

# Balancing the Earth's Radiation Budget

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CERES SET November 2007  
Victoria, BC

# Annual Mean Global Average Fluxes

- Ingoing Flux:  $1365/4 = 341.3 \text{ W-m}^{-2}$
- Outgoing Flux:
  - Reflected Shortwave 97.8
  - Outgoing Longwave 237.1
- » -----
- Net Flux: 6.4
- More than we expect for interannual variation!

# Global Imbalance

**The Imbalance is due to the  
accumulation of errors in  
measurement and data product  
generation.**

# Error Sources for Net Radiation Budget (Strawman)

- Gain of Total Channel
- Gain of Shortwave Channel
- LW Spectral Response of Total Channel
- SW Spectral Response of Total Channel
- Spectral Response of Shortwave Channel
- Limb-darkening Function
- BRDF
- Temporal Interpolation of OLR
- Temporal Interpolation of Albedo
- Solar Constant

# Effects of Errors on Budget

- Errors are Small, therefore assume Effects are Linear:

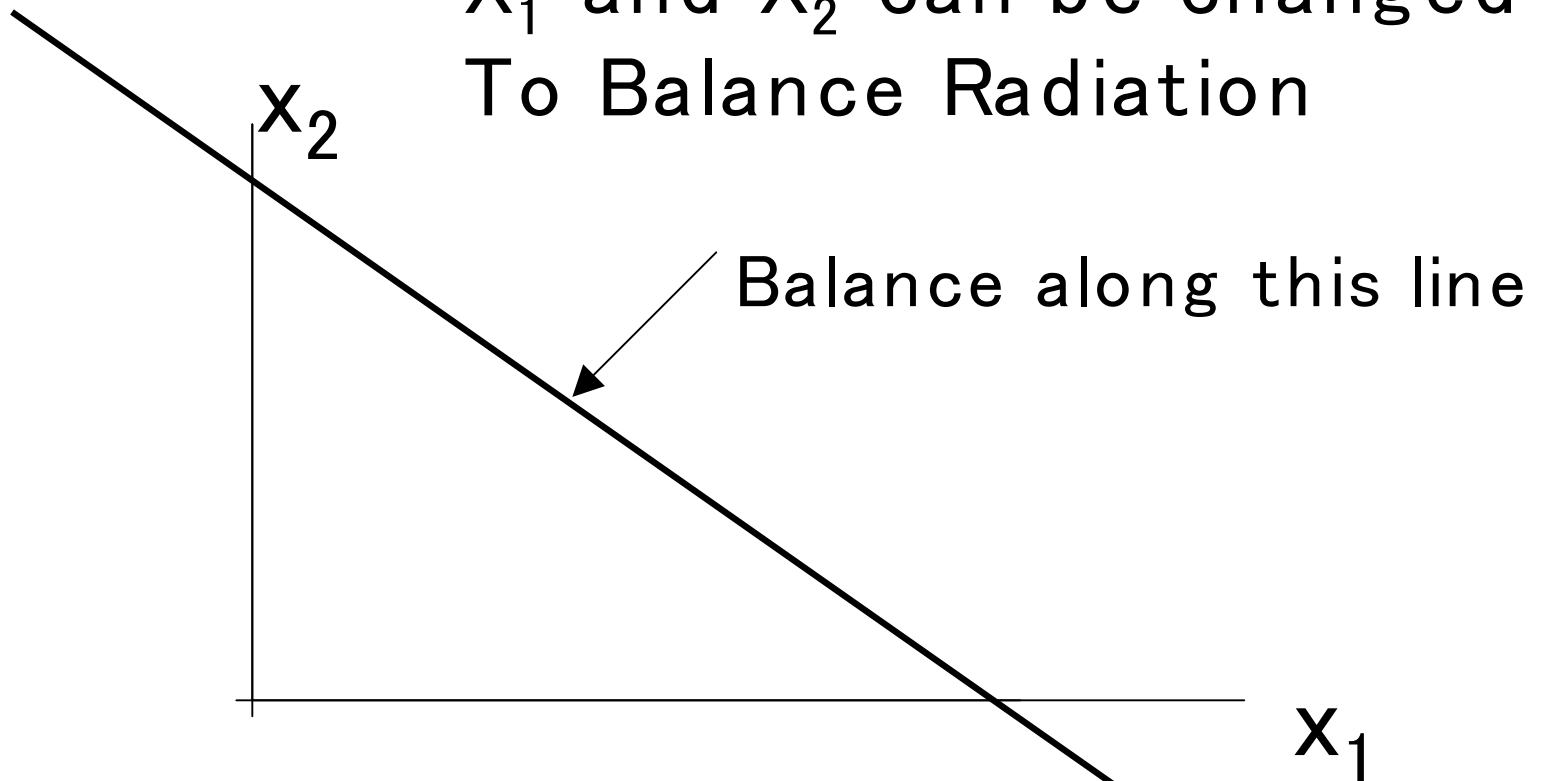
$$\sum A_i X_i = -\epsilon_{RN}$$

$$\text{or } \mathbf{a}^t \mathbf{x} = -\epsilon_{RN}$$

- Here  $A_i$  is Sensitivity of Net Radiation to parameter  $X_i$

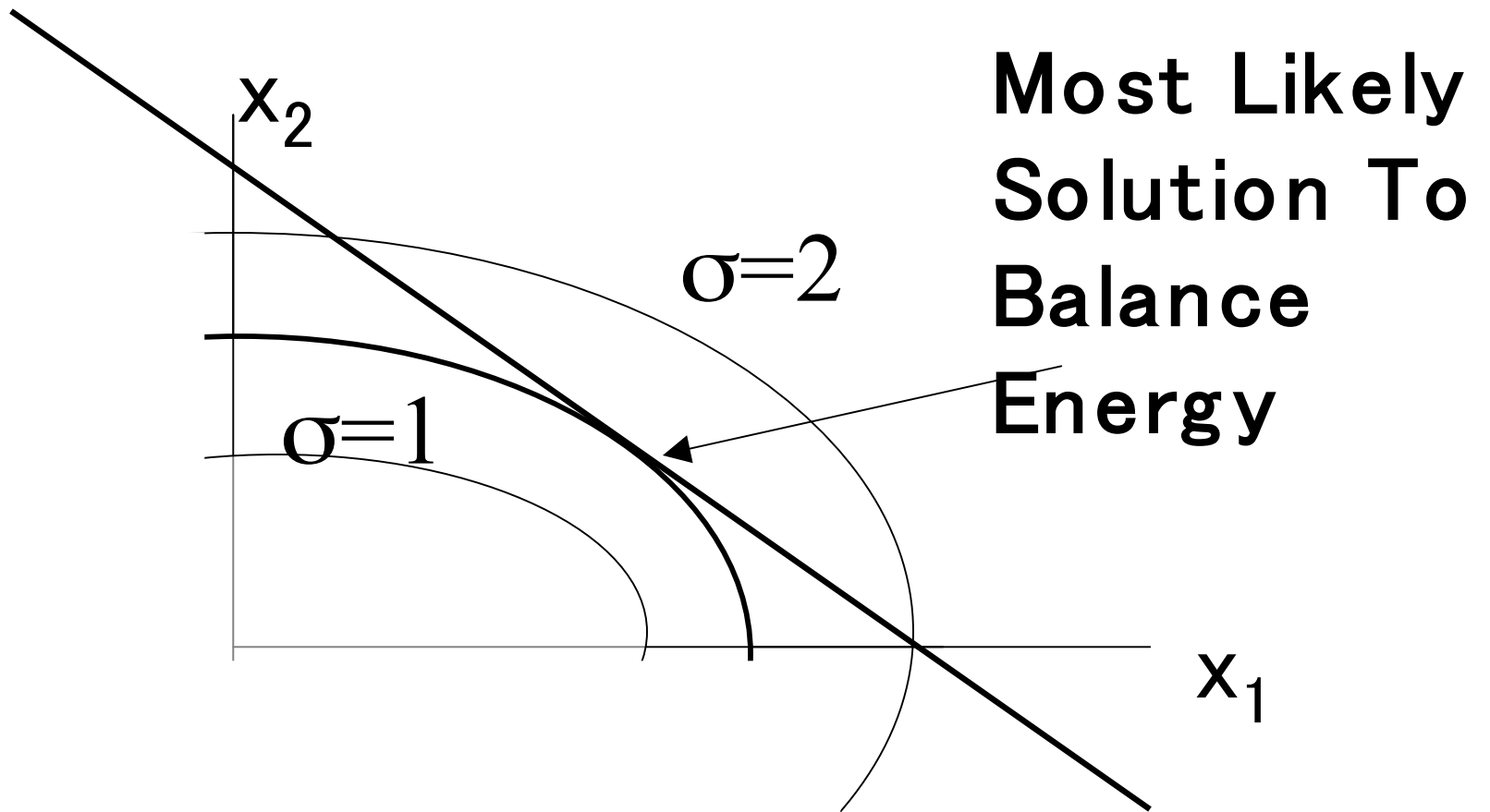
# Consider a 2-Parameter System:

$X_1$  and  $X_2$  can be changed  
To Balance Radiation



Which combination do we select?

Consider Probability of  $X_1 X_2$   
Pair:



# Probability Distribution of X

- Assume X have zero mean
- Assume X Normally Distributed
- $P(x) = M \exp(-x^t C x)$

Where C = Covariance Matrix



# Most Likely Solution to Balance Energy: Equations

- Most Likely Solution is given by minimizing  $-x^t C x$

subject to Constraint  $a^t x = -\varepsilon$

RN

Thus Minimize

$$\Omega = -x^t C x + \lambda a^t x$$

where  $\lambda =$  Lagrangian Multiplier

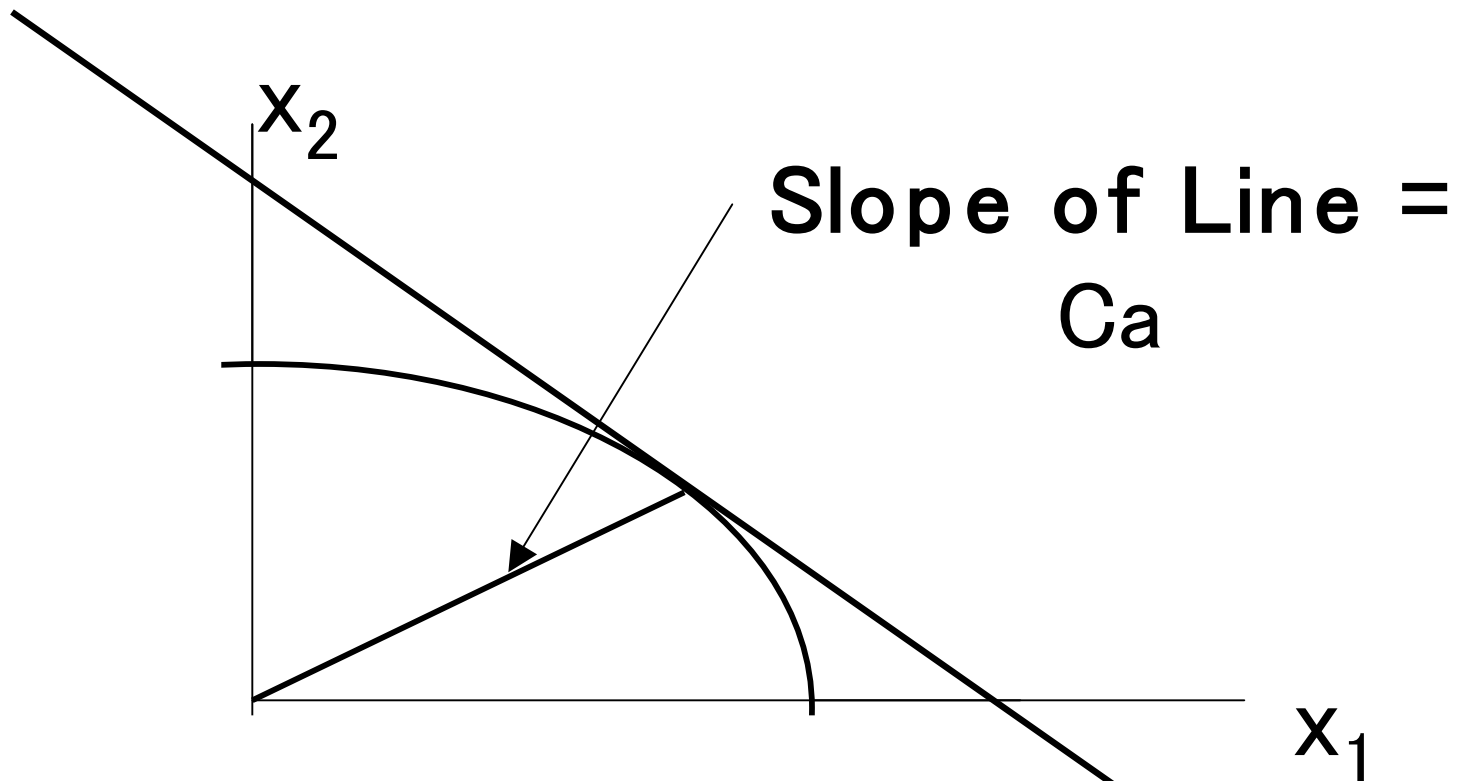
# Most Likely Solution to Balance Energy:

$$x = -\lambda Ca$$

Where

$$\lambda = (a^t Ca)^{-1} \epsilon_{RN}$$

# Most Likely Solution to Balance Energy

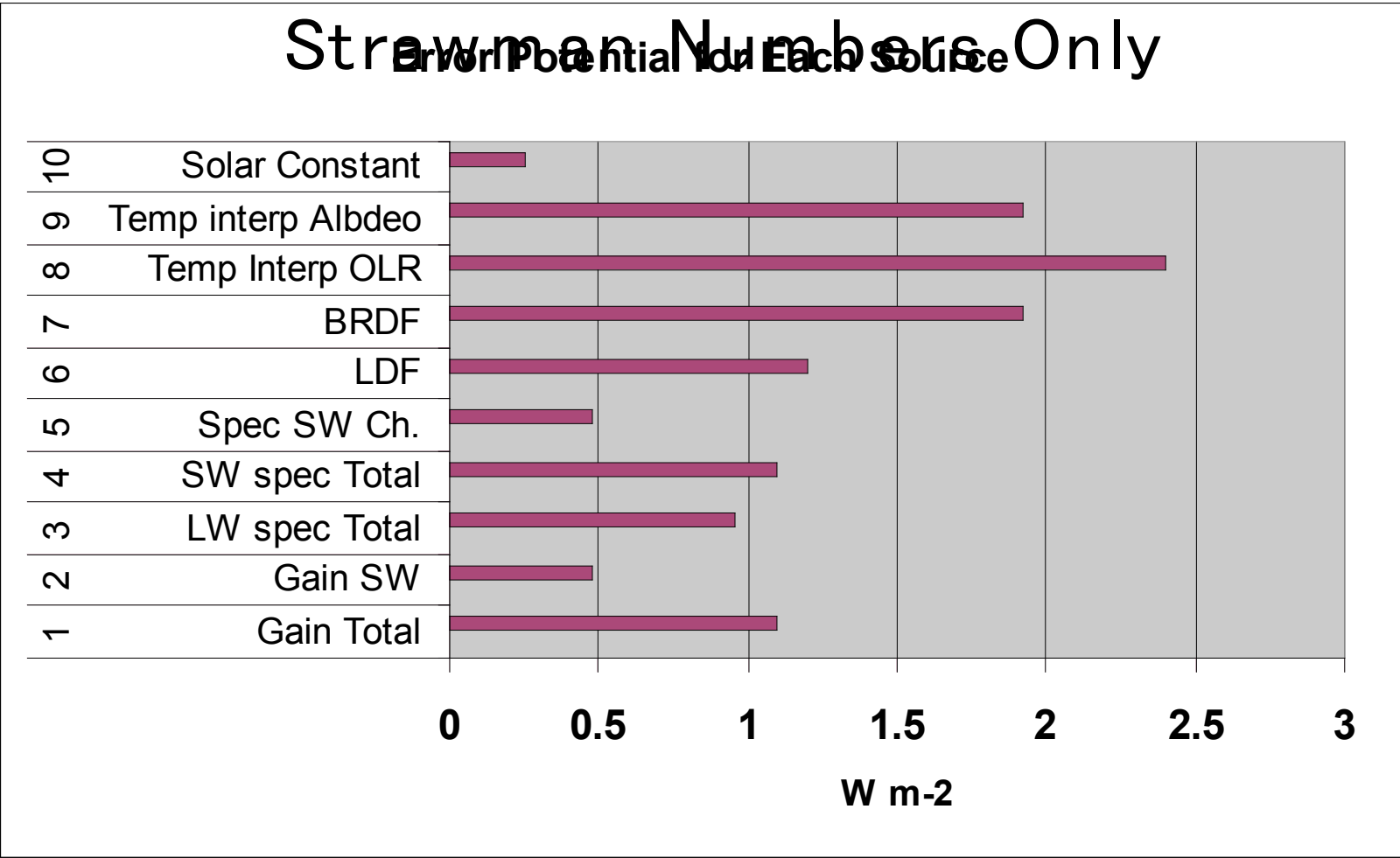


