



Climate perturbation, energy balance and feedback

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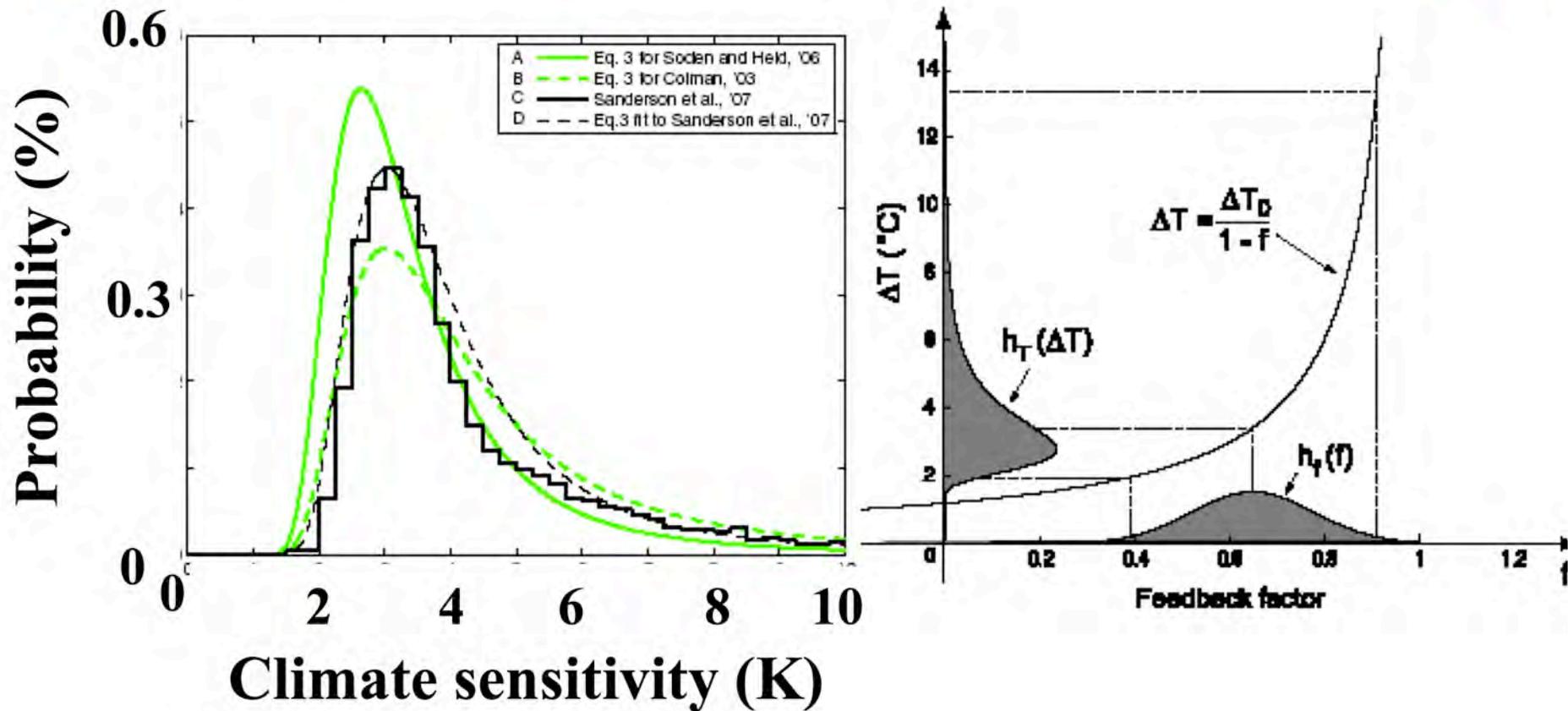
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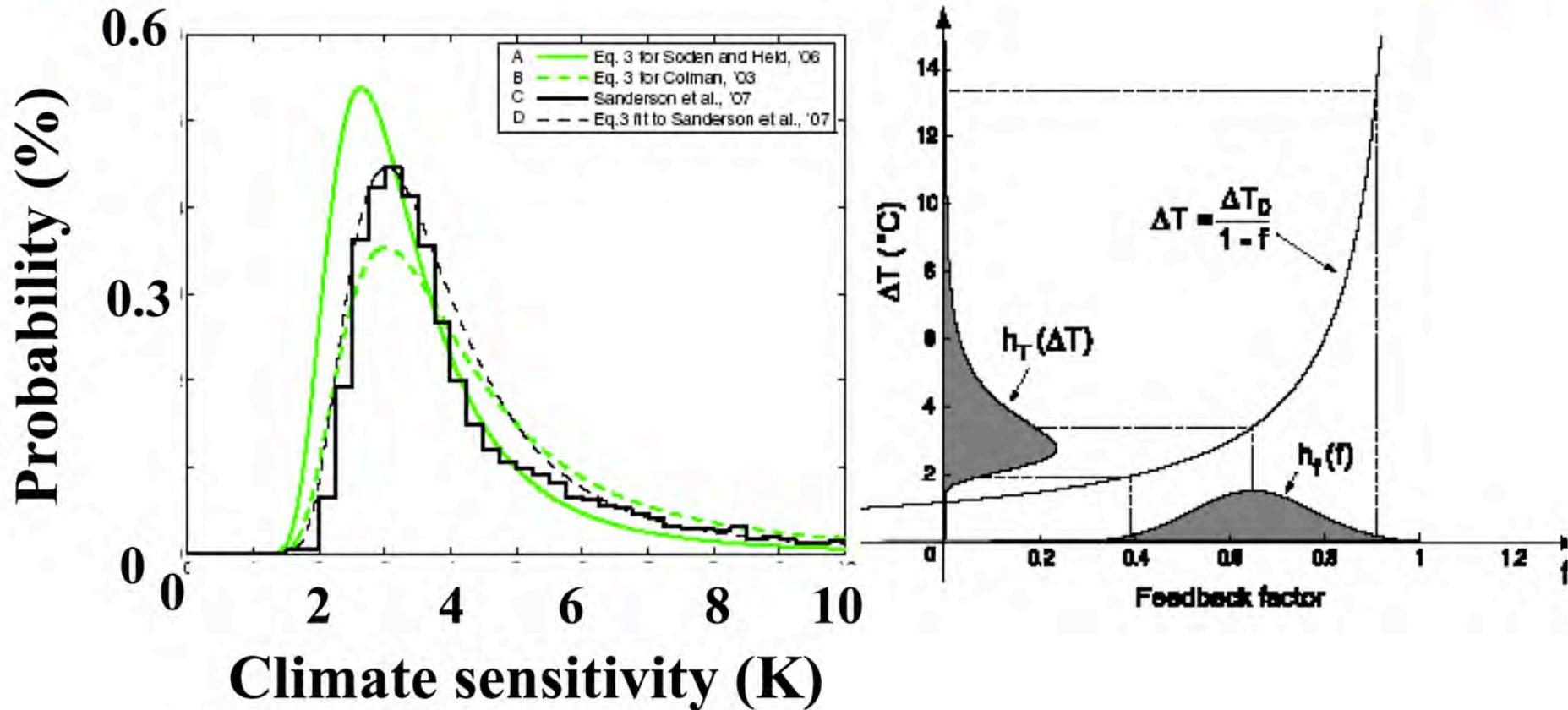
Motivation



Roe & Baker (2007) Science



Motivation



**Observations: ‘retrieval’ (estimate) or providing a key tool to reduce the uncertainty in climate sensitivity.
What is the ‘retrieval model’ for the feedback?**



Climate perturbation



$$C_p \frac{dT_s}{dt} = (1 - \alpha) S_0 - \epsilon \sigma T_s^4$$



Climate perturbation



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equilibrium state: $\Delta\alpha = 0$



Climate perturbation



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$$\begin{aligned} C_p \frac{d\Delta T_s}{dt} &= -\frac{4\epsilon\sigma T_s^4}{T_s} \Delta T_s \\ &= -\frac{4 \times 237}{288} \Delta T_s = -3.3 \Delta T_s \end{aligned}$$



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At short time scales, this feature cannot be found.



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define:
 $\Delta T_s = T$

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At short time scales, this feature cannot be found.



