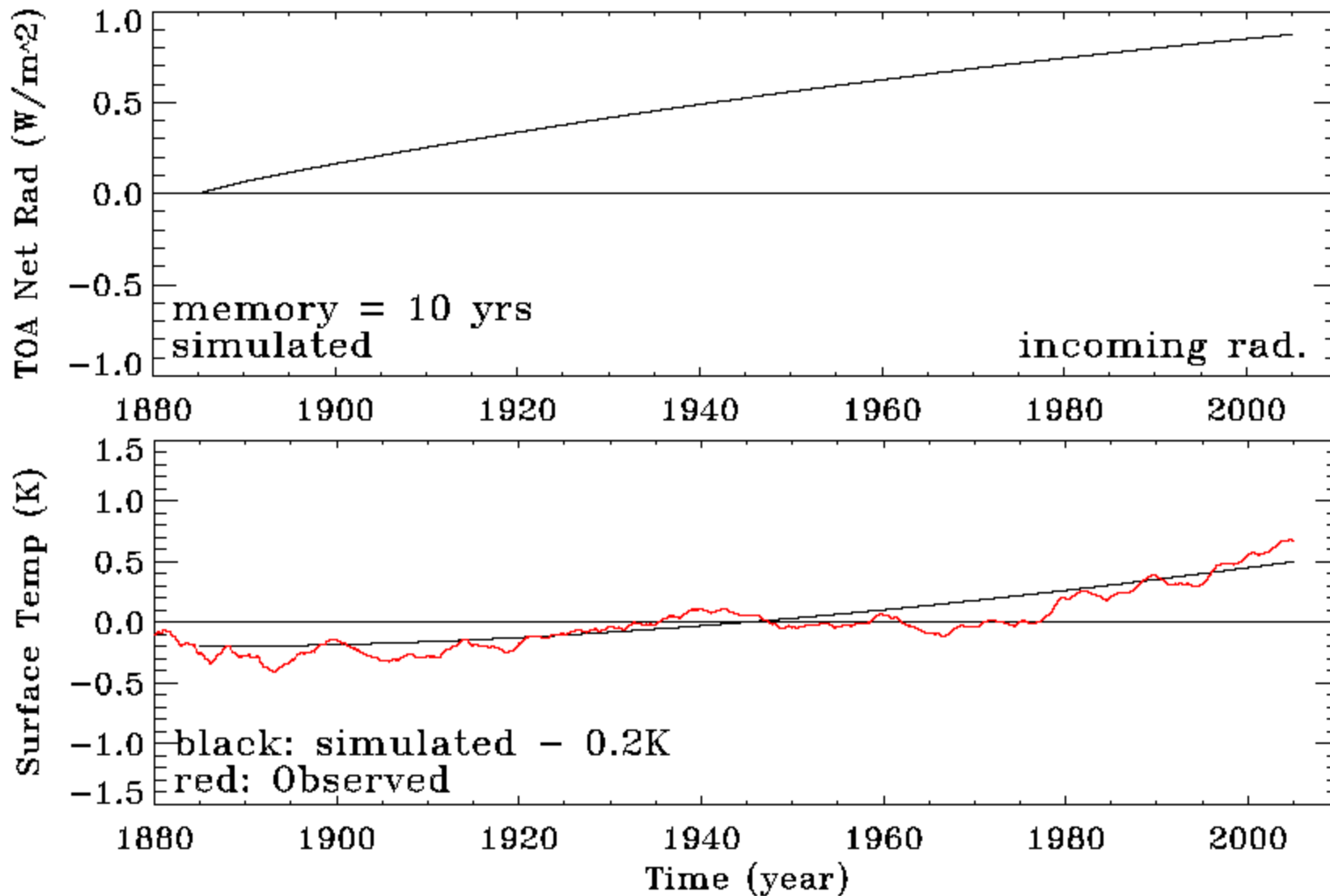


**Numerical solution of  $f_m$  and  $\eta$  (or  $\mu$ ): easier**

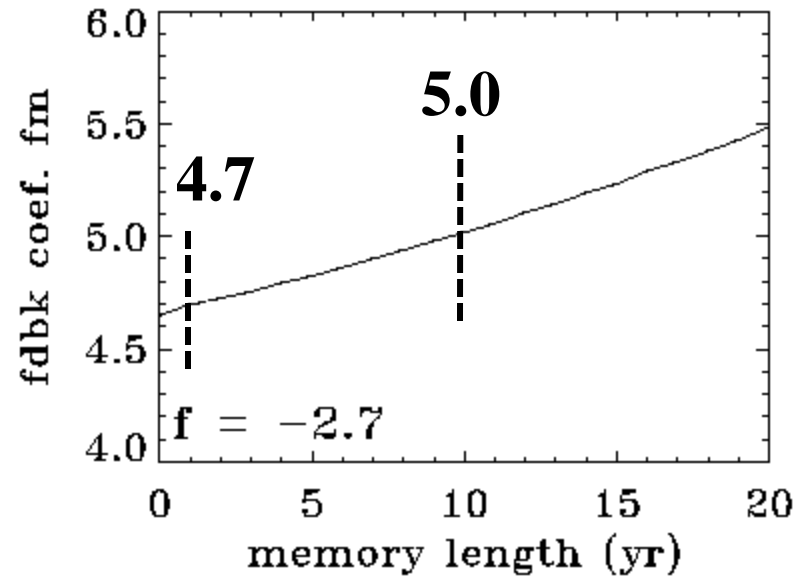
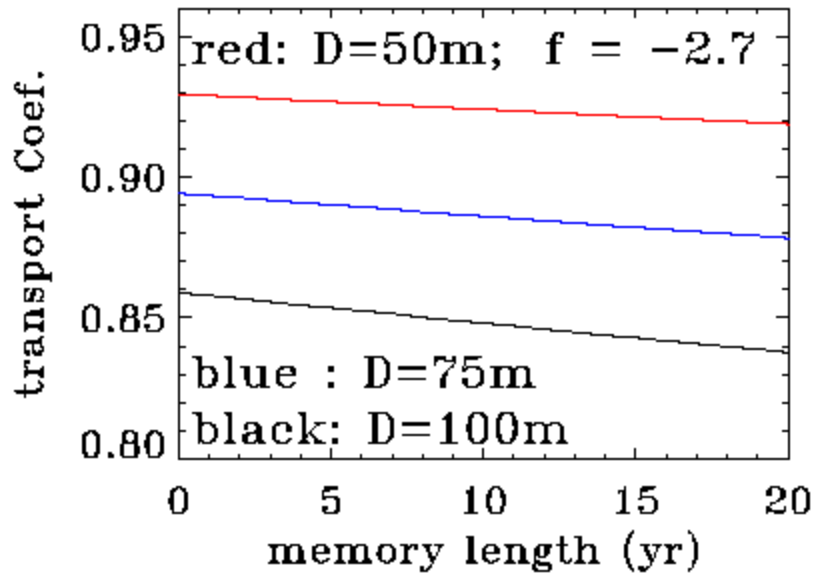