Length is proportional to  $\lambda$

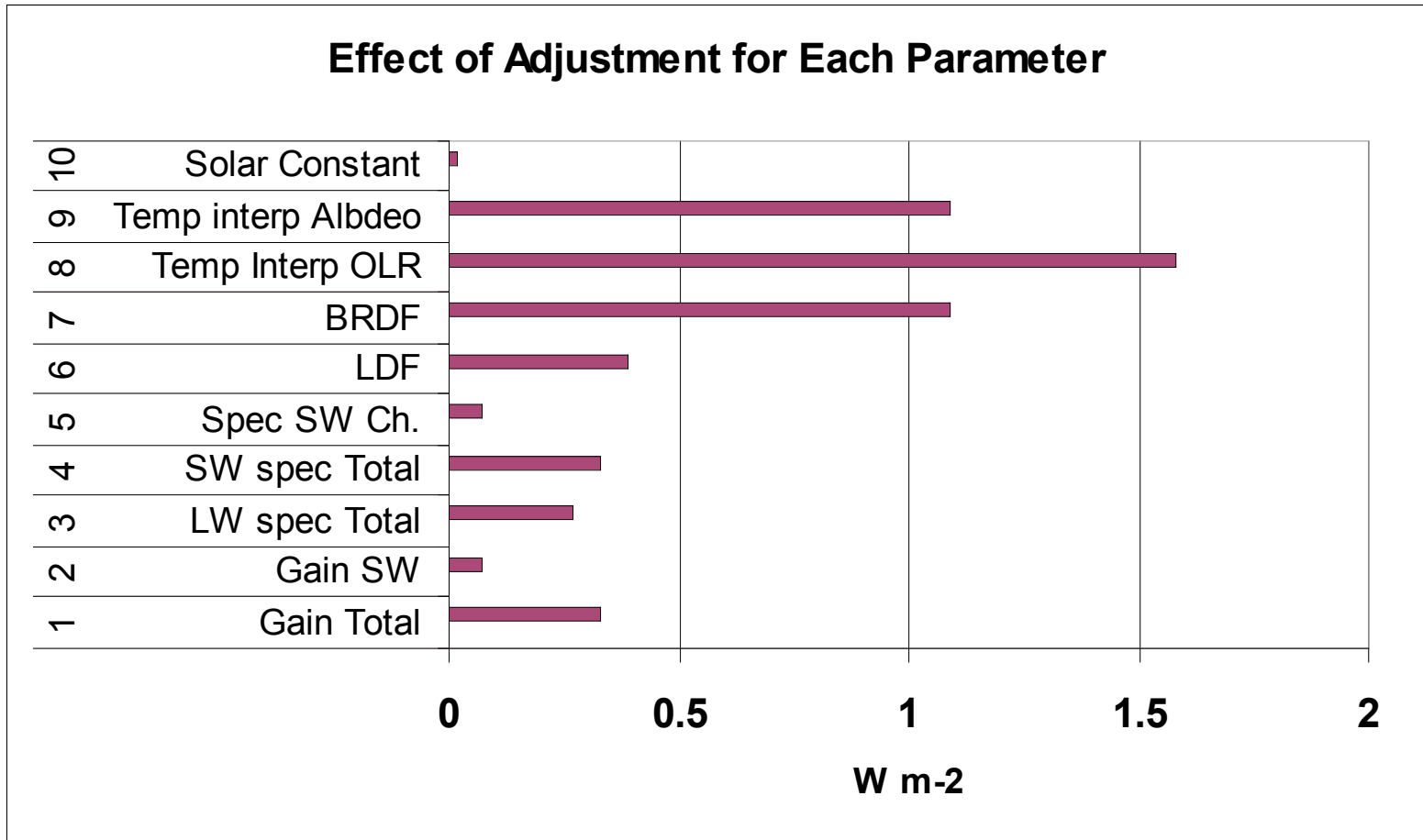
# Input for Balance $\sigma$ Strawman $A_i$