History



$$C_p \frac{dT}{dt} = -fnT$$

For steady state with small perturbation:

$$T = T_0 e^{-t/\tau} \quad \tau = C_p / fn$$



History



$$C_p \frac{dT}{dt} = -f_n T$$

short-time scale
feedback

$$C_p \frac{dT}{dt} = F - f_n T + f T = F - f_s T$$

For steady state with small perturbation:

$$T = T_0 e^{-t/\tau} \quad \tau = C_p / f_n$$

For forced small perturbation:

$$T = F(1 - e^{-t/\tau}) / f_s \quad \tau = C_p / f_s$$

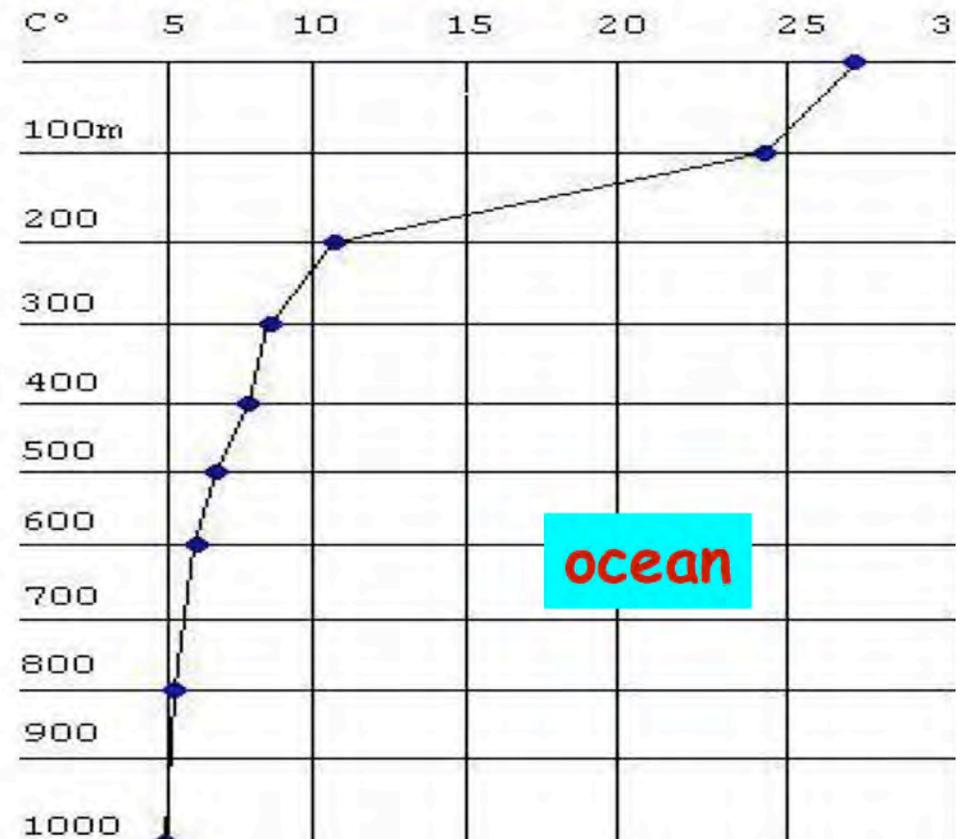


History (conti.)

Hansen et al. 1984 (Geophys. Monograph); Manabe ????

- Estimate feedback coefficient f_s
- Huge heat capacity due to oceans, thus “wait and see”
- Coupled GCM

$$C_p \frac{dT}{dt} = F - f_s T$$





Recent results



Schwartz (2007, JGR):

Equivalent heat capacity: ocean heat measurements

$$C_p = \frac{dH}{dT} \Rightarrow D = 100 \sim 110m$$



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Resulted in $f_s = 3.3 \text{ W/m}^2/\text{K}$, i.e., neutral feedback

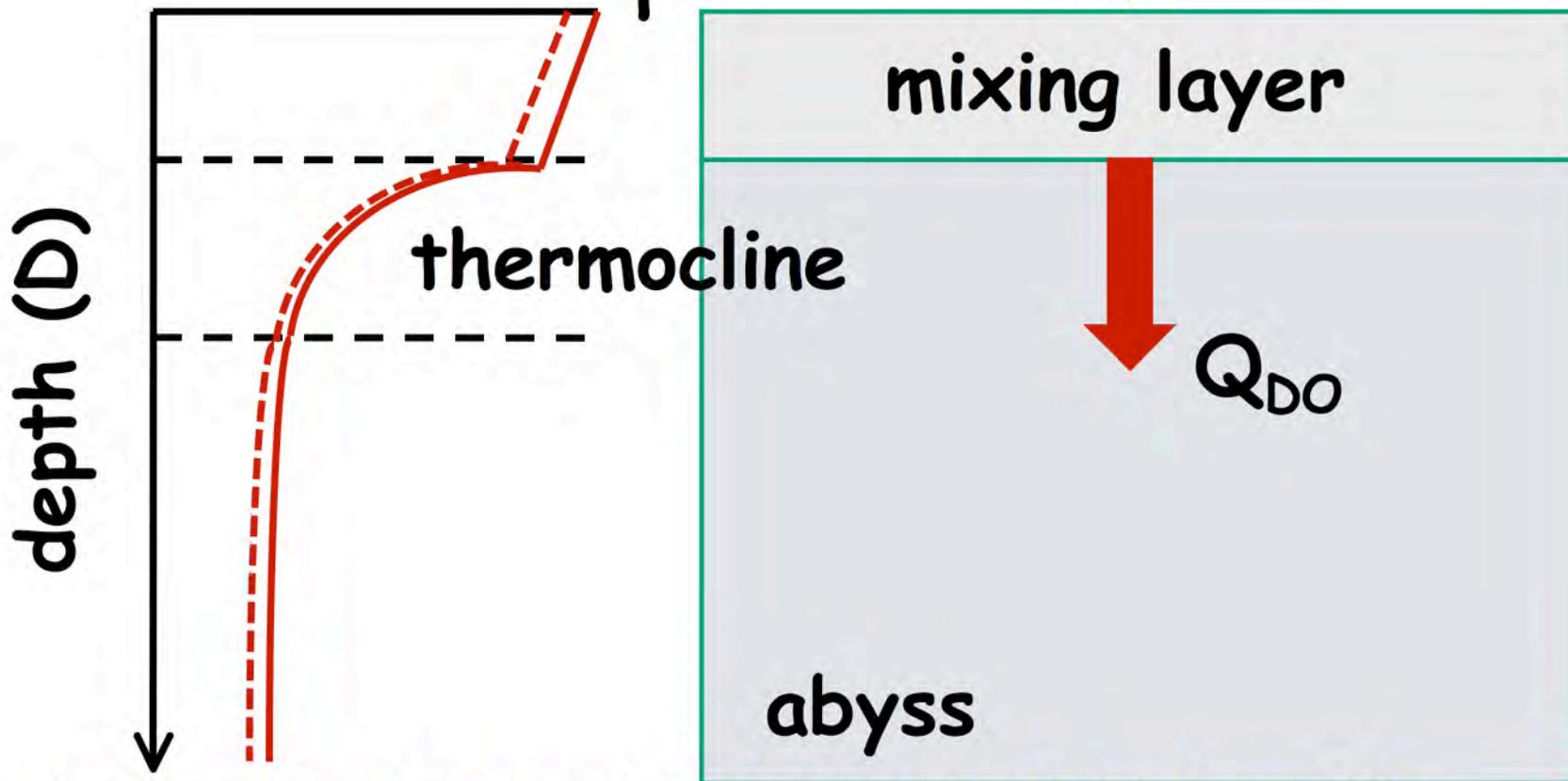
Or, $2 \times \text{CO}_2$ forcing $\rightarrow 1.1\text{K}$



Issues



only $dT_{ML} \propto dT_S$



1. Solving boundary conditions instead of initial conditions
2. D limits or deep ocean heat transport -- much longer time scale
3. Climate system memory – generalized feedback (e.g., ice sheets)



Current Approach



More general conditions are considered in this study

1. Boundary condition approach
2. System has memory with memory length t_0 (could be multi-cycles)
3. There is a deep ocean heat transport



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$$C_p \frac{dT}{dt} = F - f_s T + \frac{f_m}{t_0} \int_{t-t_0}^t T dt' - O$$

$$O = \mu \left(F - f_s T + \frac{f_m}{t_0} \int_{t-t_0}^t T dt' \right)$$

$$f_{tot} = f_s - f_m$$



Current Approach



$$\frac{C_p}{(1 - \mu)} \frac{dT}{dt} = F - f_s T + \frac{f_m}{t_0} \int_{t-t_0}^t T dt'$$

$$C_p' \frac{dT}{dt} = F - f_s T + \frac{f_m}{t_0} \int_{t-t_0}^t T dt'$$

$$C_p' = \rho S_w V / \eta = \rho S_w A D / \eta$$

$$\eta = 1 - \mu; T(t \leq 0) = 0$$



Current Approach



$$Cp' \frac{dT}{dt} = F - fsT + \frac{fm}{t_0} \int_{t-t_0}^t T dt'$$



Current Approach



$$C_p' \frac{dT}{dt} = F - f_s T + \frac{f_m}{t_0} \int_{t-t_0}^t T dt'$$

1. Avoid the difficulty on deep ocean heat storage
2. Solution is not specifically dependent on mixing layer depth, only the ratio of D/η
3. Forcing: $F = \gamma t$ ($F(t=0) = 0$; $F(t=120\text{yr}) = 1.8\text{W/m}^2$)
4. $f_s = f_n + f = 6 \text{ W/m}^2/\text{K}$; Thus, $f_{\text{TOT}} = f_s - f_m$



Current Approach



$$C_p' \frac{dT}{dt} = F - f_s T + \frac{f_m}{t_0} \int_{t-t_0}^t T dt'$$

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Reduced forms:

- 1) $t_0 = 0 \rightarrow 1^{\text{st}}$ order ODE
- 2) Ocean heat transport = 0 $\rightarrow 1^{\text{st}}$ order ODE of Hansen, Schwartz etc