**Analytic solution is also available  
(solving transcendental equations; more math)**

# Results

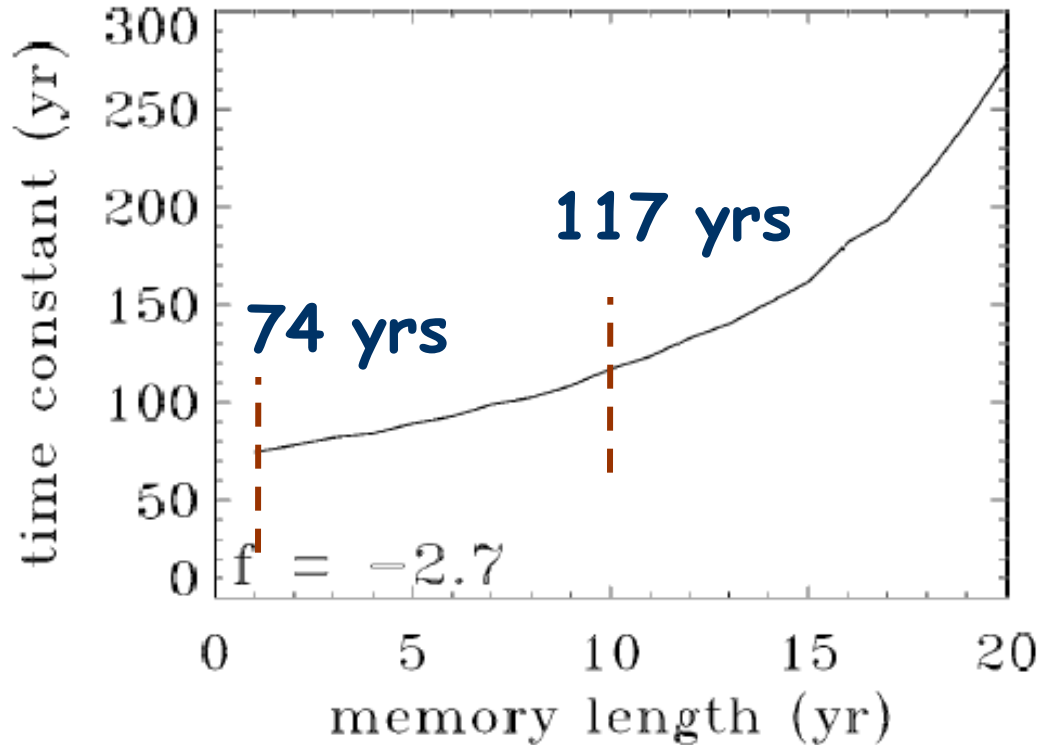






1. Most heat is transported to deep ocean ( $\mu > 80\%$ ).
2. Total feedback coefficients:  $f_{\text{tot}} = 6 - 4.7 = 1.3$  ( $t_0 = 1$  yr);  
 $f_{\text{tot}} = 6 - 5.0 = 1.0$  ( $t_0 = 10\text{yr}$ )
3. Positive feedback obtained:  
 feedback coefficients:  $f_c = 4.7 - 2.7 = 2.0$   
 $f_c = 5.0 - 2.7 = 2.3$

# Results



**gradually increases in the constant for memory length < 15 yrs**

**With deep ocean heat transport, the time constant of climate system is much longer, maybe about 70 ~ 120 yrs.**



# Linearized Approximation



$$C_p \frac{dT}{dt} = F - f_s T + \frac{f_m}{t_0} \int_{t-t_0}^t T dt' - 0$$

$$C_p \frac{dT}{dt} = F - f_{tot} T$$

$$f_{tot} = (F - C_p \frac{dT}{dt}) / T$$

$$f_{tot} = (F - Q_{net}) / T$$

$$f_{tot} = (1.8 - 0.85) / 0.65 = 1.46$$

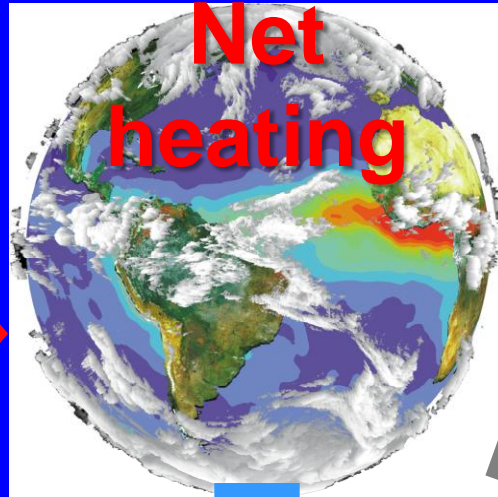
$$u = 0.91 \quad \text{assuming 100m mixed layer}$$

**Reduced forms: resulted in slightly weaker positive feedback than those of the perturbation model calculations**

# Data needed: surface temperature & TOA net radiation

long-term feedback

slow response from system memories

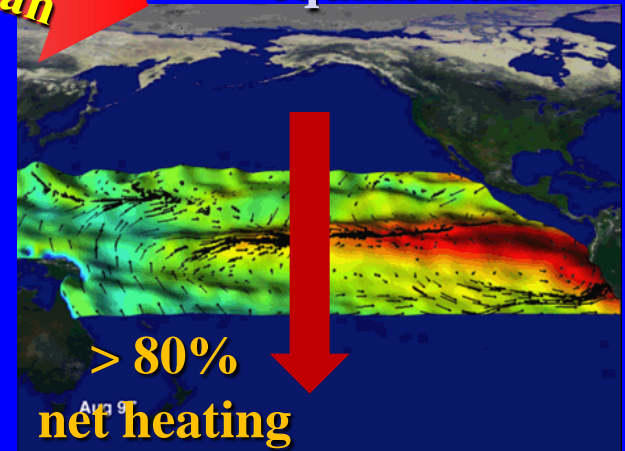


Forcing

Heat transport to deep ocean

long-time to reach equilibrium

short-term feedback





# Summary



- There are large uncertainties in the climate predictions from present global climate models.
- Energy balance model is used for explanation of observed TOA net radiation (or ocean heat storage) and surface temperature.
- Major physical processes of the climate system, such as deep ocean heat transport and system memory, are considered.
- This study targets at boundary instead of classic initial condition problems (actual climate issue).



# Summary



- Short-time scale climate system adjustment (or relaxation) alone cannot mimic climate change: different scales, different physics
- For the best estimate of  $Q_{net}$ , estimated feedback factor is 1.0 ~ 1.3, or,  $2 \times CO_2$  (or  $3.7 W/m^2$ ) warming about 2.85 ~ 3.7 K. Results is sensitive to  $Q_{net}$ , not  $T_s$  and  $f_s$ .  
(only provide a tool for public)
- There is a strong desire for long-term radiation missions with calibrations of high accuracy and precision, such as CLARREO & CERES.



# Thank You!

- ❖ Lin et al. 2010, ACP
- ❖ Lin et al. 2010, JQSRT