▪ Gain Total Ch., %	0.005	220.
▪ Gain Shortwave Ch. 96.	0.005	
▪ LW Spec. Total Ch.	0.010	96.
▪ SW Spec. Total Ch.	0.005	220.
▪ Spect. Resp. SW Ch.	0.005	96.
▪ Limb-darkening	0.005	240.
▪ BRDF	0.020	96.
▪ Temp. Interp. OLR	0.005	240.
▪ Temp. Interp. Albedo	0.005	96.
▪ Solar Constant $W \cdot m^{-2}$	1.0	.25

# Effect of 1-sigma Change of Each Parameter



# Most Likely Adjustments to Balance Budget: Strawman Only

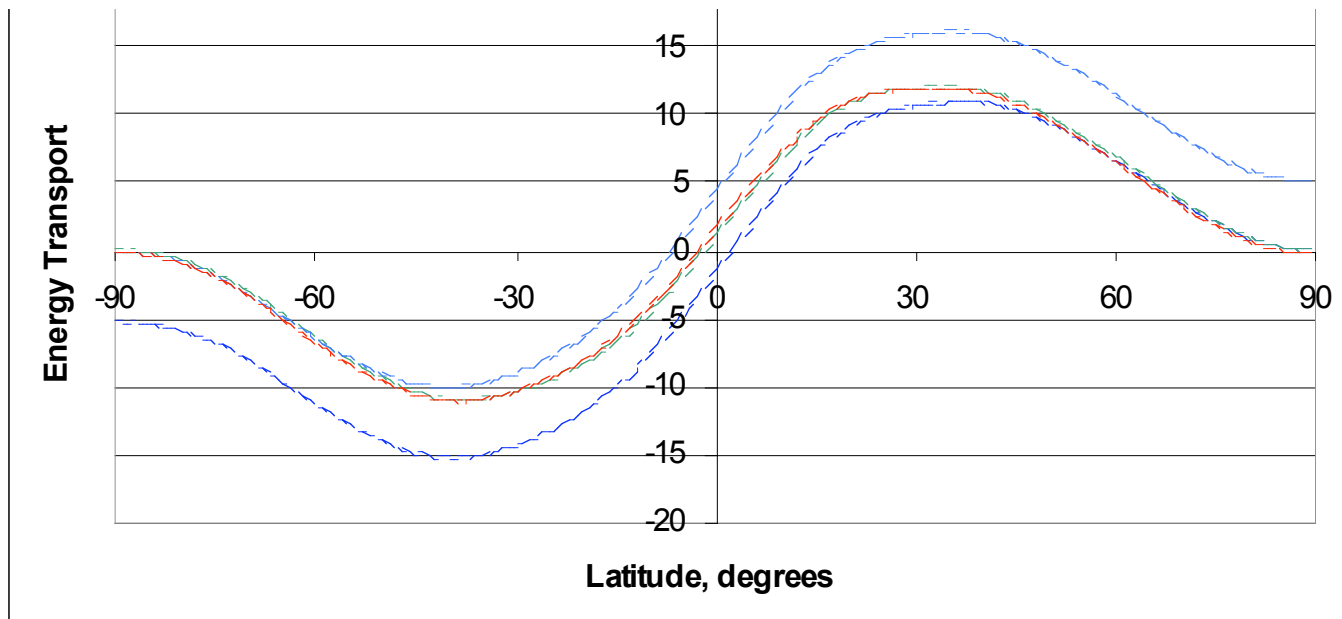


# Computation of Meridional Energy Flux:

## Application of Method

- To get meridional flux, integrate net radiative flux starting at Pole.
- Divide Flux by length of Zone to get Flux Density.