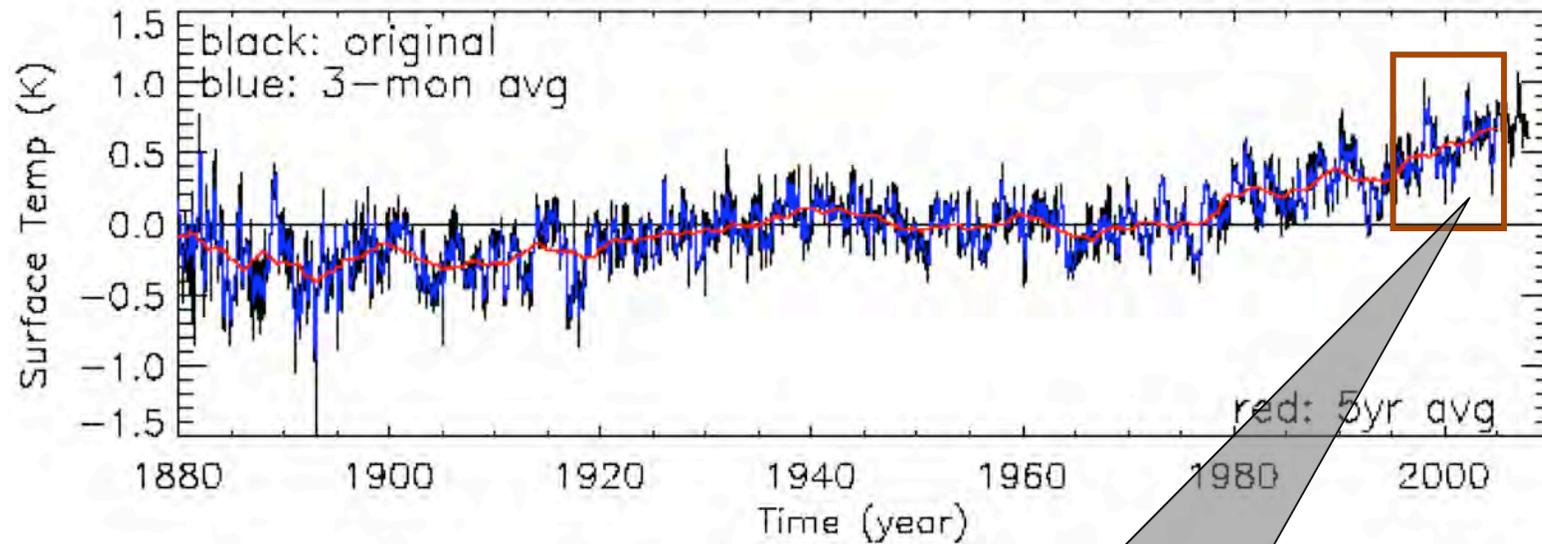


Current Approach





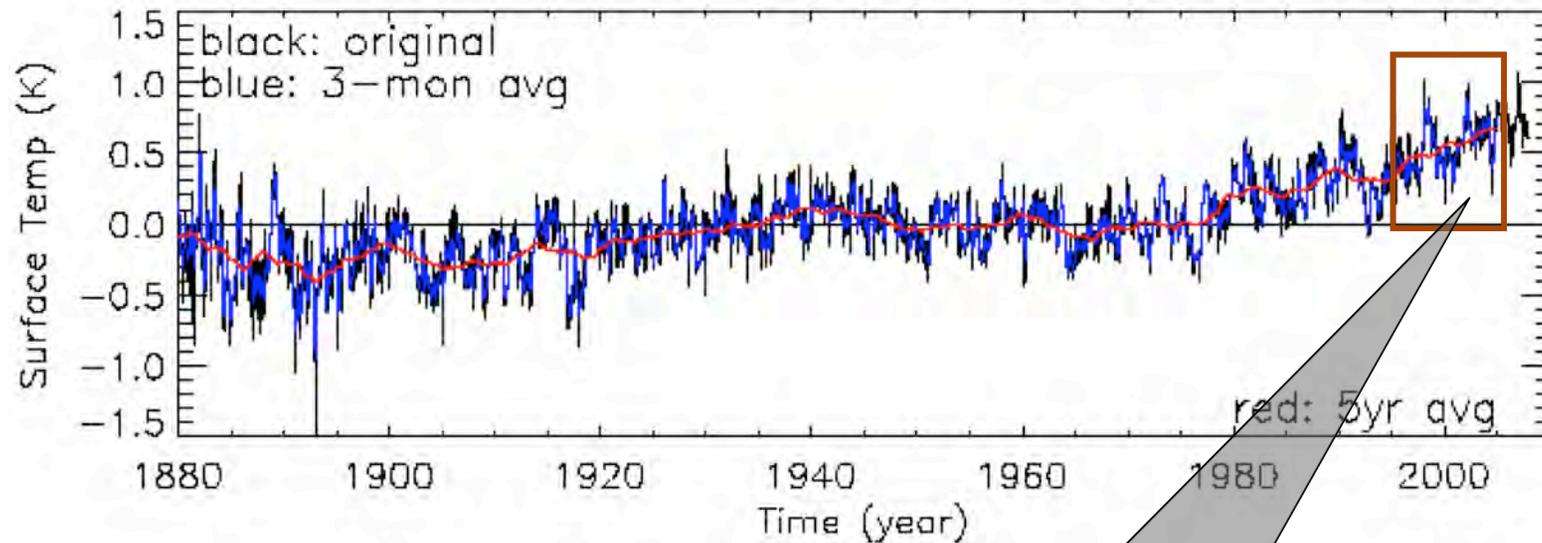
Current Approach



$T = 0.65 \text{ K}; Q_{\text{net}} = 0.85 \text{ W/m}^2$
constraints for the means of last 10 yrs



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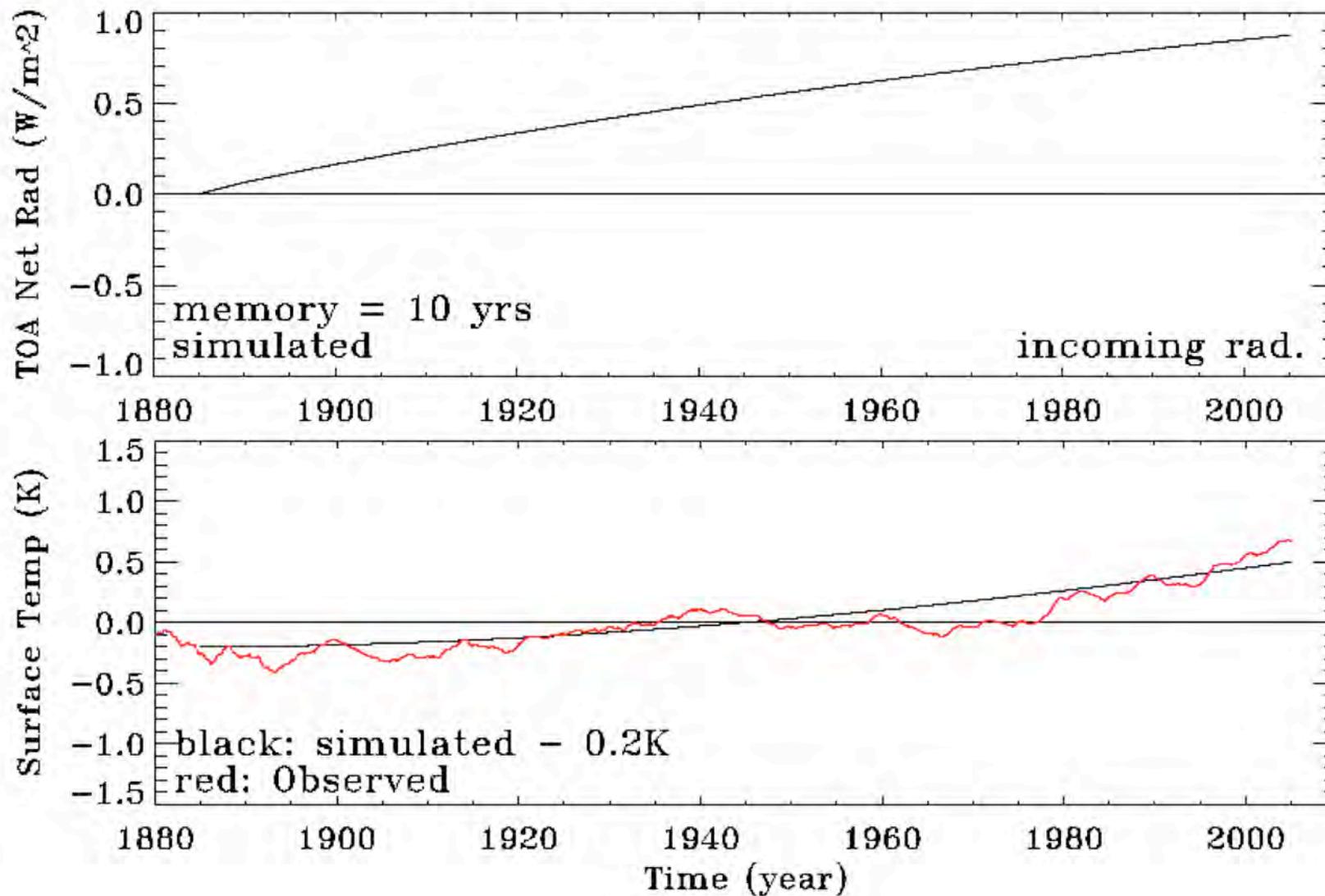
Numerical solution of f_m and η (or μ): easier



**Analytic solution is also available (not discussed here)
(solving transcendental equations; more math)**

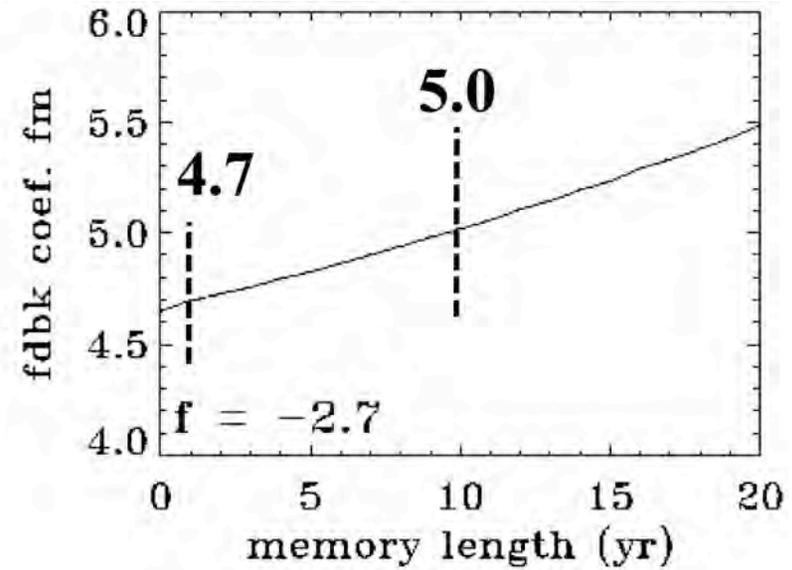
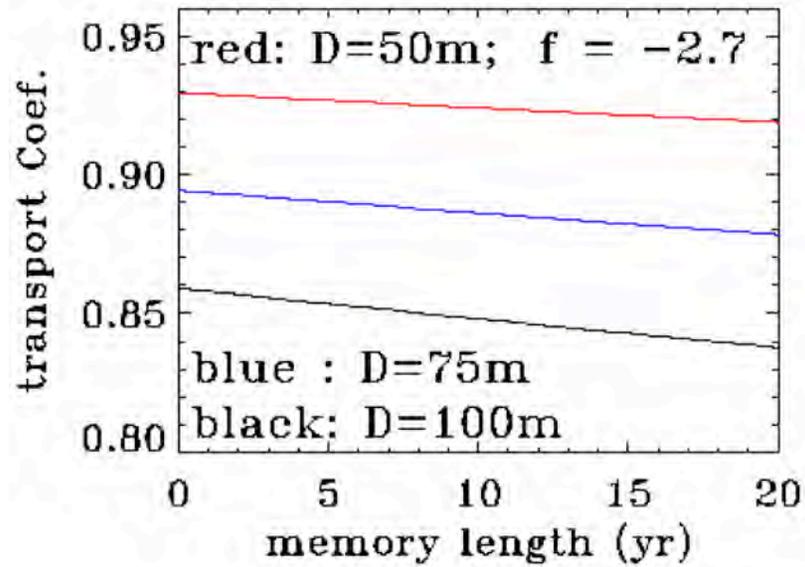


Results



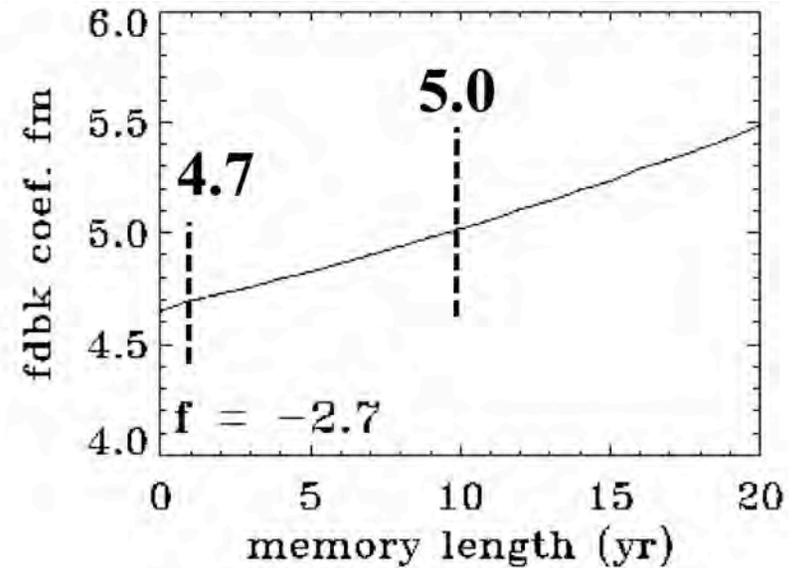
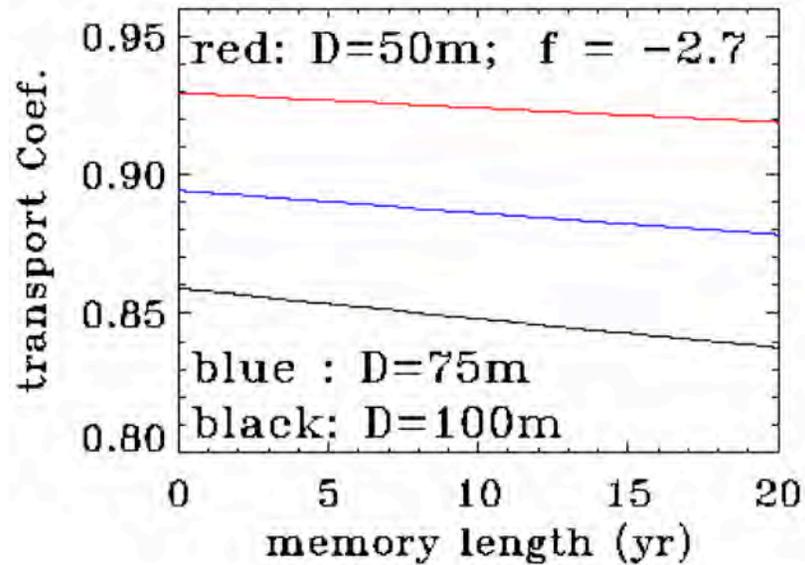


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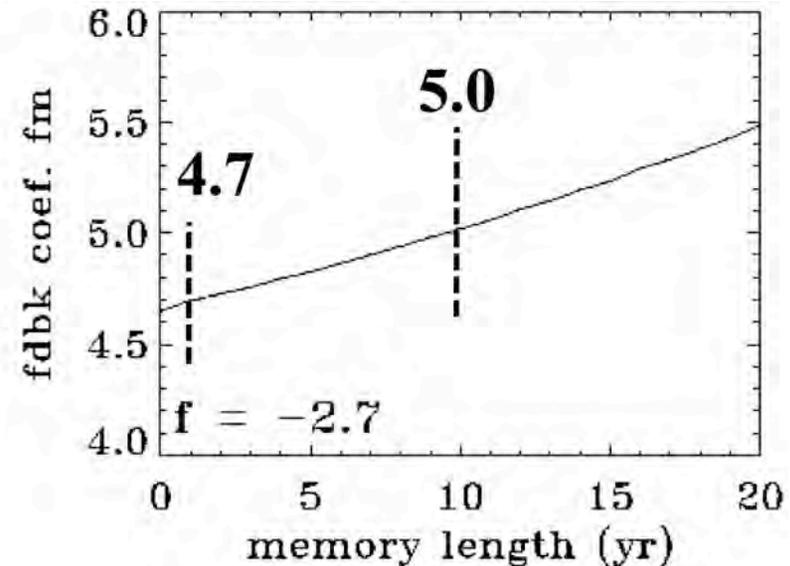
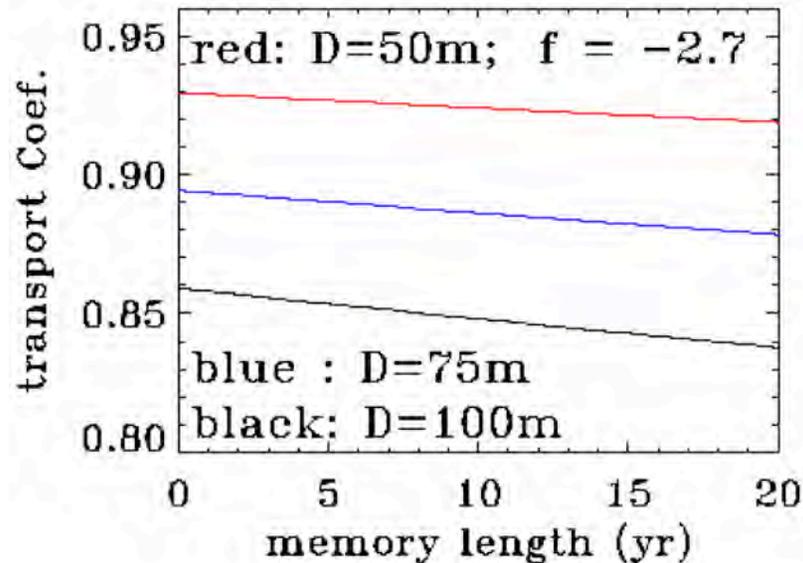
Results