- Computation assumes ZERO Annual Mean Global Average Net Radiative Flux.

# Annual Mean Meridional Energy Flux



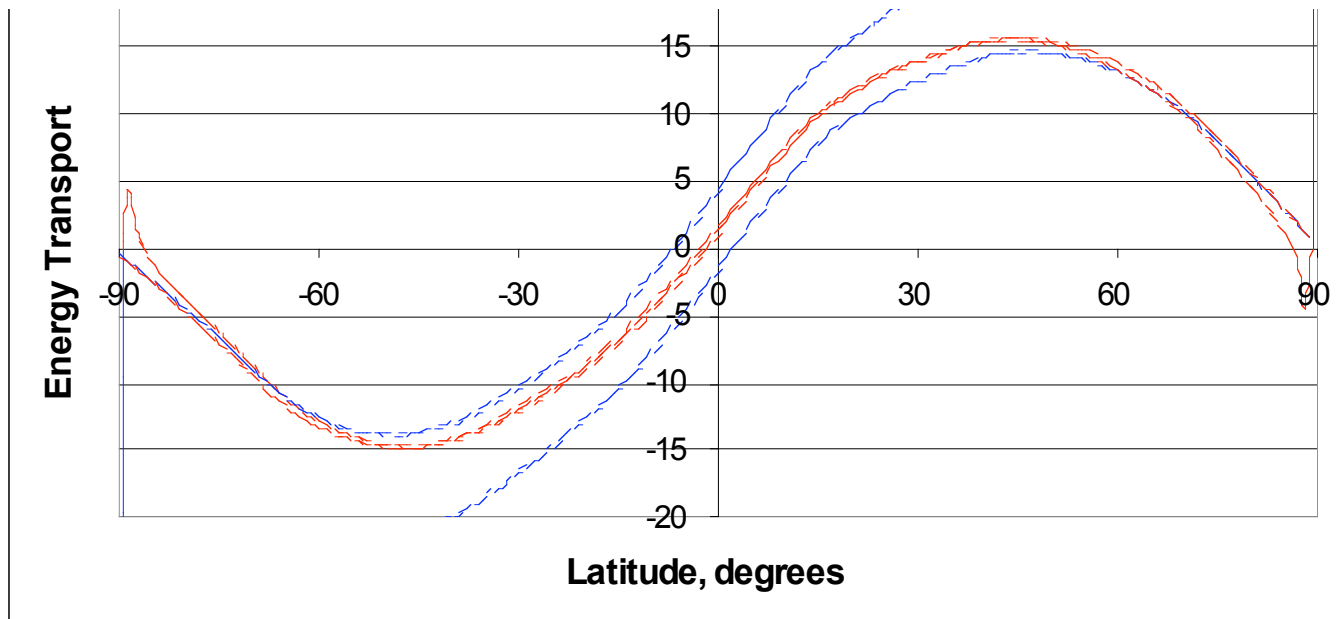
Blue lines: Original data

Red lines: Data Adjusted for Likely Errors

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# Annual Mean Meridional Energy Flux Density



Blue lines: Original data

Red lines: Data Adjusted for Likely Errors

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# Conclusions

- An Algorithm has been Developed for Adjusting Parameters in Data Production for Balancing the Radiation Budget.
- Requires Good Error Input for Valid Results. (Garbage in/Garbage out)
- We need to develop good input for this.