1. Most heat is transported to deep ocean ($\mu > 80\%$).



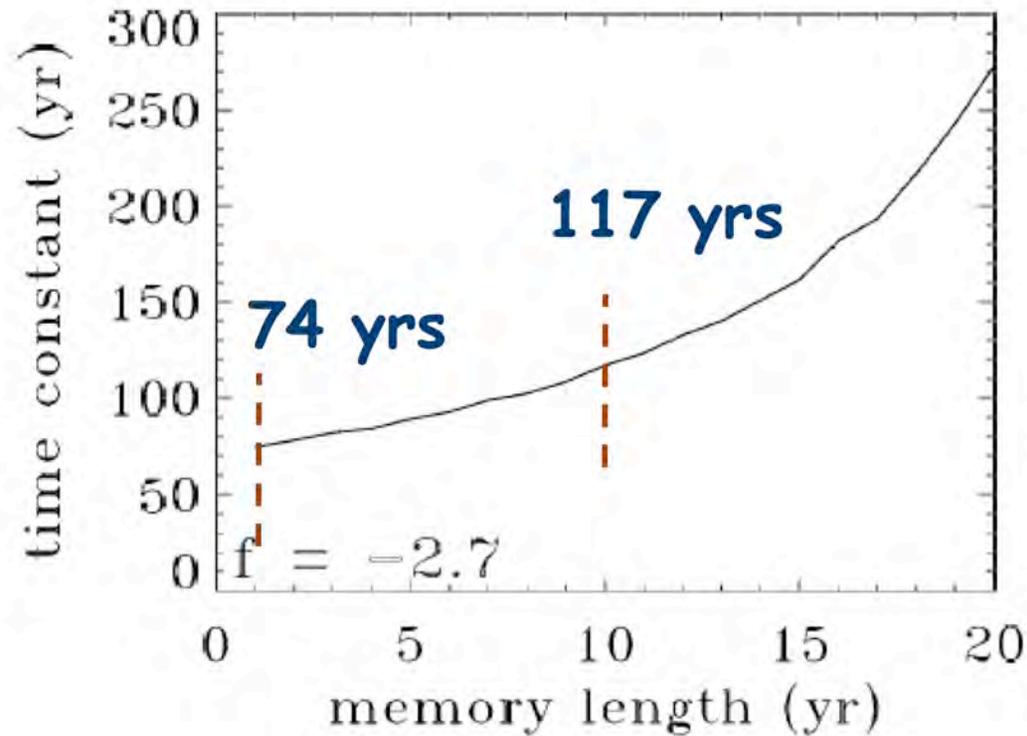
Results



1. Most heat is transported to deep ocean ($\mu > 80\%$).
2. Total feedback coefficients: $f_{\text{tot}} = 6 - 4.7 = 1.3$ ($t_0 = 1$ yr);
 $f_{\text{tot}} = 6 - 5.0 = 1.0$ ($t_0 = 10\text{yr}$)
3. Positive feedback obtained:
feedback coefficients: $fc = 4.7 - 2.7 = 2.0$
 $fc = 5.0 - 2.7 = 2.3$



Results

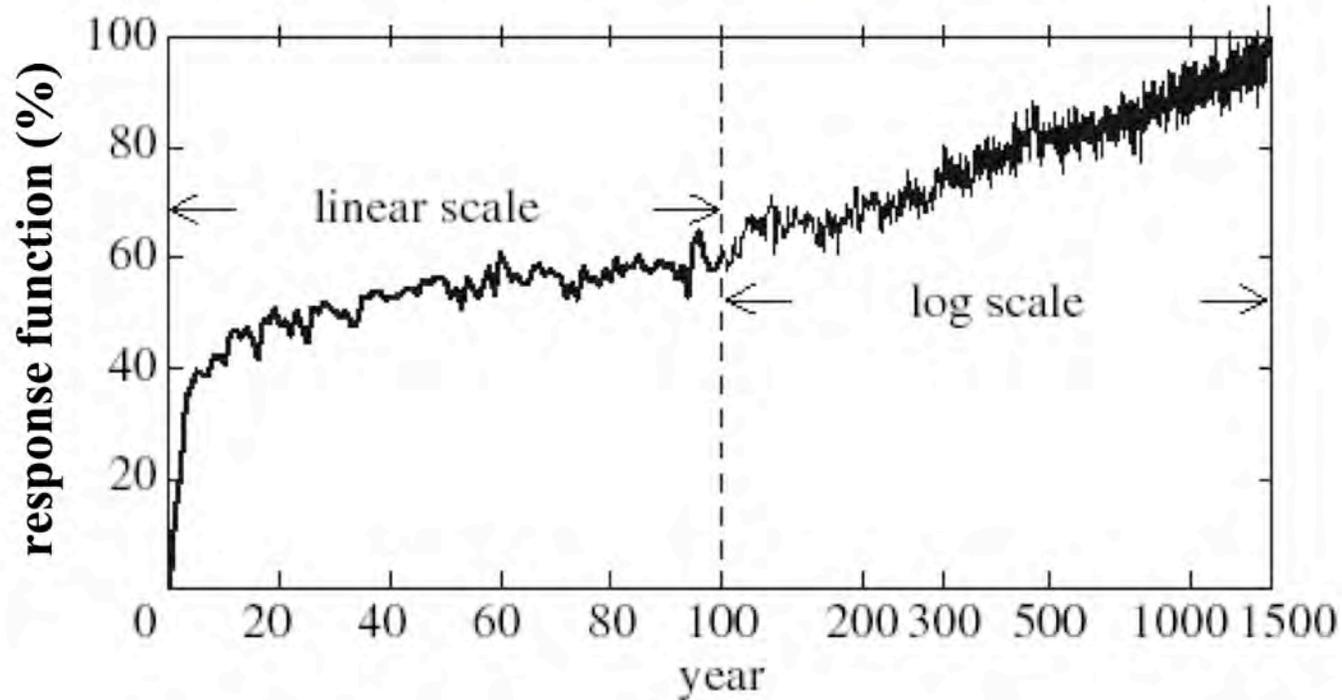


gradually increases in the constant for memory length < 15 yrs

With deep ocean heat transport, the time constant of climate system is much longer, maybe about 70 ~ 120 yrs.



GISS AOGCM



Time const.: 60% in 100 yrs
109 yrs

90% after 1000 yrs
434 yrs

Hansen et al. (2007, PTRS)



Results: asymptote





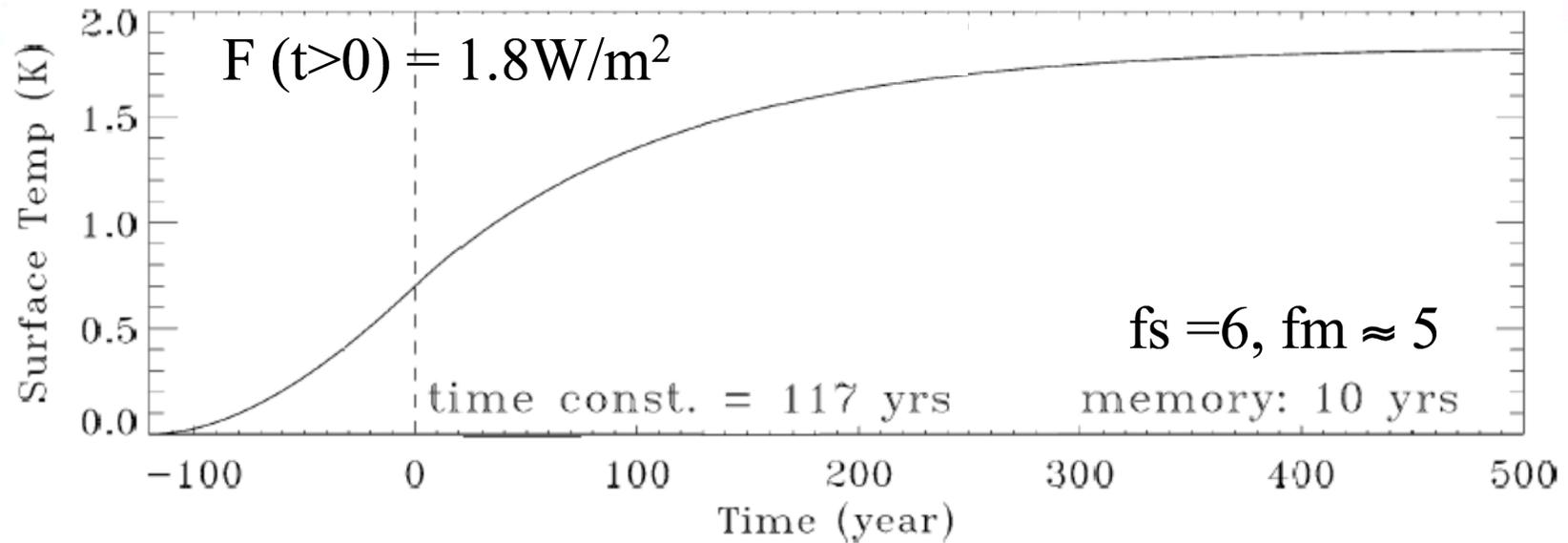
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$$0 = F - f_s T + \frac{f_m}{t_0} T t_0 = F - f_s T + f_m T$$



Results: asymptote

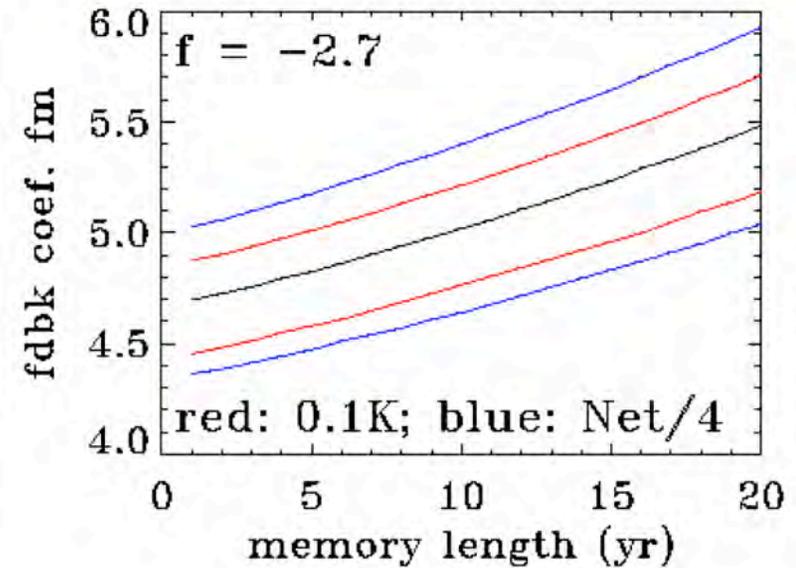
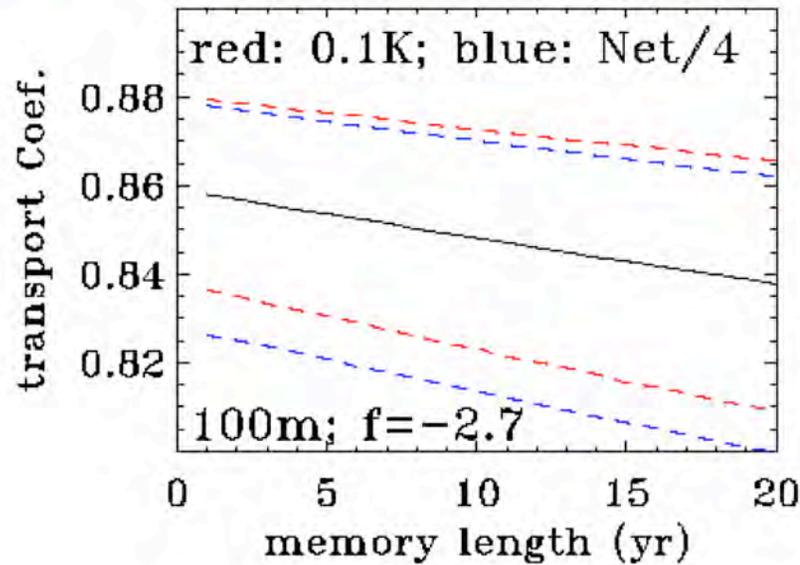


$$0 = F - f_s T + \frac{f_m}{t_0} T t_0 = F - f_s T + f_m T$$

$$T = F / (f_s - f_m) = 1.8 \text{ K}$$

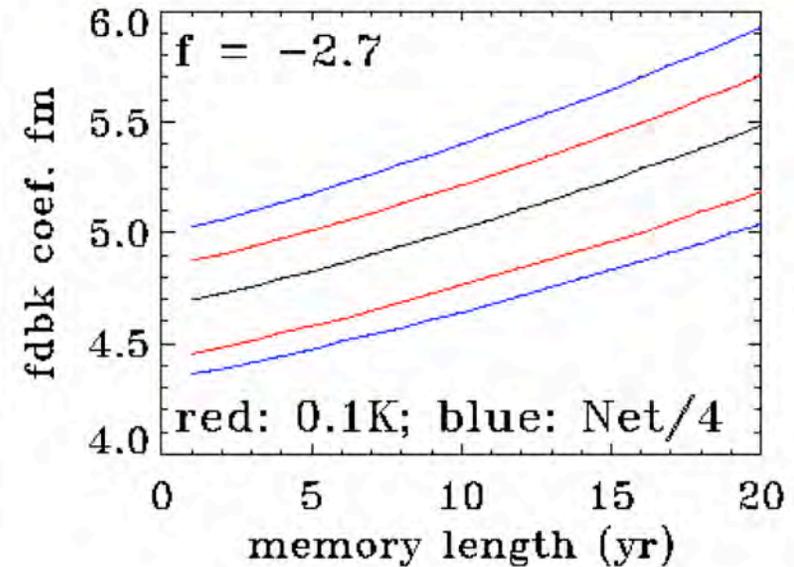
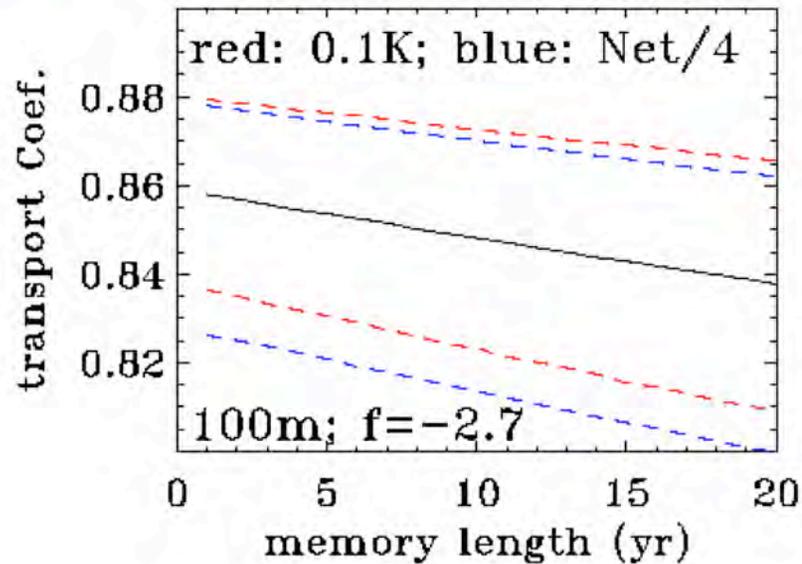


Results: sensitivity on Q and T





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Surface T uncertainty 0.1K → not very sensitive

Q_{net} uncertainty (25% or $\sim 0.2 \text{ W/m}^2$) → sensitive

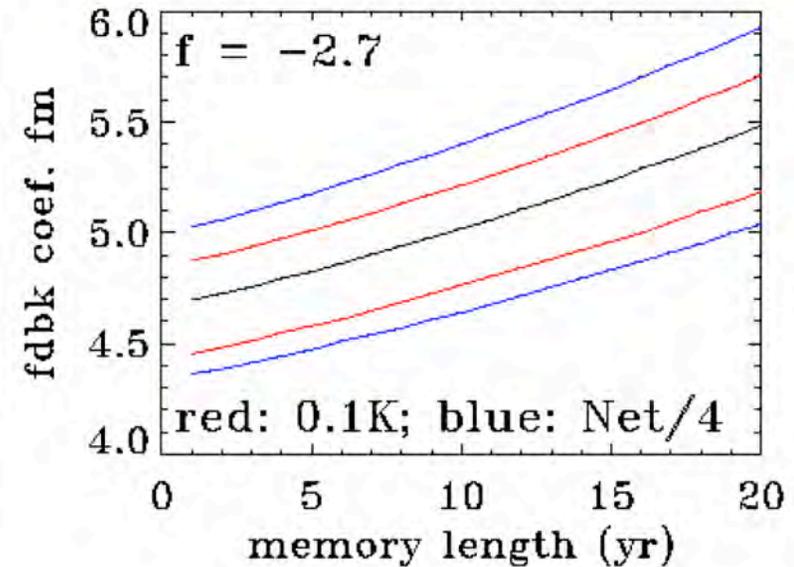
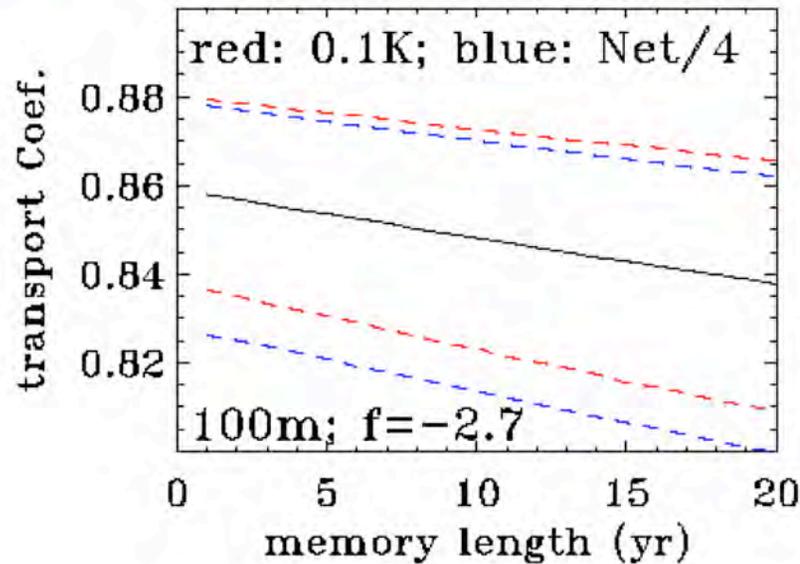
Actual error in TOA net or ocean heat storage change

measurements may be larger or smaller than 0.2 W/m^2 .

Current the best error estimate is about 0.13 W/m^2 ($1-\sigma$).



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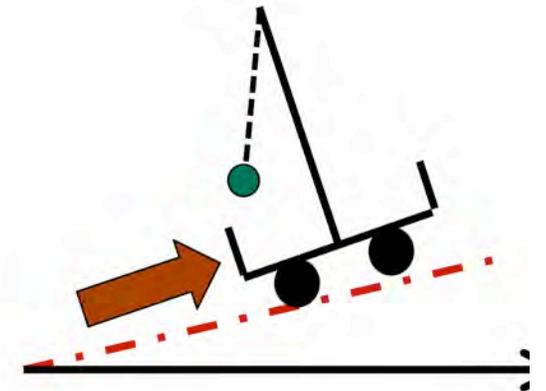
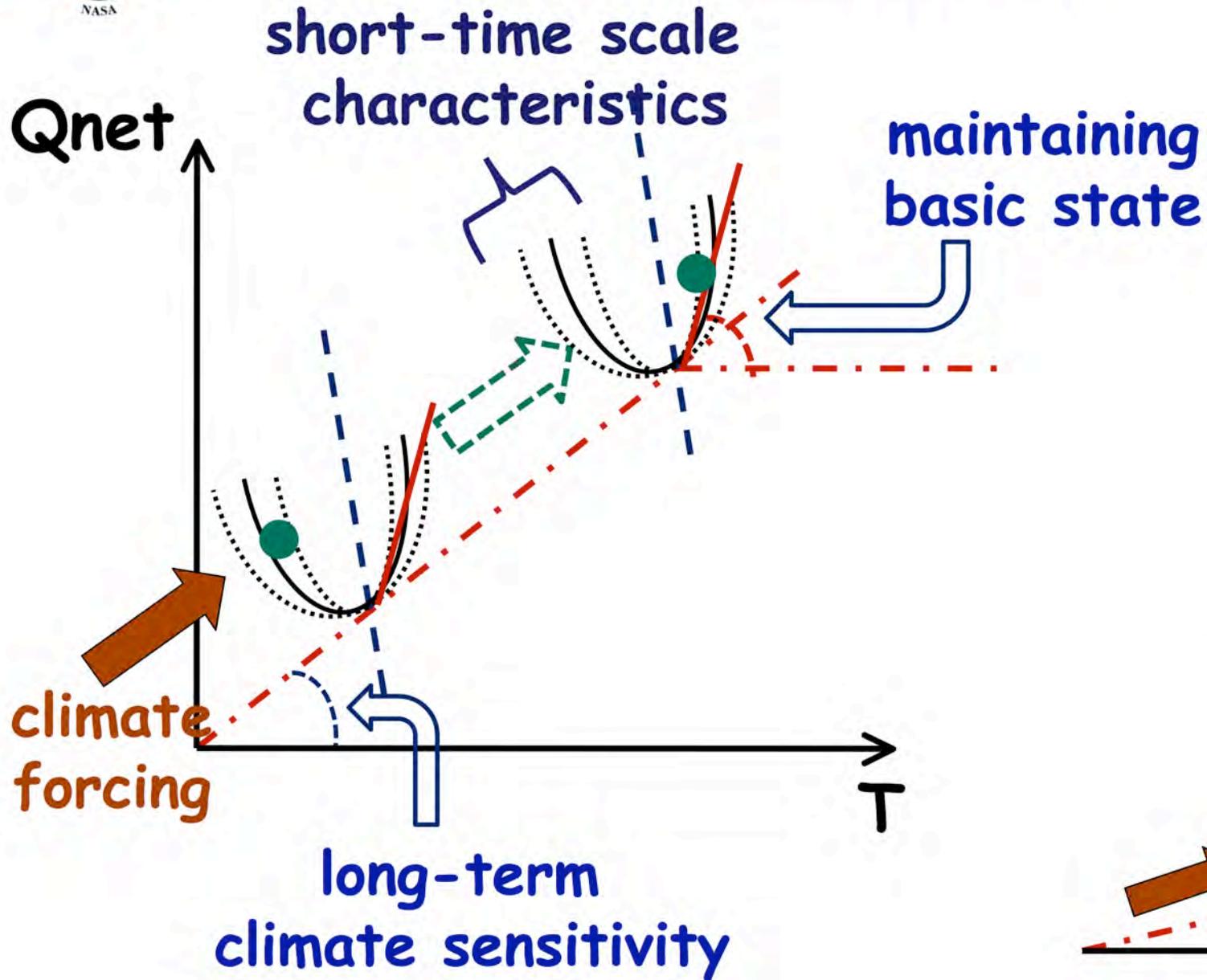
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fm: $4.7 \sim 5.0 \pm 0.26$ ($f_{\text{tot}} = 1.0 \sim 1.3 \pm 0.26$)

$T = 2.85 \sim 3.7 \text{ K}$ (-0.48K & $+1.3\text{K}$; $2 \times \text{CO}_2 = 3.7 \text{ W/m}^2$)



climate sensitivity





Summary



- Energy balance model for explanation of observed TOA net radiation (or ocean heat storage) and surface temperature.
- Major physical processes of the climate system, such as deep ocean heat transport and system memory, are considered.
- Targeted at boundary condition problem instead of classic initial condition solutions. Thus, it is really modeling the climate.
- Cannot use short-time scale climate system adjustment (or relaxation) to mimic climate change: different scales, different physics



Summary



- f_m about 4.7 ~ 5.0 (± 0.26), positive feedback factor 2.0 ~ 2.3. Or, equivalent $2\times\text{CO}_2$ (or 3.7 W/m^2) global warming 2.85 ~ 3.7 K with low & high ends 2.4 & 5.0 K, respectively.
- Time scale much longer than what Schwartz obtained and the system is not in equilibrium (or steady) state
- Key TOA $Q_{\text{net}} = 0.85 \text{ W/m}^2$
- Results: sensitive to Q_{net} values, but not GISS T and short-time scale feedbacks.
- Strong desire for long-term radiation missions with accurate absolute calibrations, such as proposed CLARREO & CERES.



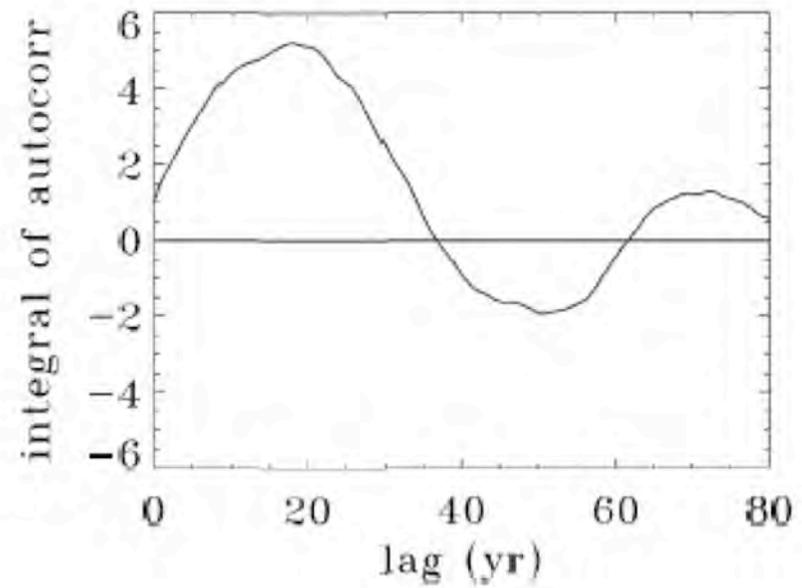
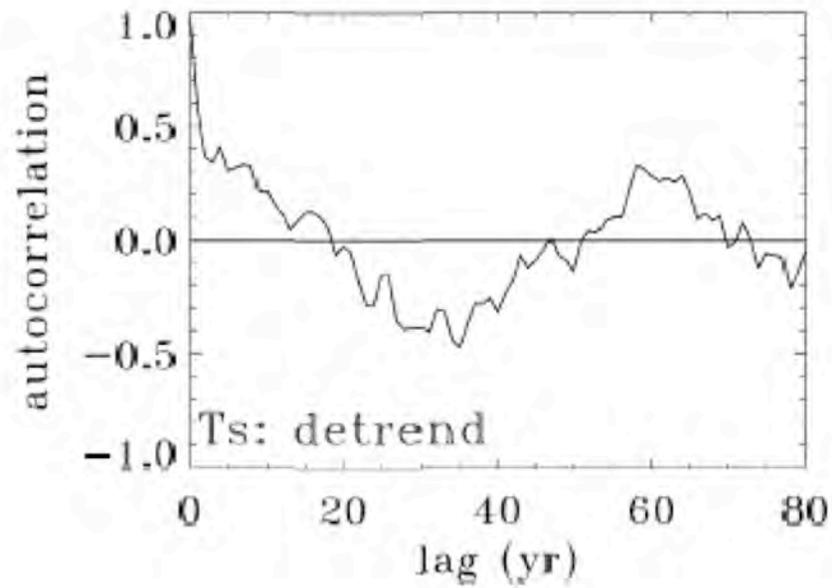
Acknowledgement



Many people, especially David Young, Gary Gibson, and Don Garber, have significant supports for this study.

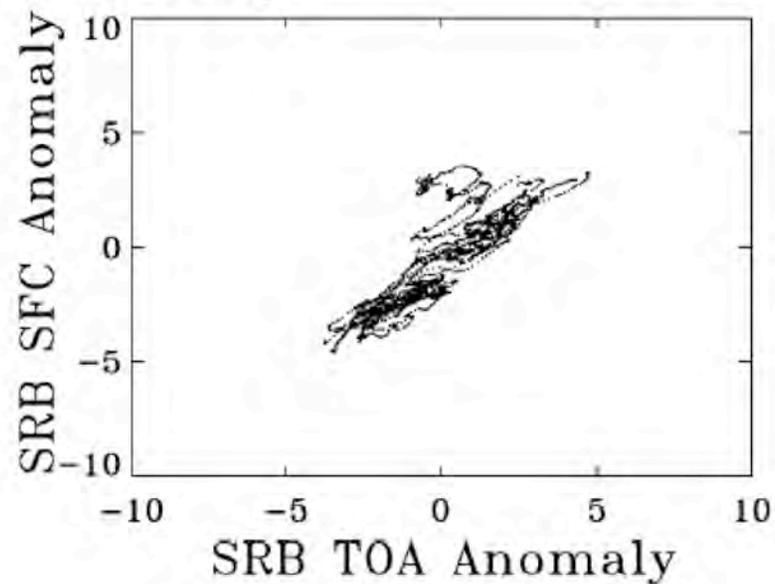
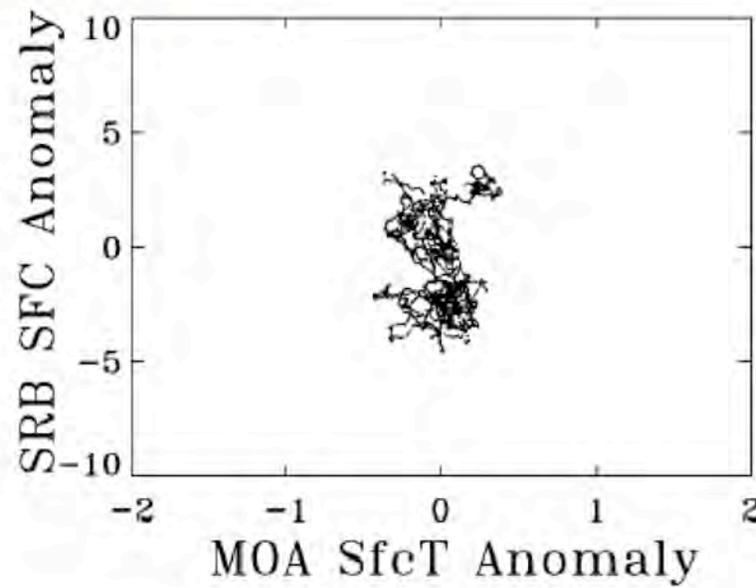
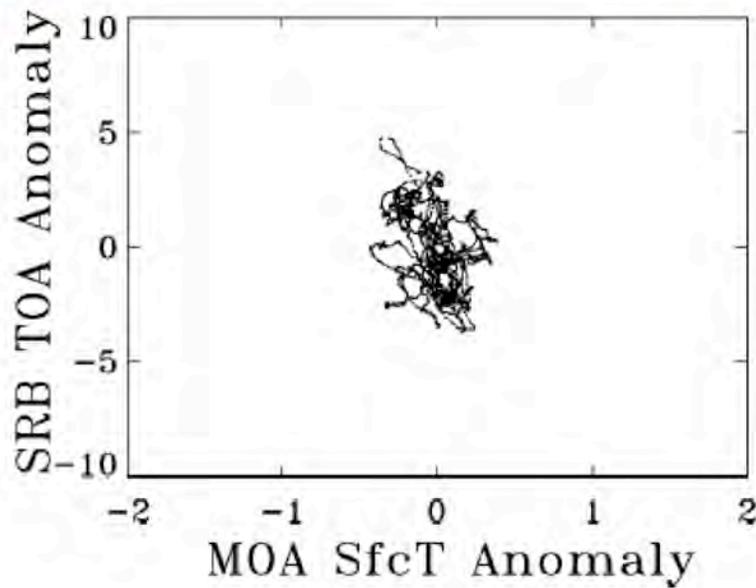


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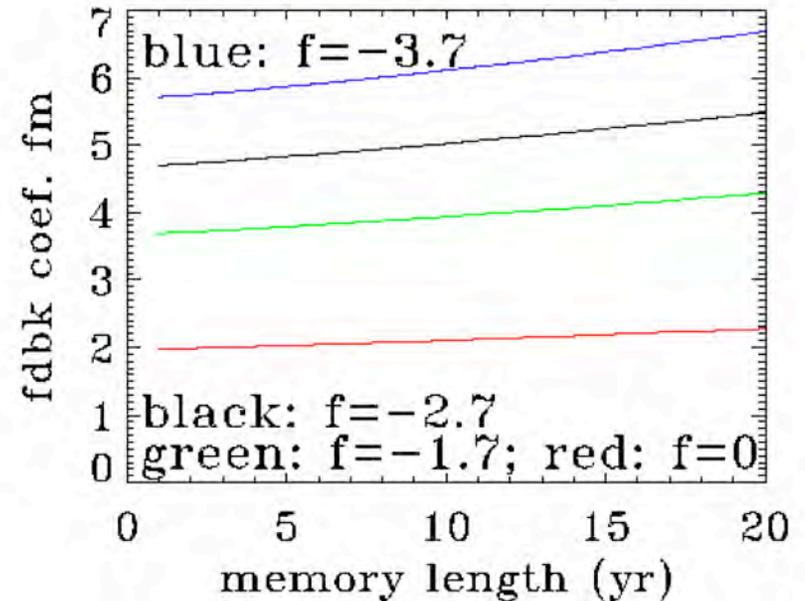
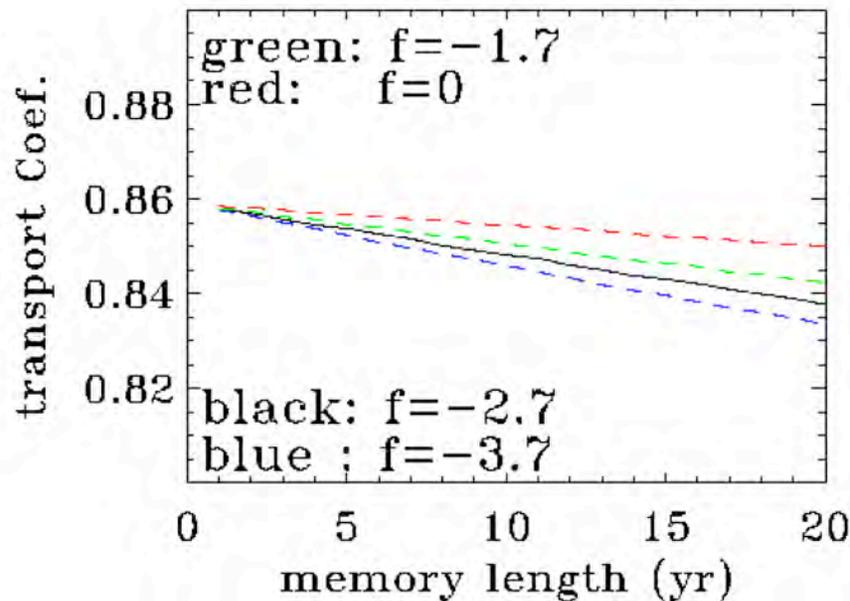


Results





Results: sensitivity on f



These fm values are parallel each other, i.e., total feedback coefficients are almost the same when memory length is fixed.

Thus, final results are not sensitive to short-term f values used.